Using this probability and the energy dependence of $\mathbf{Z}_{\mathrm{AB}}$ derived from the Boltzmann distribution, the reaction rate can be obtained. The result is:

Where $\mathbb{Z}_{\mathrm{AB}}=\pi\left(\sigma_{\mathrm{AB}}\right)^{2}<\mathrm{u}_{\text {rel }}>\left(\mathrm{N}_{\mathrm{A}} / \mathrm{V}\right)\left(\mathrm{N}_{\mathrm{B}} / \mathrm{V}\right)$

$$
\left.\mathbf{R}=\left\{\begin{array}{ll}
\pi(\sigma & \mathbf{A B}
\end{array}\right)^{2}<\mathbf{u}_{\text {rel }}>\mathrm{e}^{-\mathrm{E}_{\mathbf{A}} / \mathbf{R T}}\right\}\left(\mathbf{N}_{\mathbf{A}} / \mathbf{V}\right)\left(\mathbf{N}_{\mathbf{B}} / \mathbf{V}\right)
$$

Often $k_{R}$ is written $k_{R}=A e^{-E_{A} / R T}$

Since $<\mathbf{u}_{\text {rel }}>=(8 \mathrm{kT} / \pi \mu)^{1 / 2}$, A increases linearly with square root of $T$.

## Temperature Dependence of $\mathrm{k}_{\mathrm{R}}$

There are two places where $T$ comes into the expression for $k_{R}$

## Orientation Effects: The Steric Factor

We have left out one consideration in our model for $\mathbf{R}$, the reaction rate.

For example, in the reaction of $\mathrm{NO}+\mathrm{O}_{2}$ to form $\mathrm{NO}_{2}$, the one O from $\mathrm{O}_{2}$ must attach to the N in NO , not the O in NO !

Might expect collisions between NO and $\mathrm{O}_{2}$ that occur at the nitrogen end of NO will be more effective in producing $\mathrm{NO}_{2}$ than collisions at the $O$ end of NO!
$\mathrm{O} \mathrm{N}+\mathrm{O} \mathrm{Cl} \longrightarrow$ No reaction

## $\mathrm{ClNO}+\mathrm{ClNO} \rightarrow \mathrm{Cl}_{2}+2 \mathrm{NO}$



## Bonus * Bonus * Bonus * Bonus * Bonus * Bonus

## Units (cgs) and typical numbers:

## Chemical Kinetics: Laboratory Measurements

We now have a model for chemical reactions (Binary Collision Model) and need to deal with practical issue of how to make observations in the laboratory.

This will involve both analyzing chemical reaction data from laboratory measurements and extending our models.
A) Consider the reaction
$2 \mathrm{~A} \rightarrow \mathrm{~B}+\mathrm{C}$

Rate $\equiv$ time rate of change of concentration of any of the substances involved - reactants or products.

Usual convention: $R=-\frac{1}{2} \frac{d_{A}}{d t}=\frac{\mathrm{dC}_{\mathrm{B}}}{\mathrm{dt}}=\frac{\mathrm{dC}_{\mathrm{C}}}{\mathrm{dt}}$

Could measure the rate by measuring the composition of the reaction vessel as a function of time. Example:

$$
\begin{array}{llc}
\mathbf{t}=\mathbf{0} & \mathbf{N}_{\mathbf{A}}{ }^{\mathbf{o}}=\text { moles } \mathbf{A} & \mathbf{N}_{\mathbf{B}}{ }^{0}=\mathbf{N}_{\mathbf{C}}{ }^{0}=\mathbf{0} \\
\mathbf{t}=\mathbf{t}_{\mathbf{1}} & \mathbf{N}_{\mathbf{A}}{ }^{\prime}=\text { moles } \mathbf{A} & \mathbf{N}_{\mathbf{B}}^{\prime}=\mathbf{N}_{\mathbf{C}}^{\prime}=\text { moles } \mathbf{B}, \mathbf{C}
\end{array}
$$

Consider the reaction $2 \mathrm{~A} \rightarrow \mathrm{~B}+\mathrm{C}$

## Consider the reaction $2 \mathrm{~A} \rightarrow \mathrm{~B}+\mathrm{C}$

Two moles of A gives one mole of B. Or moles of $B$ formed must equal half the number of moles of $A$ reacted.

$$
\begin{array}{ccc}
\mathbf{t}=\mathbf{0} & \mathbf{N}_{\mathbf{A}}^{0}=\text { moles } \mathbf{A} & \mathbf{N}_{\mathbf{B}}^{0}=\mathbf{N}_{\mathbf{C}}^{0}=\mathbf{0} \\
\mathbf{t}=\mathbf{t}_{\mathbf{1}} & \mathbf{N}_{\mathbf{A}}{ }^{\prime}=\text { moles } \mathbf{A} & \mathbf{N}_{\mathbf{B}}{ }^{\prime}=\mathbf{N}_{\mathbf{C}}{ }^{\prime}=\text { moles } \mathbf{B}, \mathbf{C}
\end{array}
$$

Take deerivative of both sides with respect to $t \rightarrow$

## Consider the reaction $2 \mathrm{~A} \rightarrow \mathrm{~B}+\mathrm{C}$



In general the rate for such a reaction turns out to be a function of the concentrations of all of the substances involved
f could have any form. In many cases $f$ has the form
$k$ is a constant called the rate constant. $\alpha$ is the order of the reaction for the component $A$

$$
\alpha=1 \equiv 1^{\text {st }} \text { order in } A
$$

$$
\alpha=3 \equiv 3^{\text {rd }} \text { order in } A
$$

Overall order of a reaction $=$
$\alpha+\beta+\gamma$. The order has absolutely nothing to do with the stoichiometry of the reaction,

The point is that one knows nothing about $\alpha, \beta, \gamma$ from looking at the chemical equation for the reaction.

