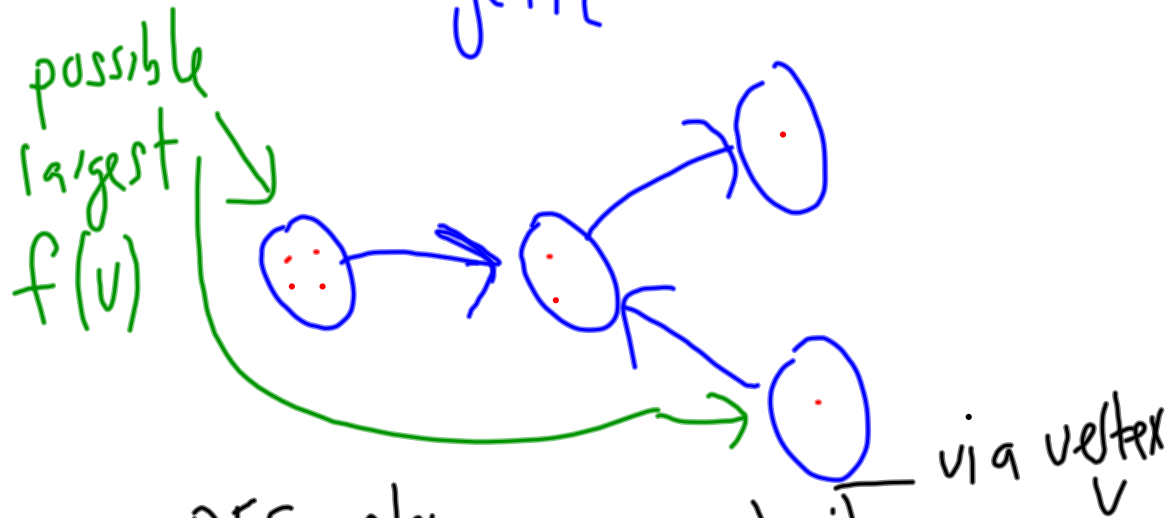


Connected  
components

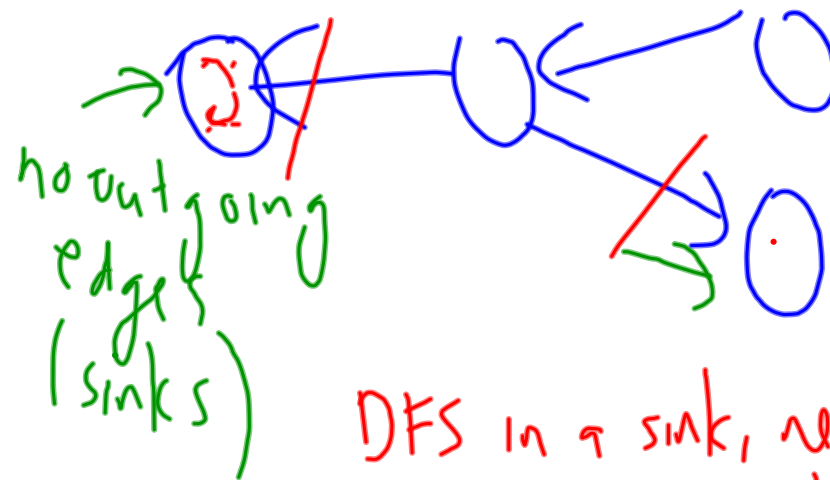
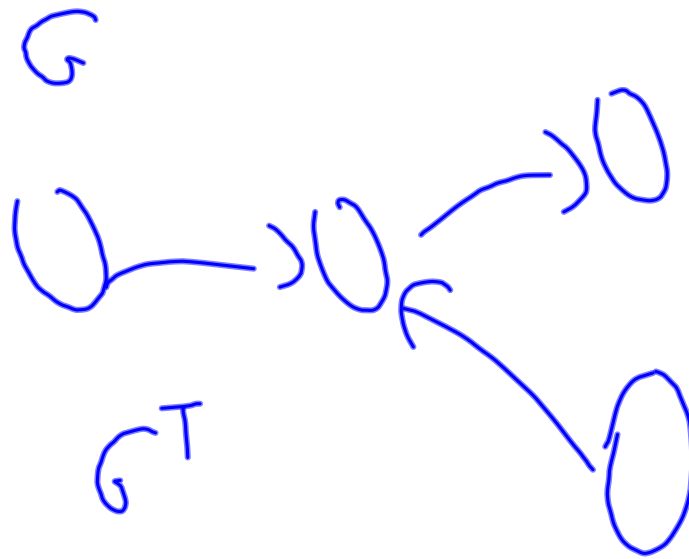
linear  $O(V + E)$

Component graph is acyclic



once DFS enters a component, it discovers all vertices in that component before finishing with  $v$ .

largest finishing time is in a source in the component graph



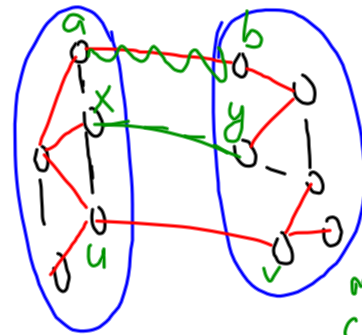
DFS in a sink, never leaves that component

edge in component graph



$$f(x) > f(y)$$

Proof Assume not. There is some cut for which the min. wt. edge is not in the MST. (call the current alleged MST  $T$ )



$(u,v)$  is the min. wt edge in  $T$  crossing the cut

$(x,y)$  is the min wt edge crossing cut

$w(x,y) < w(u,v)$ . Adding  $(x,y)$  to  $T$  creates a cycle which crosses the cut at least twice. Let  $(a,b)$  be an edge besides  $(x,y)$  that crosses the cut. My tree is  $T' = T \cup \{(x,y)\} - (a,b)$

$$w(T') = w(T) + w(x,y) - w(a,b)$$

$$\text{but } w(x,y) < w(a,b)$$

$\therefore w(T') < w(T)$  contradicts  $T$  being an MST.

