



Finite  
State Control

Poly time on a TM

= Poly time on any Digital  
Computer



$b=3$

$S: ((s,b), (b,t))$  Yes

$S: ((s,a), (a,t))$  No

$S: ((s,a), (b,t))$  No

You can verify Longest Path  
in Polynomial time.

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SAT CNF (and of  
0/1's)

$$\Phi \equiv (X_1 \vee X_2) \wedge (\bar{X}_1 \vee X_3 \vee \bar{X}_4) \wedge (\bar{X}_2 \vee \bar{X}_4)$$

Is there a setting of the variables that  
makes  $\Phi$  true  
Yes

TFTF

$$\Phi \equiv (X_1 \vee X_2) \wedge (\bar{X}_1 \vee X_2) \wedge (X_1 \vee \bar{X}_2) \wedge (\bar{X}_1 \vee \bar{X}_2)$$

No  
SAT is verifiable in poly time.  $\therefore \text{SAT} \in \text{NP}$

Are there problems that can  
be verified in poly time,  
but cannot be solved in  
poly time?

unanswered

Y subtraction of 2 ints

X addition of 2 ints

input y to Y (6, 4)

$$f(y) = (6, -4)$$

$$f(y) \text{ input to addition} \rightarrow 6 + -4 = 2$$

If  $Y \leq X$  then  $X \in P \Rightarrow Y \in P$   
Pf  $Y \notin P \Rightarrow X \notin P$

