# SELECTION, LEVERAGE, AND DEFAULT IN THE MORTGAGE MARKET\*

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#### **Abstract**

We ask whether the correlation between mortgage leverage and default is due to moral hazard—the causal effect of leverage—or adverse selection: ex-ante risky borrowers choosing larger loans. We separate these information asymmetries using a natural experiment resulting from (i) the unique contract structure of Option Adjustable-Rate Mortgages and (ii) the unexpected 2008 divergence of the indices that determine interest rate adjustments. Moral hazard is responsible for 60-70% of the correlation, while adverse selection explains 30-40%. We construct and calibrate a simple model to show that optimal regulation of leverage must weigh default-prevention against market distortions due to adverse selection.

JEL classification: D14, G21, D82

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# 1 Introduction

In the years since the financial crisis household leverage—particularly vis-á-vis mortgage debt—has come into focus as a critical element of financial stability.<sup>1</sup> In turn, policymakers have become increasingly concerned with (i) the determinants of leverage in mortgage markets and (ii) the consequences of macroprudential regulations on borrowing.<sup>2</sup> While classic theories suggest that information asymmetries between borrowers and lenders should have first order implications for both,<sup>3</sup> evidence on the empirical relevance of adverse selection in *any* credit market is difficult to come by.

In this paper we develop a strategy to explicitly test for adverse selection in the mortgage market. We then use our findings to highlight the complications selection poses for macroprudential policy. Our approach starts with a simple stylized fact: highly leveraged borrowers tend to default more frequently. The key challenge lies in determining whether this is the result of adverse selection—unobservably "risky" borrowers choosing high leverage mortgages—or whether it simply reflects a causal effect of leverage on default. This second explanation is often referred to as moral hazard. Typically, the two alternatives are observationally equivalent in the data.

Our research design exploits a natural experiment generated by the unique contract structure of Option Adjustable-Rate Mortgages (Option ARMs). These loans typically have interest rate adjustments tied to either LIBOR or Treasury rates. Though the choice between LIBOR and Treasury was not salient prior to the financial crisis, the unexpected divergence of these two financial indexes in 2008 caused borrowers who chose otherwise identical contracts to owe substantially different amounts ex-post. This variation allows us to (i) isolate moral hazard by comparing borrowers with identical initial leverage choices but different realized home equity, and (ii) identify adverse selection by comparing borrowers with different initial leverage choices but the same realized home equity.

Identifying adverse selection is crucial for understanding how the *supply* of leverage—whether a lender is willing to offer a given leverage ratio, and if so, at what interest rate—is determined in equilibrium. With adverse selection, lenders may be unable to provide the safest borrowers large loans at a fair price and/or leverage may act as a screening device to differentiate riskier types (as in models following Bester, 1985). As a result, even minor policy changes may significantly reshape the set of contracts lenders offer—with implications that differ sharply from a world with symmetric information. For instance, our analysis shows that a regulator who ignores the presence of adverse selection will (i) *overestimate* the reduction in defaults

<sup>&</sup>lt;sup>1</sup>See, for example, Geanakoplos and Pedersen (2012); Mian and Sufi (2015); Korinek and Simsek (2016)

<sup>&</sup>lt;sup>2</sup>A wave of recent academic research has accompanied this policy interest, see Corbae and Quintin (2015), Gete and Reher (2016), DeFusco, Johnson and Mondragon (2017), and Bailey et al. (2017).

<sup>&</sup>lt;sup>3</sup>e.g. Bester (1985).

<sup>&</sup>lt;sup>4</sup>This terminology in credit markets is used, for example, by Adams, Einav and Levin (2009).

generated by macroprudential restrictions on household leverage and (ii) *underestimate* the corresponding costs to borrowers, who all face higher interest rates and choose smaller loans in equilibrium.

The paper begins with a simple conceptual framework to clarify the sources of adverse selection and moral hazard in mortgage markets. The presence of moral hazard is a standard feature of many models of mortgage default (e.g. Campbell and Cocco, 2015). Because lenders face limited access to effective recourse, home equity (or a lack thereof) is a key driver of a borrower's choice to default. However, a large literature (e.g. Deng, Quigley and Van Order, 2000) has documented notable heterogeneity in this relationship across borrowers. Some "risky" borrowers default as soon as the home is worth less than than the mortgage balance whereas others will not to default until the balance significantly outweighs the value of the home. Adverse selection arises precisely when this heterogeneity is correlated with *demand* for leverage—that is, when those who are quickest to default (for unobservable reasons) also prefer larger loans.<sup>5</sup>

We then turn to our primary empirical exercise: disentangling adverse selection from moral hazard. The logic of our approach comes in recognizing that the two give distinct empirical predictions, as in Karlan and Zinman (2009). Adverse selection implies a correlation between default and a borrowers initial leverage choice—independent of the home equity a borrower actually faces. Conversely, moral hazard implies a positive correlation between default and a borrowers realized home equity—regardless of initial leverage. As a result, it is possible to separately identify the two if there is exogenous variation in borrowers' equity that is distinct from their initial leverage choices.<sup>6</sup>

In our context, the divergence of LIBOR and Treasury rates generate exactly this sort of variation. This is due to two features of Option ARMs, which have *fixed minimum payments* in the early years of the loan, but *interest rates that update monthly*. As a result, fluctuations in interest rates generate meaningful changes in the balances borrowers will ultimately owe, without impacting the amount they must pay in the short term. An identical borrower will receive different path of interest rates—and hence a different realized level of home equity—depending on (i) the loan's origination month and (ii) whether it is indexed to a LIBOR or Treasury rate.

Our analysis instruments for a borrower's home equity with the interaction between the loan's financial index and origination month, effectively a form of difference-in-difference variation. Using this strategy, we estimate that moral hazard is responsible for 60-70 percent of the baseline correlation between leverage

<sup>&</sup>lt;sup>5</sup>This framing is analogous to a model of selection on ex-post moral hazard, as in Einav et al. (2013).

<sup>&</sup>lt;sup>6</sup>A natural way to understand these implications is through a set of ideal experiments. To identify adverse selection, we would ideally reassign borrowers who have endogenously chosen different leverage to owe identical balances. A remaining correlation between the initial leverage choice and default would indicate selection. For moral hazard, the ideal experiment would randomly reassign borrowers who have chosen identical leverage to owe *different* balances. A correlation between these randomly assigned balances and default would then reflect a causal effect.

<sup>&</sup>lt;sup>7</sup>While a standard adjustable-rate product might adjust payments to adjust to account for interest accrual, for Option ARMs any excess accrual is absorbed into the balance.

and default, while adverse selection is responsible for the remaining 30-40 percent. Our results imply, for example, that a 10-point reduction in a borrower's loan-to-value ratio two years after origination would reduce the average probability of default by over 4 percentage points.

The fixed (and unusually small) minimum payments for Option ARMs facilitate our analysis by allowing us to set aside the role of monthly payments in the default decision. However, doing so may limit our ability to extend our insights to the broader market, where borrowers short term liquidity concerns may play an important role. Borrowers with high original leverage typically must make larger payments. These borrowers may therefore default because they chose to not—or cannot—make those payments. A potential concern is that the role of monthly payments might be so strong as to render concerns regarding adverse selection second order from a policy perspective.

To address the role of monthly payments—and to show that our estimates extrapolate to the mortgage market more generally—we utilize a similar identification strategy in a large sample of more traditional hybrid adjustable rate mortgages. For these loans, the divergence of LIBOR and Treasury rates led to sharp changes in monthly payments for similar borrowers, without impacting home equity. We use this variation to estimate the impact of monthly payments on default. We find that a \$200 increase in borrowers payments, sustained over a year, increase the probability of default by approximately 1 percentage point. We then use these estimates to understand the relative importance of payments in comparison to adverse selection and moral hazard. In this sample we find that monthly payments and moral hazard are approximately equally important in explaining the correlation between leverage and default. Furthermore, the relative roles of moral hazard and adverse selection are similar to the decomposition we provide for Option ARMs. These results suggest that all three channels are of first order importance from a policy perspective and that our overall results are not specific to the sample of borrowers choosing Option ARMs.

Following the empirical analysis, our final step considers the implications of our findings from a regulatory perspective. Our estimates of the impacts of changes in home equity and monthly payments on default are directly policy relevant. These quantify the effectiveness of ex-post policies that relieve borrowers' balances or reduce payment sizes, respectively. However, understanding the impact of ex-ante regulation in the presence of adverse selection is more challenging. While it is clear that restrictions on mortgage contracts may have profoundly different impacts on equilibrium with and without adverse selection, there is no standard framework to evaluate such policies. Even the appropriate characterization of equilibrium in competitive contexts with adverse selection is controversial, and equilibria may fail to exist under conventional definitions.<sup>8</sup>

To assess ex-ante regulations, we develop a stylized structural model and calibrate it using our esti-

<sup>&</sup>lt;sup>8</sup>e.g. Rothschild-Stiglitz.

mates. To ensure the existence of equilibrium, we use the robust equilibrium concept recently proposed by Azevedo and Gottlieb (2017). We consider, as an example, the impact of a loan-to-value cap—a widely used policy tool intended to reduce mortgage defaults by restricting leverage. We find that this policy is indeed effective in limiting defaults, but to a lesser extent than a naive regulator who ignores the presence of adverse selection would expect. Furthermore, adverse selection generates unexpected welfare losses due to knock on effects. While the regulation only mechanically forces the risky borrowers initially above the cap to take smaller loans, its effects ultimately propagate through the entire distribution. Safer borrowers initially below the cap also choose to take less leverage in order to maintain separation from riskier types and obtain suitably low interest rates. We find that, in equilibrium, interest rates rise across the whole loan-to-value distribution and all borrowers choose smaller loans. A regulator who ignores adverse selection will fail to predict these knock on effects.

This paper is most closely related to the growing empirical literature on asymmetric information in credit markets. Our primary contribution to this work comes in identifying a form of ex-post variation in the size of a borrower's loan that is unknown to borrowers when selecting contracts. A number of influential papers attempt to distinguish between adverse selection and moral hazard by exploiting ex-ante variation—experimental, regulatory, or institutional—in the set or shape of contracts offered. These include Ausubel (1999) and Agarwal, Chomsisengphet and Liu (2010) on the US credit card market; Adams, Einav and Levin (2009) and Einav, Jenkins and Levin (2012, 2013) on subprime auto loans; Hertzberg, Liberman and Paravisini (2018) on online consumer credit; and Dobbie and Skiba (2013) on payday lending. However, these approaches require strong assumptions as to why the relevant variation in ex-ante contracts does not also generate selection on unobservables. Furthermore, we do so in the largest and arguably most important consumer debt market in the US, in which there has been relatively little work on disentangling these asymmetries. In

Our second contribution comes in connecting work on information asymmetries to broader debates on the role of macroprudential regulations on household leverage. As noted in Cerutti, Claessens and Laeven (2017), macroprudential caps (along the dimensions of loan-to-value or debt-to-income) are in place in over 41 countries as of 2014. A growing literature explores the ways in which this prudential regulation

<sup>&</sup>lt;sup>9</sup>We are also heavily indebted to broader empirical work on asymmetric information in insurance and other markets. Particularly Chiappori and Salanié (2000), Cardon and Hendel (2001), Finkelstein and Poterba (2004), Finkelstein, McGarry et al. (2006), Finkelstein and Poterba (2014), Hendren (2013), as well as recent work examining the welfare implications of information asymmetries such as Einav, Finkelstein and Cullen (2010), Einav et al. (2013), and Einav, Finkelstein and Schrimpf (2010).

<sup>&</sup>lt;sup>10</sup>For example, mortgage balances represented 68 percent of consumer debt in the first quarter of 2016. See the Federal Reserve Bank of New York's May 2016 Quarterly Report on Household Debt and Credit.

<sup>&</sup>lt;sup>11</sup>One early exception is Edelberg (2004), who uses structural assumptions to test for adverse selection and moral hazard in a broad class of consumer debts, including mortgages. Ambrose, Conklin and Yoshida (2015) and Jiang, Nelson and Vytlacil (2014), consider selection into and within low documentation mortgages. There is also related work in the home equity lending market, in particular Agarwal et al. (2011) and Agarwal, Chomsisengphet and Liu (2016).

impacts credit markets, and evaluates their effectiveness. These include: Greenwald (2018), Gete and Reher (2016), DeFusco, Johnson and Mondragon (2017), and Behn, Haselmann and Vig (2017). We provide the first empirically grounded evidence highlighting the complications that adverse selection poses for regulations of this form.

Our estimates of the causal impacts of home equity and monthly payments also both contribute to the literature on mortgage default in their own right. Our key innovation is our use of cross-sectional borrowerlevel variation in interest rates—and hence balances—which is impossible to generate in most contexts. Vandell (1995) provides an overview of early research on the role of home equity in borrower's exercise of the default option. More recent work, including Bajari, Chu and Park (2008), Foote, Gerardi and Willen (2008), Elul et al. (2010), Bhutta, Shan and Dokko (2010), and Gerardi et al. (2015), has stressed the joint importance of triggers such as liquidity and job loss alongside home equity in mortgage default. Palmer (2015) decomposes variation in defaults across cohorts of subprime mortgages into a portion due to home equity and a portion due to relaxed lending standards. However, the majority of this literature identifies the impact of home equity on default using variation that results from changes in local home prices. Our borrower-level variation in home equity avoids the potential for measurement error and other endogeneity concerns inherent to the use of home price variation. A recent exception is Ganong and Noel (2017), which uses experimental evidence from the HAMP program based on a sample of loan modification applicants. Our strategy provides a counterpoint to their work by focusing on less deeply underwater borrowers. Indeed—in contrast to their results—we find strong evidence that borrowers balances causally drive default decisions. Our estimates on monthly payments—and our identification strategy—complement a series of papers investigating the impacts of interest rate resets on delinquency and other outcomes for borrowers with adjustable-rate mortgages. This includes Fuster and Willen (2017), Tracy and Wright (2012), Di Maggio et al. (2017), and Gupta (2017).

The paper is structured as follows: Section 2 lays out key definitions and provides a framework describing information asymmetries in the mortgage market. Section 3 provides background information on ARMs and the data used in the paper. Section 4 presents the empirical strategy. Section 5 presents results on the Option ARM sample, while Section 6 uses the a hybrid ARM sample to isolate the role of payment shocks. Section 7 shows the results of simulations, and Section 8 concludes.

# 2 Definitions and Sources of Information Asymmetries

In this section we define adverse selection and moral hazard as they pertain to the relationship between mortgage borrowers and lenders. We then discuss why we might expect information asymmetries to exist in mortgage markets, highlighting a particular sort of borrower-level heterogeneity—individual differences in willingness to default—that provides a source of adverse selection.

#### 2.1 Definitions of Adverse Selection and Moral Hazard

The definitions of adverse selection and moral hazard that we specify follow largely from those used in Adams, Einav and Levin (2009):

- (I) *Moral Hazard*: The mortgage market exhibits moral hazard if there is a causal relationship between the size of a borrowers' loan liability and default. That is, all else equal, those who face higher balances ex-post default more frequently.
- (II) *Adverse Selection:* The mortgage market exhibits adverse selection if unobservably risky borrowers—those who are more likely to default with contract terms held equal—select higher leverage contracts.

Defining adverse selection in this way is fairly standard and adheres closely to the discussion in Chiappori and Salanié (2013) on insurance markets. Adverse selection exists if there is an exogenous correlation between a borrower's demand for leverage and the unobservable credit risk he poses to the lender.<sup>12</sup>

By moral hazard, we simply mean the causal impact of greater loan balances on borrower default. This definition of moral hazard is somewhat broader than usual. Typically, a credit market can be said to exhibit moral hazard if (i) the expected returns to the lender depend on some non-contractable action of the borrower and (ii) that action is itself influenced by the terms of the loan contract. If default is considered a strategic choice, our definition aligns with this traditional notion; because default itself can be thought of as the non-contractable action taken by the borrower. However, default may not be an active choice in certain circumstances. Borrowers may be insolvent or credit constrained to the extent that they are mechanically unable to make payments. While the discussion below primarily highlights the strategic channel, the definition we use does not, in principal, rule out defaults due to a mechanical relationship between the loan balance and default.

## 2.2 Sources of Information Asymmetries in Mortgage Markets

Moral hazard arises naturally from the limited liability that is implicit in a mortgage contract: lenders cannot effectively contract against borrowers defaulting when their mortgages are underwater. For any given borrower, a larger balance increases the probability of owing much more than the home is worth, which in

<sup>12</sup>While there are a number of possible underlying models that could generate such a relationship, the equilibrium implications of the correlation are largely independent of the source, so we do not specify a mechanism in the baseline definition.

turn increases the probability of default. Of course, legal restrictions vary from state to state, with some explicitly prohibiting lenders from recovering any excess balance from the borrower beyond the home itself in the event of default. 13 However, even in states with laws that are favorable to lenders, deficiency judgments are relatively rare in practice (Pence, 2006)

What is the source of heterogeneity in borrower risk that leads to adverse selection? As a baseline, consider a simple model of mortgage default—often referred to as the frictionless option model—in which borrowers strategically default immediately when the value of their home drops below the value of the mortgage. Unless borrowers have individual (and private) insights into the future path of real estate prices, this model leaves little room for adverse selection. Borrowers default according to a uniform rule.

However, a large literature suggests that borrowers do not default according to a frictionless option model (see Vandell, 1995, for a review). There is significant heterogeneity in willingness to exercise the default option (Deng, Quigley and Van Order, 2000), and a growing consensus that negative equity is a necessary but not sufficient condition for default (Bhutta, Shan and Dokko, 2010; Elul et al., 2010). Borrowers typically do not default until they owe substantially more on their mortgage than the home is worth. Note that there is no necessary need for a behavioral explanation for this phenomenon. There are real costs associated with default, including credit score reductions, moving costs, and social stigma. These costs may vary in the population reflecting, for instance, cross-sectional differences in the value of future access to credit or the private value of accessing local schools. This variation in the default trigger across borrowers is difficult to observe or contract upon, and generates adverse selection to the extent that it is correlated with a borrower's propensity to default.

This notion can be shown—in a stylized manner—with a simple default rule. Consider a borrower i who owes a loan balance B for a house with value H. The borrower must choose between repaying the loan and receiving the value of the home, or defaulting, which entails both losing the home and incurring any costs of default  $C_i$  (e.g. moving costs or credit score reductions). This gives rise to the following rule: borrowers default if

$$H - B$$
 <  $C_i$ 
Value of Repaying Value of Defaulting

The key feature for our purposes is simply that  $C_i$  may be different for different individuals i. Some borrowers may have very low  $C_i$  and default anytime H < B, whereas others may have relatively high  $C_i$ . For a given distribution of housing values ex-ante—and a fixed balance—borrowers with lower  $C_i$  will be more

<sup>&</sup>lt;sup>13</sup>California, for example, has laws that explicitly prevent the lender from recovering any balance from the borrower beyond the home itself in the case of default for owner-occupied homes with 1-4 units. Alternatively, Illinois allows deficiency judgments that can only be relieved in bankruptcy.

14 *H* might alternatively be thought of as the option value of continuing to service the mortgage.

likely to default. At least some portion of these heterogeneous costs  $C_i$  is likely to be unobservable to the lender.

Adverse selection arises when this unobserved heterogeneity in default risk is correlated with a borrower's demand for leverage when selecting a mortgage. In other words, if riskier borrowers—e.g. those with unobservably low values of  $C_i$ —prefer higher leverage mortgages. In classic models of adverse selection, this correlation exists because borrowers have private information about their risk when choosing a loan.<sup>15</sup> For example, if they have some private signal regarding the value of  $C_i$ . A borrower who knows ex-ante that he is relatively unlikely to repay will prefer to put less money down—i.e. to choose a higher leverage loan—and will be willing to accept an increased interest rate to do so.

In Appendix A we outline a simple two period version of such a model, and show that a Spence-Mirrlees single crossing condition holds: risky borrowers are relatively more willing to accept large balances (i.e. higher interest rates) in exchange for more leverage. The equilibrium implications of this sort of selection are familiar from the literature on collateralized lending following Bester (1985) and more general work on screening in the tradition of Rothschild and Stiglitz (1976). In competitive contexts, leverage acts as a screening device. Because safe borrowers value leverage less, they choose sub-optimally low leverage (compared to the first best) in order to differentiate themselves from risky borrowers.

Of course, a correlation between default risk and leverage demand might occur even if borrowers are not so forward looking as to take into account their default probability when selecting a mortgage. For example, a borrower who has limited access to cash for a down payment when selecting a mortgage may also find it disproportionately costly to raise the funds to repay the loan. For the purposes of our empirical exercises, the precise mechanism underlying this correlation is not crucial, although we are required to make assumptions when conducting policy simulations in Section 7.

# 3 Background and Data

In this section, we provide background on Adjustable-Rate Mortgages (ARMs) generally and the Option Adjustable-Rate Mortgage in particular. We focus on the unique features of the Option ARM product that are key to our identification strategy. Because these loans feature fixed payment schedules and variable interest rates, changes in the benchmark financial indices used to determine interest rate adjustments translate directly to changes in borrowers' balances. We then discuss the natural experiment we exploit: the

<sup>&</sup>lt;sup>15</sup>See, e.g. Brueckner (2000) and Bester (1985).

<sup>&</sup>lt;sup>16</sup>In other words, borrowers with low costs of default place a higher value on implicit hedge against home price reductions provided by the option to default. One way to think about this framework is as a model of selection on (ex-post) moral hazard, as in Einav et al. (2013). Lenders cannot contract on the action of default, the willingness to take that action varies in the population, and borrowers are privately informed of their own willingness.

divergence of the two most common financial indices used for Option ARMs. Finally, we discuss the characteristics of borrowers that chose Option ARMs relative to the larger population of mortgage borrowers and describe the data sources used in the empirical analysis.

## 3.1 Background on ARMs

Traditional Hybrid ARM mortgage contracts feature fixed interest rates and fixed payments for a set initial period—usually 5 or 7 years. After the initial period interest rates begin to adjust according to market conditions, usually changing annually or semi-annually. These interest rates are calculated as the sum of a fixed component (*margin*) and a variable component (*index*). Monthly payments are designed to be fully amortizing, that is, calculated to exactly pay off the loan over the full term at current interest rates. As a result, payments change to keep pace with interest rates and may unexpectedly increase if interest rates rise.

According to lenders, the potential danger of these unexpected payment increases motivated the creation of the Option ARM.<sup>17</sup> Banks wanted a product that incorporated floating interest rates while protecting borrowers from sharp payment increases and mortgage holders from the associated default risk. The Option ARM is characterized by a series of features that reflect this desire:

- (I) *Fixed minimum payment schedule:* Borrowers are offered a small initial monthly payment, often based on the fully amortizing payment for an extremely low "teaser" interest rate. For the first 5 years, this payment adjusts upward once yearly by a fixed amount, usually 7.5 percent. After 5 years, the minimum payment adjusts to the fully amortizing amount.<sup>18</sup>
- (II) *Monthly interest rate changes:* While interest rates Hybrid ARMs adjust annually or semi-annually, Option ARMs update much more frequently—usually monthly. New interest rates are calculated as the sum of a fixed margin component and an index term to proxy for the cost of funds to the lender.
- (III) *Negative amortization:* The minimum payment required in a given month will often be lower than the amount of accrued interest. In these circumstances, Option ARMs allow for negative amortization, that is, allow the excess interest accrual to be incorporated into the balance. As a result, the loan balance will typically grow in the early years of the mortgage.
- (IV) *Proposed Payment Options:* The name, Option ARM, refers to a menu of payment options offered on borrower's monthly statements. In addition to the minimum payment, statements offer the possibility

<sup>&</sup>lt;sup>17</sup>See Golden West's history of the Option ARM, available at http://www.goldenwestworld.com/wp-content/uploads/history-of-the-option-arm-and-structural-features-of-the-gw-option-arm3.pdf.

<sup>&</sup>lt;sup>18</sup>In theory, 7.5 percent is a cap, and the minimum payment might adjust by less if a 7.5 percent increase were to exceed the fully amortizing payment. In practice, the cap is nearly always binding. The schedule may also be interrupted if the loan balance rises above a fixed proportion of the original home value, often 110 or 125 percent.

of an interest only payment—covering the entirety of the interest accrual—along with amortizing payments calculated according to 15- and 30-year schedules. These possibilities are suggestions. Only the minimum payment is binding, and the borrower may in principle make any payment between the options or in excess of the 15-year amortizing payment (sometimes subject to certain caps). In practice most borrowers make the minimum payment every month.

For the purposes of the identification strategy, (I) and (II) are key. Because payments are fixed for the first 5 years borrower's balances change as a function of realized interest rates.<sup>19</sup> In the next subsection we discuss these features in greater depth.

In the years leading up to the crisis, Option ARMs became a significant fraction of the market, representing approximately 9 percent of originations in 2006.<sup>20</sup> As the crisis hit, borrowers with Option ARMs defaulted at high rates. In the sample studied here, 41 percent of borrowers were seriously delinquent (60 days past due) on their mortgages at some point within the first 5 years, and 33 percent wound up in foreclosure. The combination of high default rates and non-traditional features made Option ARMs a poster-child for excess in mortgage lending (see Amromin et al., 2011). Their role in the crisis has been highlighted by various media sources and policymakers—Ben Bernanke noted that "the availability of these alternative mortgage products proved to be quite important and, as many have recognized, is likely a key explanation of the housing bubble." Despite these criticisms recent research has argued in favor of these products, both suggesting that they approximate the optimal mortgage contract when borrowers have stochastic income (Piskorski and Tchistyi, 2010)<sup>21</sup> and noting potential benefits from a macroprudential perspective (Campbell, Cocco and Clara, 2017).

#### 3.2 Diverging Indices and Interest Rate Resets

Our identification strategy exploits the divergence of the two most common financial indices used to determine interest rate adjustments for Option ARMs: LIBOR and Treasury rates.<sup>22</sup> Prior to the crisis, borrowers had little reason to prefer one index to another. Although there tended to be a spread between LIBOR and Treasury rates—for example, the spread between 1-year CMT and 1-year LIBOR was generally below 50

<sup>&</sup>lt;sup>19</sup>All analyses performed here consider outcomes within the first 5 years. Appendix Figure A.I presents a sample balance and payment trajectory for an Option ARM to highlight these product features from origination through that period.

<sup>&</sup>lt;sup>20</sup>See the <sup>2008</sup> Mortgage Market Statistical Annual. In the 1980s and 1990s, the Option ARM was primarily a niche product directed towards sophisticated borrowers. The flexibility of payments was intended to appeal to borrowers who expected their income to rise in the future or those with high income volatility. With the growth of a secondary market for non-traditional mortgages in the early 2000s, banks began to market Option ARMs as affordability products, allowing borrowers to purchase more expensive homes than they would be able to afford with a traditional mortgage. Borrowers might take out such loans with the intention of refinancing the mortgage or selling the home after several years, and thus never making payments much above the initial minimum.

<sup>&</sup>lt;sup>21</sup>See also Guren, Krishnamurthy and McQuade (2018), who confirm the findings in Piskorski and Tchistyi (2010), but also suggest that the Option ARM may perform particularly poorly in crises.

<sup>&</sup>lt;sup>22</sup>The Treasury indicies for Option ARMs are nearly always the 1-year Constant Maturity Treasury (CMT) or the 12-month Moving Treasury Average (MTA). Typically LIBOR refers to the 3-month LIBOR. We restrict our sample to exclusively these indicies.

basis points—the two indices moved quite closely together, and any fixed difference could be accounted for in the margin. Furthermore, Bucks and Pence (2008) suggest that borrowers tended to be uninformed about their contract terms. When asked what index their loan depended on, only 25 percent of borrowers responded with plausibly correct indices. 30 percent of borrowers simply answered that they did not know.

If borrowers were unaware of the distinction between indices, why did some end up with a Treasury index and others with LIBOR? Much of the variation comes as a result of the lender. Appendix Table A.I shows the proportion of LIBOR-indexed loans for the top originators in the sample of Option ARMs. Most originators appear to specialize in either LIBOR or Treasury indices, and some offer only Treasury rates. A similar—if slightly less pronounced—pattern can be seen among servicers. According to Gupta (2017), differences across lenders are often a function not of the borrowers they lend to, but rather their intentions on the secondary market.

The interest rate divergence between the two indices is illustrated in Panel A of Figure I, which shows the spread between the 1-year Constant Maturity Treasury (CMT) and 1-year LIBOR. While there were fluctuations in the years preceding the crisis, the difference was contained in a relatively narrow band. However, in mid-2007, Treasury rates began to fall and the spread increased, eventually peaking at over 3 percentage points in late 2008 following the Lehman Brothers bankruptcy filing and the AIG bailout.

Panel B of Figure I displays the impact of this phenomenon for a large sample of adjustable-rate mort-gages, including the Hybrid ARMs we study in Section 6. The black line shows the average difference in interest rates between resetting loans indexed to LIBOR versus Treasury for each month. There is a notice-able spike in the in-sample difference in early 2009, corresponding to the late 2008 spike in Panel A. The red line in Panel B shows the in sample difference in default for resetting loans indexed to LIBOR versus Treasury. In sync with the spike in relative interest rates, there was a sharp spike in relative defaults in early 2009. In the month that LIBOR-indexed loans experienced the most severe difference in interest rates, they also exhibited the most severe difference in defaults. While this figure does not capture our primary strategy precisely, it illustrates the basic concept: the divergence of LIBOR and Treasury indices generated meaningful differences in the interest rates borrowers faced, with subsequent consequences for default patterns.

But how do differences in interest rates cleanly translate into differences in loan balances? This is where the unique features of the Option ARM come into play. For a hybrid adjustable-rate product, a change in the interest rate also changes the monthly payment, which adjusts to ensure that the payments are fully amortizing at the new rate. However, because the minimum payments are set in the initial period for Option ARMs, changes in interest rates have *no direct contemporaneous impact* on monthly obligations. As the mortgage must account for changes in the interest rate somehow, any additional interest accrual is incorporated directly into the balance. This means that—for Option ARMs—the divergence between Treasury and LIBOR

rates caused borrowers with otherwise identical loans to have sizable differences in loan balances ex-post. Appendix Figure A.II provides a stylized example of this pattern. Consider two identical \$100,000 loans at origination, one of which faces a high realization of interest rates, while the other faces a low realization. Two years into the loan, the two borrowers will still have the same monthly payment, but the first borrower may owe thousands of dollars more than the second.

The impact of a LIBOR or Treasury index on the loan balance is not uniform across the sample period. Each origination month for each index generates a unique path of interest rates and a unique balance trajectory. Figure II demonstrates this difference-in-difference variation in borrower's balances. The plot shows the loan balance over time for four sample \$100,000 loans: one LIBOR- and one Treasury-indexed loan originated in January 2005, and one of each originated in January 2007. Each of the four shows a distinct balance trajectory. We use precisely this difference-in-difference variation: the interaction between a borrower's index and origination month in our empirical strategy.

#### 3.3 Data

The data on ARMs and Option ARMs used in this paper are taken from a loan-level panel of privately securitized mortgages provided by Moody's Analytics (formerly provided by Blackbox Logic) representing over 90 percent of non-agency residential mortgage-backed securities. These data provide detailed information about loans at origination, including borrower information, property characteristics, and contract terms. They also include dynamic information on monthly payments, loan balances, modifications, delinquency, and foreclosure. In our primary analysis we limit our sample to the approximately 500,000 Option ARMs originated between 2004 and 2007 that are tied to either LIBOR or Treasury and have initial loan-to-value ratios between 50 and 100. In Section 6, we consider an alternative sample of approximately 450,000 5/1 Hybrid ARMs.

#### 3.4 Summary Statistics: Balance Across Indices

Panel A of Table I shows summary statistics for the primary Option ARM sample studied here, divided between loans indexed to Treasury and those indexed to LIBOR. Note that Treasury is the dominant index for Option ARMs, representing approximately 90 percent of loans. Despite this, the majority of variables are reasonably balanced across the two groups. Borrowers have fairly high FICO credit scores for both indices, with an average of 706 for Treasury loans and 714 for LIBOR loans. While the unique characteristics of the

 $<sup>^{23}</sup>$ These figures are based on simulated loans with a margin of 3.5 for both samples, based on the 3-month LIBOR and 12-month MTA respectively.

Option ARM may have attracted a certain sample of the population, the growth in credit supply went to high credit quality borrowers.<sup>24</sup>

One peculiarity distinguishing Option ARMs from conforming loans is the rarity of income verification. Given borrowers with high credit scores, low required monthly payments, protections against payment increases, and generally favorable expectations about housing prices, lenders were relatively unconcerned about borrowers' ability to meet monthly obligations. This led to a prevalence of low or no documentation loans: 79 percent for Treasury and 77 percent for LIBOR. For these loans, borrowers provided little or no formal evidence of sufficient income to meet monthly payments, often simply stating income with no verification. <sup>25</sup>

The original leverage choice—summarized by the origination loan-to-value ratio (LTV)—is also quite similar across the two indices at 76.6 for Treasury and 77 for LIBOR. This is slightly larger than conforming loans purchased by Fannie Mae or Freddie Mac but below the average LTV for subprime adjustable-rate mortgages. Nearly all loans are subject to some form of prepayment penalties and the majority of both Treasury and LIBOR loans are for primary residences. There is a difference in the average margin for each—3.21 for Treasury loans versus 2.85 for LIBOR—but this gap reflects the baseline spread between the indices themselves.

The four most common states for both indices are California, Florida, Arizona, and Nevada, reflecting the broader mortgage market. While Treasury loans are slightly more concentrated in California, the overall geographic patterns are similar across states. Appendix Figure A.III shows this relatively consistent geographic density: between 5 and 15 percent of loans are indexed to LIBOR in nearly all states. The largest difference between the two samples is in the timing of origination. LIBOR loans are significantly more concentrated in 2004, while Treasury loans are more heavily represented in 2005 and 2006. This pattern is also reflected in the slightly higher average balances for Treasury loans. To account for any potential index-related variation all of our analysis includes a control for whether loans are linked to LIBOR or Treasury.

<sup>&</sup>lt;sup>24</sup>The average credit score in the US is below 690, while the average among conforming loans purchased by Freddie Mac is 723 (Frame, Lehnert and Prescott, 2008). Amromin et al. (2011) find that borrowers with complex mortgages tend to be sophisticated, with high incomes and credit scores relative to the subprime population.

<sup>&</sup>lt;sup>25</sup>In the market as a whole in 2007, low or no documentation loans represented only 9 percent of outstanding loans. However, nearly 80 percent of Alt-A securitizations in 2006 were low or no documentation, mirroring the pattern in this sample (Financial Crisis Inquiry Commission, 2011).

<sup>&</sup>lt;sup>26</sup>The average original LTVs for Fannie Mae and Freddie Mac in 2007 were 72 and 71, respectively according to Frame, Lehnert and Prescott (2008).

<sup>&</sup>lt;sup>27</sup>The stated level of owner occupancy is likely an overstatement due to false reporting by unreported investors (Piskorski, Seru and Witkin, 2015).

# 4 Empirical Strategy

In this section we describe a simple empirical model of borrower's leverage and default choices. We then clarify the distinct empirical predictions of both moral hazard and adverse selection in this context. Finally, we show how the model translates to a series of estimating equations and describe the strategy we use to separately identify adverse selection and moral hazard.

## 4.1 An Empirical Model of Leverage Demand and Default

To specify a model of borrower default, we begin with the rule discussed in Section 2. At a given point in time t, a borrower i defaults if their equity in the home—the difference between the home price ( $H_{it}$ ) and the loan balance ( $B_{it}$ )—drops below some borrower specific cost of default:  $H_{it} - B_{it} < -C_{it}$ .

For our purposes, it is convenient to define the borrowers *Negative Equity* as the difference between the balance owed and the value of the home ( $E_{ijt} = B_{it} - H_{it}$ ). Rearranging and decomposing the individual specific costs into observable and unobservable components, we may rewrite the default rule as:<sup>28</sup>

$$D_{i,t+1} = \mathbb{1}\{\alpha E_{it} + x_i'\beta + \varepsilon_{it} > 0\}$$
(1)

where  $D_{i,t+1} = 1$  if borrower i defaults between period t and t + 1.

While the borrower's contract choice is the result of a complex maximization problem, we abstract from this structure and specify a linear demand model for leverage. Letting  $L_i$  represent the original LTV chosen by borrower i and  $x_i$  be the full set of observables that lenders are able to price on:

$$L_i = \chi_i' \psi + v_i. \tag{2}$$

Within this framework, moral hazard and adverse selection have straightforward empirical predictions:

- (I) Moral Hazard:  $\alpha > 0$  provides evidence of a moral hazard effect.  $\alpha$  quantifies the causal impact of the borrower's equity on default.  $\alpha$  can also be interpreted as the (square-root of the) precision of unobserved default costs in the population.
- (II) Adverse Selection:  $\rho = Corr(v_i, \varepsilon_{it}) > 0$  provides evidence of adverse selection. Borrowers who choose higher than average  $L_{ij}$  based on unobservables (large  $v_i$ ) are more likely to default holding home equity constant (large  $\varepsilon_{it}$ ).

<sup>&</sup>lt;sup>28</sup>We decompose  $-C_{it} = x_i' \frac{\beta}{\alpha} + \frac{1}{\alpha} \varepsilon_{it}$ , where  $x_i$  is a set of observable characteristics available to the lender at origination, and  $\frac{1}{\alpha} \varepsilon_{it}$  is the unobservable portion of the borrower's default costs.  $\alpha$  is then the reciprocal of the standard deviation of the default costs in the population.

## 4.2 Estimating Equations

In practice, our primary specifications collapse equations 1 and 2 into a single reduced form specification.<sup>29</sup> For borrower i in MSA j at loan age t, we estimate:

$$D_{it+1} = \mathbb{1}\{\alpha E_{it} + \gamma L_i + x_i'\beta + \omega_{m(i)} + \delta_{index_i} + \zeta_{j(i)} + u_{it} > 0\}.$$
(3)

Here,  $D_{jt+1}$  is a measure of default between year t and t+1.  $E_{ijt}$  is a measure of the borrower's negative equity, measured either as the current difference between a borrower's balance and the value of the home or as the current LTV.  $L_i$  is the borrower's initial leverage choice, measured as the original LTV. The vector  $x_i$  contains the set of all borrower characteristics and loan features known to the bank at the time of contracting. We include fixed effects for the origination month of the loan  $(\omega_{m(i)})$ , the index choice  $(\delta_{index_i})$ , and the borrower's MSA  $(\zeta_j(i))$ . Standard errors are clustered at the MSA level. Most specifications additionally allow for state specific time trends. Importantly, we separately estimate the above cross-sectionally at different loan ages, so do not include loan age effects (or time effects separate from origination month) in our specifications. In this reduced form specification, we interpret  $\gamma > 0$  as evidence of adverse selection and  $\alpha > 0$  as evidence of moral hazard. For robustness, and to provide parameters that are more directly relevant for our simulations in Section 7, we also explicitly estimate a joint model of Equations 1 and 2 (alongside Equation 4, described below).  $^{30}$ 

$$\varepsilon_{it} = \gamma (L_i - x_i' \psi - \theta_{m_i} - \eta_{index_i}).$$

Replacing  $\varepsilon_{it}$  in Equation 1 and collapsing month and index fixed effects gives Equation 3.

 $^{ar{30}}$ To estimate Equations 1, 2 and 4 jointly, we impose a parametric structure on the errors. In particular:

$$\left(egin{array}{c} arepsilon_{it} \ v_i \ e_{it} \end{array}
ight) \sim N \left(egin{array}{ccc} 0 & 1 & & & \ 0 & , \left[egin{array}{ccc} 1 & & & \ 
ho_{arepsilon v} \sigma_v & \sigma_v^2 & & \ 
ho_{arepsilon e} \sigma_e & 
ho_{ve} \sigma_v \sigma_e & \sigma_e^2 \end{array}
ight]
ight).$$

Again, we estimate cross-sectionally at different t and hence make no assumption about the evolution of errors over time. This specification allows a relatively straightforward estimation. We effectively employ a control function approach following Blundell and Powell (2004), incorporating an additional linear equation. The benefit of this approach is that we are able to recover a few parameters that provide a basis for simulation in Section 2. Perhaps most importantly, we directly recover  $\rho_{\varepsilon v}$ , the correlation between  $\varepsilon_{ijt}$  and  $v_i$ . This correlation determines the strength of the adverse selection effect. Furthermore, under the normality assumption, we are able to recover the underlying distribution of the default costs  $C_{it}$ . Recalling that  $-C_{it} = \sigma_{\varepsilon}(x_i'\beta + \omega_{m(i)} + \zeta_{j(i)} + \delta_{index_i} + \varepsilon_{it})$ , we have:

$$C_{it}|x_i,\omega_{m(i)},\zeta_{j(i)},\delta_{index_i}\sim N\bigg(\frac{-(x_i'\beta+\omega_{m(i)}+\zeta_{j(i)}+\delta_{index_i})}{\alpha},\frac{1}{\alpha^2}\bigg).$$

The variance of the distribution of  $C_{it}$  characterizes the moral hazard effect while  $\rho_{\bar{v}v}$  summarizes the degree to which borrower's knowledge of their place in this distribution impacts leverage demand.

<sup>&</sup>lt;sup>29</sup>In particular, we write  $\varepsilon_{it} = \gamma v_i + u_{it}$ , where  $\gamma > 0$  holds if  $v_i$  and  $\varepsilon_{it}$  are positively correlated, that is, if there is adverse selection (In the normal case,  $\gamma = \rho \frac{\sigma_{\varepsilon}}{\sigma_{v}}$ ). Replacing  $v_i$  using Equation 2 gives

#### 4.3 Identification

The basic challenge in separately identifying  $\alpha$  and  $\gamma$ —the effects of current equity and initial leverage on default—is the mechanical relationship between  $L_i$  and  $E_{it}$ . In the absence of other differences, borrowers with identical  $L_i$  will tend to have identical  $E_{it}$ . For borrowers consistently making minimum payments, there are only two factors that might cause those with identical  $L_i$  to have different  $E_{it}$ : differences in home prices or differences in interest rates that lead to different balances.

Unfortunately, shocks to home prices may, in general, be correlated with  $u_{it}$ . For example, a local labor market shock may influence both home prices and, separately, the borrower's probability of default. Additionally, because home prices can never be observed directly but rather must be inferred from the sale prices of surrounding homes,  $E_{it}$  is measured with error. Similarly, variation across time in interest rates is likely correlated with macro conditions, while cross-sectional variation potentially reflects borrower's endogenous contract choices. Isolating exogenous variation in  $E_{it}$  is non-trivial but necessary to accurately estimate  $\alpha$  and  $\gamma$ .

To address the challenges of estimating moral hazard and adverse selection, we introduce an instrumental variable approach that uses the divergence of LIBOR and Treasury rates. In our analysis,  $E_{ijt}$  is instrumented by a function of the borrower's index choice and origination month:

$$E_{it} = f_t(m_i, index_i) + \lambda_{m(i)} + \mu_{index_i} + x_i' \pi_t + \phi_{j(i)} + e_{it}.$$

$$\tag{4}$$

As described in Section 3, we focus on plausibly exogenous variation in  $E_{ijt}$  that comes from the interaction of the borrower's index and the origination month of the loan. Using this difference-in-difference variation allows us to control for any origination month-specific cohort effects or trends in the macro-economy, while also accounting for any fixed differences between borrowers with different indices.<sup>31</sup>

Implementing this strategy involves choosing a functional form for  $f_t(m_i, index_i)$ . In what follows, we focus primarily on a specification that exploits all possible variation in the interaction between the month of origin and the index, that is:

$$f_t(m_i, index_i) = \lambda_{m_i} \times \mu_{index_i}$$

In words, we use a full set of fixed effects for every possible {Index Type, Origination Month} pair as instruments for the borrower's home equity. This specification has the advantage of limiting assumptions about functional forms and provides a large number of instruments. However, because this large set of instruments does not provide an easily interpretable first stage and may suffer from problems associated

<sup>&</sup>lt;sup>31</sup>Our difference-in-difference framework also allows us to control for fixed lender characteristics, even for originators or servicers who exclusively feature one of the two indices.

with many weak instruments we also use a second, complementary, option. We mechanically calculate the full balance trajectory for a sample loan for each index type and origination month. The sample loan sets all potentially endogenous terms, which vary for any given loan, to standard values.<sup>32</sup> As a result, the instrument captures the variation in the balance that is driven by the interest rate realizations while excluding any variation due to endogenous contract choices. We refer to the instrument developed using this calculation as the "simulated" instrument.

#### 5 Results

In this section, we describe the central empirical results of the paper. We begin by defining a few variables used in the analysis. Next, we describe first stage results: the instruments we use are correlated with borrower's balances and payments, are directly predictive of default in a reduced form, and do not predict borrower characteristics such as credit scores. We then turn to the results of the primary, single equation model of default. We find strong evidence of both moral hazard and adverse selection, which hold across numerous robustness checks. Finally, we discuss the estimation of the joint model of leverage demand and default choice which provides parameters that directly inform the simulations presented in Section 7.

## 5.1 Definitions of Key Variables

The empirical analysis revolves around three variables: default  $D_{it+1}$ , original leverage  $L_i$ , and current equity  $E_{it}$ . Here, we discuss the definitions of each as used below:

- (I) **Default** ( $D_{it+1}$ ): Default is defined as a borrower being 60 or more days past due on monthly payments. Typically,  $D_{it+1}$  measures the outcome of default between years t and t+1. However, when explicitly stated,  $D_{it+1}$  may also refer to default at any point between loan origination and t+1.
- (II) **Original Leverage** ( $L_i$ ): Original leverage is measured as original loan-to-value in percentage terms.<sup>33</sup>
- (III) **Current Equity** ( $E_{it}$ ): we use two alternative measures of  $E_{it}$  throughout the analysis. The first is the borrower's *negative equity*. This is defined as the current balance on the loan less the value of the home. The second is the borrower's current *loan-to-value*, the ratio of the current balance to the current value of the home. Both of these measures grow as the borrower's balance increases and fall if the price of

 $<sup>^{32}</sup>$ A margin of 3.5, an initial loan size of \$400,000, and a minimum payment based on a 1.75 percent teaser rate.

<sup>&</sup>lt;sup>33</sup>While the CLTV (combined loan-to-value), which incorporates any second liens, is sometimes used as a measure of leverage, my focus here is on the leverage contained in a particular contract. We control for the presence of any observable additional liens in all specifications.

the home increases. As home values are generally only recorded when houses are sold, we follow the literature and impute the current home value based on local home price indices.<sup>34</sup>

Unfortunately, we do not observe  $E_{it}$  for borrowers who exit the sample prior to time t. This prevents us from using the full sample for specifications that incorporate current home equity. However, given the contract terms for a mortgage—the margin, initial monthly payment, initial balance, and index—predicting the balance up to the first delinquency or partial prepayment is a straightforward mechanical calculation. Using just loan terms at origination and interest rates, we are able to predict the observed values of  $E_{it}$  with a high degree of accuracy ( $R^2 > 0.95$ ). In regressions that incorporate the full sample, we use these imputed values of  $E_{it}$ , which are available for all borrowers, rather than the observed values.

### 5.2 First Stage

The plots in Figure III highlight a few features of the instruments for  $E_{it}$  used in the main analysis. Because the primary specification uses a large number of fixed effects, and hence does not provide an easy to interpret first stage, we use the simulated instrument described above—a single variable—to produce these figures. This variable allows us to address three points.

First, do borrowers actually have significantly higher  $E_{it}$  when the instrument suggests balances should be high? Panel A of Figure III shows that this is the case. The plot presents the coefficient on the simulated instrument from the simplest possible specification for considering relevance: a regression of  $E_{it}$  on the instrument, controlling for origination month and index fixed effects. When the simulated instrument is high, borrowers'  $E_{it}$  are high. This pattern holds across the first several years of the loan, although the size of the correlation declines over time.

Second, Panel B shows that borrowers also default more when the instrument is high. This is a reduced form and shows coefficients from an identical exercise to that in Panel A, replacing  $E_{it}$  with default  $E_{it}$ . Third, Panel C shows evidence of instrument exogeneity. Despite predicting borrowers' balances and defaults, the instrument is not correlated with FICO credit scores, a key measure of borrowers' creditworthiness.

Table II shows a more formal first stage. The coefficients shown are analogous to those in Panel A of Figure III, utilizing the simulated instrument. However, because the primary specifications use the full set of  $\lambda_M \times \mu_{index}$  fixed effects, we also include *F*-statistics calculated using the full set of fixed effects. At 24 months, predictive power is strong, with *F*-statistics suggesting that the instruments are relevant in both the

<sup>34</sup>We use Zillow's zip code level home price index, available at http://www.zillow.com/research/data/.

fixed effects and simulated instrument specifications (although the *F*-statistic drops below 10 when using fixed effects to predict negative equity).<sup>35</sup>

## 5.3 Main Results: Single Equation Model

Our central results involve unpacking a simple relationship: the positive correlation between original leverage  $L_i$  and default. Figure IV shows an unconditional baseline version of this relationship. There is a strong positive relationship between borrowers' initial choice of LTV and the probability of default within the first five years of the loan.

We now turn to our primary specifications, which attempt to isolate the roles of adverse selection in this relationship following Equation 3. In the main tables, we use linear probability models and a standard instrumental variables approach. In the Appendix we show probit versions, accounting for the endogeneity of  $E_{ijt}$  following Blundell and Powell (2004).

The main tables are structured to show three versions of each specification of interest: baseline, OLS, and IV. The baseline specification shows an analogue of Figure IV: the relationship between original leverage ( $L_i$ ) and default. This specification includes relevant controls but excludes any measure of current equity. Our OLS specifications additionally include a measure of  $E_{ijt}$ , but do not attempt to account for endogeneity. Finally, in the IV regressions we explicitly instrument for  $E_{ijt}$  with the full set of  $\lambda_m \times \mu_{index}$  fixed effects. The coefficient on  $L_i$  gives the adverse selection effect, while the coefficient on  $E_{ijt}$  gives the moral hazard effect. Comparing the IV regressions to the baseline regressions gives a sense of the role of each in the baseline correlation between leverage and default.

Table III presents the primary set of specifications for Option ARMs, showing a cross-section of borrowers 24 months after origination.<sup>36</sup> This table includes  $E_{ijt}$  defined as both current negative equity (Panel A) and current LTV (Panel B). In different specifications we include two levels of controls: a basic set with only origination month and index fixed effects, and a comprehensive set, including MSA fixed effects, flexible controls for the original FICO credit score (dummies for each 20-point bin), state-level time trends, loan originator and servicer fixed effects, and controls for documentation, loan purpose, occupancy, property type, prepayment penalties, private mortgage insurance, second liens, and the original home value.

The left-hand side of Panel A shows that there is strong evidence of both adverse selection and moral hazard when defining  $E_{ijt}$  as current negative equity and including only basic controls. The estimated moral hazard effect in the IV specification suggests that a \$100,000 increase in negative equity increases probability

 $<sup>^{35}</sup>$ Because the current loan-to-value or negative equity at 24 months is only observed for loans that actually survive to those points, the first stage regressions in the first four columns of Panel A are necessarily conducted on a selected sample. Columns (5)-(8) of panel A replaces the observed values of  $E_{it}$  with imputed values, which allows the use of the full sample. While the F-statistics only exceed 10 without covariates, both versions of the instrument are relevant (if weak) with the full sample.

<sup>&</sup>lt;sup>36</sup>Cross-sections at other loan ages are shown in the Appendix.

by 4.5 percentage points (17 percent). The estimated adverse selection effect suggests that a 10-point increase in the borrower's original LTV is associated with a 3.3 percentage point (12.5 percent) increase in the one year default probability. The OLS results are quite similar, showing slightly larger moral hazard effects and a slightly larger role for adverse selection. Comparing the role of original LTV in the IV regression (0.331) to that in the baseline estimate (0.586) implies that adverse selection is responsible for more than half of the baseline correlation. However, it is crucial not to over-interpret the coefficient on original LTV with this limited set of controls. Without controlling for information available at loan origination, this result pools true selection on unobservables with lenders' steering of riskier borrowers towards smaller loans.

The right-hand side of Panel A includes the full set of controls and shows (i) a larger moral hazard effect and (ii) an adverse selection effect that is similar in levels but smaller as a fraction of the baseline estimate. The estimated moral hazard effect implies that a \$100,000 increase in negative equity increases the one year default probability by 8.9 percentage points (33.5 percent). The estimated adverse selection effect shows that, all else equal, borrowers who choose 10-point larger initial LTVs are 2.6 percentage points (10 percent) more likely to default between 24 and 36 months. However, including the full set of controls also leads to a significant increase in the baseline correlation between original LTV and default. As a result, adverse selection accounts for approximately 36 percent of the baseline correlation with appropriate controls. This leaves moral hazard responsible for the remaining 64 percent.

Panel B repeats the exercise from Panel A but defines  $E_{ijt}$  as current loan-to-value. With full controls the effects are quite similar to those found in Panel A. Adverse selection is responsible for 32 percent of the baseline correlation between original LTV and default. The remaining 68 percent is due to moral hazard. These estimates imply that borrowers that choose 10-point higher original LTVs are 2.3 percentage points more likely to default between 24 and 36 months, all else equal, while a 10-point increase in current LTV at 24 months increases the probability of default by just over 4 percentage points. Furthermore, specifications without controls highlight the potential complications of ignoring the information available to the bank. The OLS and IV show negative (although insignificant) coefficients on original LTV when controlling for current LTV.

# 5.4 Robustness for the Single Equation Model

Appendix B discusses a number of tables intended to serve as robustness checks to Table III and to provide alternative estimates of interest. Appendix Table A.II considers how the results in Table III change across three relevant subgroups. The basic results are as follows: we find stronger moral hazard effects in states with limited recourse vs. those with full recourse, stronger selection effects in no/low documentation loans

versus full documentation loans, and minor differences in purchase vs. refinance mortgages.

To show that the effects we find are not specific to default at 24 months, Appendix Table A.III presents identical regressions to those in Table III, except with current  $E_{ijt}$  defined at 48 months and the dependent variable defined to be default between 48 and 60 months. The results are similar to those at 24 months, though somewhat muted. Results are also similar when choosing other periods. To deal with the potential for differential survival to 24 months, Appendix Table A.IV considers the impact of the original LTV and current  $E_{ijt}$  on cumulative default outcomes, that is, on default at any point up to 36 months. These estimates show strong evidence of both moral hazard and adverse selection. Details of the approach and estimation are outlined in Appendix B.

Appendix Tables A.V A.VI and A.VII explore further robustness. The results are robust to (i) alternative functional forms of  $E_{ijt}$ , (ii) probit and control function specifications, which are potentially more realistic than the linear probability model, (iii) the use of the simulated instrument rather than the full set of fixed effects, and (iv) alternative definitions of default, ranging from mild (30 days past due) to extreme (foreclosure).

#### 5.5 Joint Model

The final step of our empirical analysis is to estimate a joint model of leverage demand alongside the default choice. Doing so allows us to recover parameters that more directly relate to the model developed in the Appendix and that can be used to inform the simulations developed in the next section. Because of the increased computational complexity of this estimation, we slightly reduce the richness of included controls, e.g. substituting MSA fixed effects with state fixed effects. We estimate the model separately at 24, 36, and 48 months, and again define  $E_{ijt}$  as both current LTV and home equity. These estimates are presented in Table IV and qualitatively align with estimates from the single equation model.

The primary benefit is in providing estimates of three parameters: (i)  $\rho_{\varepsilon v}$ , the correlation between the errors in the leverage and default choices, where a positive value indicates adverse selection, (ii)  $\sigma_{\varepsilon} = \frac{1}{\alpha}$ , the standard deviation of the default error in units of  $E_{ijt}$ , where a positive and significant value of  $\alpha$  indicates moral hazard (corresponding to a finite positive value of  $\sigma_{\varepsilon}$ ), and (iii) the mean of borrower's default costs, conditional on observables. This can also be interpreted as the default threshold, that is, the level of  $E_{ijt}$  above which the average borrower (with a given set of observables) defaults. While the estimates at 24 and 36 months show strong evidence of both adverse selection and moral hazard—a positive  $\rho$  and  $\alpha$ —the estimates at 48 months are less precise.

The first and fourth columns display the estimated parameters at 24 months, with  $E_{ijt}$  defined in terms

of negative equity and current LTV, respectively. The estimated threshold for default in the first column (at average values of observables) is just under \$100,000, meaning that a borrower will not default until the balance on their loan is \$100,000 above what the home is worth. The standard deviation of the default error in this specification is approximately \$190,000. Similarly, the fourth column suggests that the average borrower must owe 1.34 times what the home is worth before defaulting. The standard deviation of unobserved default costs in the population is just over 50 percent of what the home is worth:  $\sigma_{\varepsilon} = 0.55$ . Finally, the correlation between unobserved default costs and the unobserved portion of the original leverage (original LTV) choice—which measures adverse selection—is significant, and just under 0.07. We use these estimates to parameterize the model in Section 7.

# 6 Hybrid ARMs and the Role of Payment Shocks

The preceding results decompose adverse selection and moral hazard using a sample of Option ARMs. The particular features of the Option ARM product have two advantages: they provide a source of variation in borrowers ex-post balances and enable us to largely ignore the role of monthly payments in our analysis.

Using a single product also has at least two potential drawbacks. The first is a standard external validity concern: would our estimates vary in a more representative sample of mortgages? The second is more specific to our context: outside of the special case of the Option ARM, borrowers with high leverage mortgages may default for a third reason beyond adverse selection or the causal impact of home equity. In particular, there is potential for a payment channel: typically borrowers with greater leverage must also make proportionally larger monthly payments to service their debts.<sup>37</sup> It is possible, in principle, that this payment channel is so large as to be the first order concern when regulating leverage, rendering the relevance of adverse selection moot.

To account for both of these concerns, we repeat the basics of our empirical strategy on a sample of more traditional hybrid adjustable-rate mortgages: which we refer to as 5/1 ARMs. While these mortgages do not have features that allow us to replicate our IV strategy, we are still able to conduct OLS versions of our analysis to establish comparability. Perhaps more importantly, these mortgages *do* have particular features that allow us to credibly identify the effect of monthly payments on default. This allows us to appropriately account for the payment channel and to consider its relative importance in comparison to adverse selection and moral hazard.

 $<sup>^{37}</sup>$ The causal role of mortgage payments in default has also been analyzed by a growing literature, including Ganong and Noel (2017) and Di Maggio et al. (2017).

#### 6.1 Adverse Selection and Moral Hazard for 5/1 ARMs

5/1 ARMs have a series of different characteristics compared to Option ARMs. They feature fixed interest rates for the first 5 years of the loan. Through these years, monthly payments are set to be fully amortizing over a 30 year period given the fixed interest rate. After five years, borrowers face monthly payments based on a new interest rate—called the *reset rate*—linked to a financial index, again usually a Treasury rate or LIBOR. The interest rate subsequently adjusts yearly for the remainder of the loan. Each time the interest rate adjusts payments also change to be fully amortizing over the remainder of the loan term given the new interest rate. This means that monthly payments may jump sharply when the reset rate is substantially different from the previous rate, subject to caps and floors regulating the size of these payment shocks. We return to these jumps when we discuss payment changes below. Panel B of Table I shows summary statistics from the 5/1 sample we use. Again, the two samples are broadly similar on observables, although average balances are a bit higher in the Treasury sample. Notably, a much larger fraction of 5/1 ARMs are linked to LIBOR relative to Option ARMs.

We begin, in Panel A of Table V, by replicating OLS versions of a subset of the results shown in Table III on the 5/1 sample. In particular, we estimate Equation 3 using current LTV as a measure of current equity, again between 24 and 36 months. We first consider, as a baseline, the relationship between leverage and default in this sample. Column 1 shows that, conditional on observables, a 10 point increase in original LTV is associated with a just under 8 percentage point increase in default, just slightly above our estimates in the Option ARM sample. In the second column, we include current LTV as well. Note that, in the absence of an instrument, current LTV is primarily identified as the result of changes in home prices: borrowers with identical contracts in different areas will have different current LTVs because their homes gained or lost value. Our estimates suggest that a 10 point increase in current LTV is associated with a 2.6 percentage point increase in default. Further, when we include current LTV, the coefficient on original LTV falls to 0.480.<sup>38</sup>

The difference between the first and second columns suggests that approximately 60% of the correlation between leverage and default in this sample is attributable to original leverage. This is significantly higher than the role of adverse selection—36%—in our Option ARM sample. However, as noted above, the correlation between original leverage and default in the 5/1 ARM sample may in part be driven by larger monthly payments. In sample, a ten point higher original LTV is associated with an approximately \$500 increase in the monthly payment. As such, it is necessary to account for the role of monthly payments in order to appropriately capture adverse selection. As a first attempt, column 3 additionally includes monthly payments

 $<sup>^{38}\</sup>mbox{These}$  are analogous to columns 4 and 5 of Panel B in Table III.

as a control variable. This inclusion leaves the coefficients on Original and Current Loan-to-Value effectively unchanged. Furthermore, the coefficient on payments is extremely small and negative. While this might suggest a minimal role for payments, it is difficult to interpret this result directly because monthly payments are so highly correlated with initial leverage, and because any variation in payments conditional on initial leverage is unlikely to be exogenous. In the next subsection we describe a strategy that allows us to explicitly identify the role of monthly payments and to appropriately decompose the overall correlation between leverage and default.

#### 6.2 The Causal Impact of Monthly Payments on Default

To identify the effect of monthly payment on defaults for 5/1 ARMs, we consider the sharp changes in borrower's payments that come when the interest rate resets for the first time 5 years after the loan is originated. Once again, we exploit the fact that some borrower's interest rates were indexed to LIBOR while others were indexed to a treasury rate. Crucially, for 5/1 mortgages, these indexes do not affect borrowers balances in the first five years. Instead, the index comes into play only when the rate resets. Borrowers reset rates—and hence monthly payments—are determined as a fixed margin above the value of their index at the time of reset. Just as in our primary empirical strategy, this creates a form of difference-in-difference variation: borrowers payments at the time of reset vary sharply based upon (i) whether they are indexed to treasury or LIBOR, and (ii) the particular month in which they originated the loan.

To capture this variation in monthly payments, we again conduct a difference-in-difference strategy by slightly modifying Equation 3 to include a term for the monthly payment. For a borrower i at loan age t:

$$D_{it+1} = \mathbb{1}\{\tau p_{it} + \alpha E_{it} + \gamma L_i + x_i'\beta + \omega_{m(i)} + \delta_{index_i} + \zeta_{j(i)} + u_{it} > 0\}.$$
 (5)

Where  $D_{it+1}$  here continues to refer to delinquency between age t (in this case 5 years) and t+1 (6 years).<sup>39</sup> The new term  $p_{it}$  is the borrowers monthly payment. Our primary coefficient of interest is  $\tau$ , the causal impact of the payment on default. We again instrument—this time for the monthly payment rather than negative equity—with the full set of index  $\times$  origination month interactions:<sup>40</sup>

$$p_{it} = m_i \times index_i + \lambda_{m(i)} + \mu_{index_i} + x_i' \pi_t + \phi_{i(i)} + e_{it}.$$
 (6)

We present results in Panel B of Table III. The first and third columns show results from OLS versions of

 $<sup>^{39}</sup>$ We choose t+5 years as the date of the first sharp change in interest rates.

<sup>&</sup>lt;sup>40</sup>Appendix Figure A.IV shows a few basic tests suggesting instrument exogeneity. Instrumented payments do not predict borrower's loan terms (margin and original leverage) or credit scores.

Equation 5, with and without our full set of controls and fixed effects. Notice that—as in Panel A—the coefficients on monthly payments are negative and economically negligible. However, in the second and fourth columns we show results from our full IV specification. These estimates suggest an economically meaningful and statistically significant causal effect of monthly payments on default. For example, the results in column 4 suggest that a \$1000 increase in borrowers' monthly payments would increase the probability of default by over 5 percentage points. These results complement the findings of Fuster and Willen (2017) who also find strong impacts of monthly payments on default.

# 6.3 Decomposing the Correlation Between Leverage and Default for 5/1 ARMs

As a final exercise we use our estimates in Panel B to de-bias our results in Panel A and decompose the correlation between leverage and default into three possible components: moral hazard, adverse selection, and the causal effect of payments.

We proceed in three steps. We first note that in the 5/1 sample a 10 point increase in borrower's original LTV is associated with a \$502 increase in the monthly payment. Next, we combine this with our estimates in Panel B and estimate that this \$502 payment increase in turn increases the probability of default by 2.85 percentage points. Finally, we use these estimates to debias the results in column 2 of Panel A. Those estimates suggest that, overall, a 10 point increase in original LTV is associated with a 4.8 percentage point increase in default. We subtract 2.85 percentage points to account for the role of monthly payments, and are left with 1.95 percentage points. We attribute this remainder to adverse selection.

After debiasing, we are able to compute the relative roles of all three channels in explaining the overall correlation between leverage and default. Recall that column 1 suggested that a 10 point increase in original LTV was overall associated with a 7.8 percentage point increase in the probability of default. Of this, we attribute 25% to adverse selection (1.95/7.8), just over 36% to the payment channel (2.85/7.8), and the remainder (39%) to moral hazard.<sup>41</sup>

There are a two primary takeaways from this exercise. First, our results suggest that adverse selection, moral hazard, and the payment channel all play relatively comparable roles, at least in the sense that none is an order of magnitude larger than the others. Additionally, the roles of adverse selection and moral hazard are roughly comparable in the 5/1 ARM sample and the Option ARM sample. This is true both in levels and relative to one another: these estimates suggest that moral hazard explains 61% of the combined moral hazard/adverse selection effect, as opposed to 64% for option arms. Overall, our results suggest that the information asymmetries we study are empirically relevant: policy makers should not focus on payments

<sup>&</sup>lt;sup>41</sup>Note that there is no explicit need to de-bias the coefficient on current LTV. As noted above, our estimates suggest a 10 point increase in current LTV is associated with 2.5 percentage point increase in default.

to the detriment of selection and moral hazard. Further, our estimates using Option ARMs appear to be similar to those derived from more traditional mortgage products.

# 7 Simulations and Policy Analysis

In this section, we highlight the implications of our estimates for policy. After briefly discussing the relevance of our reduced form estimates we turn to analyzing a particular policy—an LTV cap—in a simulation framework. We view an LTV cap as a fairly representative example of the types of macroprudential regulations that have been implemented in various countries since the recession. In addition to concerns about asset price booms and busts, these policies are commonly motivated by moral hazard, under the assumption that limiting consumer leverage directly reduces the scope for ex-post default. In our analysis, we quantify the value of LTV caps in lowering default rates and identify the default externalities policymakers need to account for when designing such policies. The key innovation in our analysis, however, is the introduction of adverse selection. We argue that ignoring the role of adverse selection leads policymakers to (i) *overestimate* the reduction in defaults generated by a reduction in the LTV cap and (ii) *underestimate* the welfare loss generated because borrowers face higher interest rates and take smaller mortgages. To address the challenges of evaluating counterfactual policies in competitive markets with adverse selection, we use the equilibrium concept proposed by Azevedo and Gottlieb (2017).

#### 7.1 The Impact of Home Equity and Ex-Post Balance Writedowns

Our estimates on the causal effect of loan balances on default—or moral hazard—directly link to various policy proposals surrounding the regulation of consumer leverage regulation. Such estimates are essential, for instance, in order to predict the effectiveness of ex-post principal writedowns in preventing mortgage defaults. Our estimates in Table III suggest that, for the sample studied here, a 10 percentage point reduction in all borrowers' LTV at 24 months would have reduced defaults within a year by just over 15 percent. Relative to the literature, these estimates are on the large side, but not outside of normal bounds. For example, Bajari, Chu and Park (2008) find that a 25-point increase in the current LTV is necessary to generate a 15 percent increase in the default probability. Alternatively, Elul et al. (2010), find that borrowers with increasing CLTV from between 100 and 110 to between 110 and 120 raises the quarterly default hazard by about 30 percent of the mean.

After the crisis, a number of debt relief policies were enacted, for example the Home Affordable Mortgage Refinance Program Principal Reduction Alternative (HAMP PRA). Scharlemann and Shore (2016) use a kink in the schedule for HAMP PRA to analyze the effectiveness of the regulation. They estimate that

principal writedowns—balance reductions of 28 percent on average—reduced the quarterly delinquency hazard by 18 percent (from 3.8 percent per quarter to 3.1 percent).<sup>42</sup> However, their study examines only those who participated in the program (and hence were already delinquent), while our estimates consider the full population of active borrowers.

#### 7.2 A Model to Evaluate Ex-Ante Regulations

While our moral hazard effects are valuable in informing the design ex-post regulation, understanding the effects of ex-ante regulations on welfare—in the presence of adverse selection—requires (i) the specification of a model of borrower and lender behavior and (ii) an equilibrium concept. We begin with the model:

#### 7.2.1 Consumer Preferences

We consider a two period model. In the first, consumers purchase a home of fixed size and choose a mortgage. In the second, a stochastic ex-post home value is realized. Borrowers then either default or repay the balance on the loan.

In the first period, borrowers face a menu of contracts that each have two elements: a loan size/leverage  $L_k$  and a balance  $B(L_k)$ . Given a contract  $\{L_k, B(L_k)\}$  and a distribution of home prices, we characterize the observed portion of a borrower's ex-ante based on the model in Appendix 2:

$$U_{i}(L_{k}) = u(y_{0} - (H_{0} - L_{k})) + \beta \left[\underbrace{\int_{\underline{h}}^{B(L_{k}) - C_{i}} u(y_{1} - C_{i}) dF(H_{1})}_{\text{Default}} + \underbrace{\int_{B(L_{k}) - C_{i}}^{\overline{h}} u(y_{1} + H_{1} - B(L_{k})) dF(H_{1})}_{\text{Repayment}}\right].$$

As in the theoretical model, the only source of heterogeneity in  $U_i$  is  $C_i$ , the borrower's private costs of default. However, in practice, borrowers choose mortgages on the basis of a number of factors beyond just their default costs. Recall that the estimated correlation between the leverage choice and a borrower's private default costs was only 0.07. In a richly specified model, initial mortgage choice might also be a function of heterogeneity in each borrower's income, preferences (e.g. risk aversion or intertemporal elasticity of substitution), or period 0 knowledge of future  $C_i$ .

We abstract from these details and consider a simplified model in which borrowers' utility for a contract with a particular leverage choice is characterized by an observed portion, as defined above, and an independent, idiosyncratic error  $\epsilon_{iL}$ :

$$V_i(L_k) = U_i(L_k) + \epsilon_{iL}.$$

This error captures, in a reduced form way, all factors that influence borrowers with the same  $C_i$  to choose

<sup>&</sup>lt;sup>42</sup>Ganong and Noel (2017) also study underwater borrowers, find no effect of changes in borrowers equity.

different contracts. When the variance of  $\epsilon_{iL}$  is high, there is a weak relationship between  $C_i$  and the chosen L. When the variance is low, the correlation increases.

It is convenient to specify  $\epsilon_{iL}$  to be type 1 extreme value, in which case a borrower's choice probability for a given L can be written as:

$$P_{ik} = \frac{e^{\gamma U_i(L_k)}}{\sum_{k'} e^{\gamma U_i(L_{k'})}},$$

where  $\gamma$  is a viscosity parameter determined by the variance of  $\epsilon_{iL}$ . Of course, this specification imposes a standard independence of irrelevant alternatives (IIA) assumption, which may not hold in a more sophisticated model of heterogeneity across borrowers.

#### 7.2.2 Lender Profits

With these choice probabilities in hand, computing lender profits is straightforward. We assume lenders are able to recover a fraction  $\delta \leq 1$  of what the home is worth in the case of default. The expected profits of a lender selling contract  $\{L_k, B(L_k)\}$  to borrower i with private default cost  $C_i$  are:

$$\pi(L_k, B(L_k); C_i) = -L_k + \frac{1}{1 + r_f} \left[ \underbrace{\int_{\underline{h}}^{B(L_k) - C_i} \delta H_1 dF(H_1)}_{\text{Default}} + \underbrace{\int_{B(L_k) - C_i}^{\overline{h}} B(L_k) dF(H_1)}_{\text{Repayment}} \right].$$

The expected profits of a lender are the profits for each individual i, multiplied by the probability that i chooses contract k, integrated over the distribution of  $C_i$  (specified here as G(C)):

$$\Pi_k = \int P_{ik} \pi(L_k, B(L_k); C_i) dG(C).$$

#### 7.2.3 Equilibrium Concept

There is no clear consensus on the appropriate definition of equilibrium in competitive markets with adverse selection (Chiappori and Salanié, 2013). Furthermore, because equilibria often fail to exist under standard concepts, e.g. Rothschild-Stiglitz, evaluating the counterfactual implications of policy can be difficult. However, a recent development by Azevedo and Gottlieb (2017) characterizes an equilibrium concept that is both robust—an equilibrium always exists—and straightforward to implement in a variety of applications. Equilibria of this form satisfy three requirements: (i) consumers optimize over the available set of contracts, (ii) lenders make zero profits on each contract, and (iii) there is free entry, in the sense that the equilibrium is robust to small perturbations, as defined formally in Azevedo and Gottlieb (2017).

For the purposes of simulation, using this equilibrium concept is straightforward. We calculate equilibrium in what Azevedo and Gottlieb (2017) call a perturbation. We propose a fixed set of contracts

(in the example presented, every integer LTV between 50 and 100). We then consider a mass of behavioral borrowers—uniformly distributed across contracts—equal to 1 percent of the population, who always choose a given contract. Behavioral borrowers pay back the loan in all states of the world and as a result are costless to the lender. We use a fixed point algorithm to determine equilibrium. In each iteration, consumers choose optimally taking prices as given, and interest rates are adjusted down or up for profitable or unprofitable contracts. Convergence is achieved when the absolute value of profits across all contracts fall below a predefined threshold. The existence of behavioral borrowers is crucial for convergence to intuitive equilibria. Because behavioral borrowers are costless, the interest rate on any contract that is only purchased by these types is reduced until either (i) a risky borrower is indifferent between the contract and his current choice or (ii) the interest rate reaches the risk free rate. This rules out equilibria with contracts that have arbitrarily high prices and only make zero profits because they are not chosen.

#### 7.2.4 Calibration

We calibrate three features of the simulation to the estimates from Table IV. We define the mean and variance of the private costs of default based on those estimated in Column 4 of IV. Furthermore, we choose  $\gamma$ , or equivalently the variance of  $\epsilon_{iL}$ , so that the correlation between borrowers' choice of L and  $C_i$  in Regime I below matches the estimated  $\rho_{\varepsilon v}$  in Column 4. All other parameters are set based on the data when possible and explicitly described in the bottom panel of Table VI. For the purposes of the simulation, we assume that borrowers have exponential utility, with CARA coefficient a.

#### 7.3 Welfare Implications of an LTV Cap

We consider the implications of a decreased LTV cap, that is, a limit on the initial loan provided by lenders. This can be thought of as roughly the mirror image of a standard policy in insurance markets: a mandated minimum level of coverage. We evaluate three policy regimes:

- (I) LTV Cap of 100: In the first regime, lenders do not observe  $C_i$ , and equilibrium is as discussed above, with all loans making zero profits. The set of potential contracts contains all original LTVs between 50 and 100.
- (II) LTV Cap of 90 (No Supply Response): The second regime presents a naive view of the impact of an LTV cap of 90, ignoring the impacts of adverse selection. This regime evaluates the choices made by borrowers if an LTV cap of 90 were implemented but lenders did not otherwise adjust their contracts. As a result, lenders may make positive or negative profits under this regime.

(III) LTV Cap of 90 (With Supply Response): The final regime considers the equilibrium allocation of credit when lenders are able to endogenously adjust contracts in response to a change in the LTV cap.

#### 7.3.1 A Naive Evaluation of an LTV Cap: No Supply Response

We first consider a comparison of Regimes I and II, which can be thought of as the anticipated response to an LTV cap for a naive policymaker. For these purposes, we consider a naive regulator to be one who understands borrower preferences and can anticipate the contracts borrowers will choose from any given set, but who disregards adverse selection. Such a policymaker believes that the proportion of defaults for a given contract does not depend on the population purchasing that contract, and hence that there will be no supply response to a change in the LTV cap. The intuition behind this comparison is demonstrated by the dark and light gray bars in Figure V. This figure shows results with an exaggerated degree of adverse selection, to better present the patterns across the three regimes, while Table VI presents numbers based on simulations calibrated to the empirical results.

The dark gray bars illustrate the allocation of original LTV under Regime I and exhibit a basic pattern of adverse selection. While all borrowers would prefer initial loans with LTVs of 100 in a world with perfect information, the clustering of the riskiest borrowers raises the interest rate of a 100 LTV loan significantly. As a result, safe borrowers take smaller loans to distinguish themselves from risky types and avoid paying inflated interest rates. In other words, adverse selection leads to a partially separating equilibrium.

The expected impact of the regulation from the perspective of a naive regulator is illustrated with the light gray bars. Under the naive view, the only borrowers impacted by the regulation are those initially choosing LTVs above 90. The borrowers who choose contracts with original LTVs below 90 in Regime I will continue to do so, while the majority of those choosing original LTVs above 90 will bunch close to the LTV cap.<sup>43</sup> Furthermore, the naive view will expect a significant reduction in defaults generated by the regulation. Because it assumes no heterogeneity across borrowers in default propensities, borrowers who choose an LTV of 90 under Regime II are expected to default at the same rate as borrowers choosing an LTV of 90 under Regime I.

Columns 1 and 2 of Table VI compare Regimes I and II. There is indeed a reduction in loan size, from \$278 thousand to \$260 thousand and a corresponding expected reduction in average interest rates from 14.8 to 12.1 percent. Because Regime II does not allow lenders to change interest rates, this reduction is entirely the result of borrowers choosing smaller loans with lower rates. Furthermore, by failing to account for the inherent riskiness of the borrowers who are shifted from LTVs above 90 to LTVs below 90, the naive

 $<sup>^{43}</sup>$ Because borrowers have a random component  $\epsilon_{iL}$  of their preference for contracts, and because of the IIA assumption, borrowers who initially chose LTVs above 90 will not strictly choose contracts at 90. Rather, they will distribute their choices across remaining loans such that the relative choice probabilities are the same before and after the regulation.

regulator expects the reduction in defaults to be significantly larger than it actually is, even without a supply response. The naive view suggests that an LTV cap of 90 would cut the fraction of defaults by approximately 20 percent, from 0.11 of borrowers to just under 0.09. Appropriately accounting for the risk of the borrowers initially allocated above 90 reveals the true reduction to be closer to 13 percent.

#### 7.3.2 Allowing a Supply Response

In addition to overstating the reduction in defaults generated by the regulation, the naive view understates the reduction in mortgage size generated by knock-on effects of the regulation. Reducing the LTV cap does indeed force some risky borrowers to decrease their LTV to 90. However, as a result, the interest rates on 90 LTV loans must also rise. Correspondingly, some borrowers who previously chose LTVs of 90 will choose slightly smaller loans, thereby leading lenders to increase interest rates on those smaller loans and causing further knock-on effects. In the presence of adverse selection, leverage can be seen as a sorting device. Eliminating high LTV loans does not eliminate the incentive of borrowers to differentiate themselves, but instead forces them to do so over a smaller range of loans. The leftward shift of the white bars in Figure V relative to the light gray bars demonstrates the additional reduction in mortgage size due to knock-on effects. In the calibrated simulations of Regime III, shown in the third column of Table VI, the knock-on effects cause an additional reduction in loan size of more than \$200 on average. Furthermore, because lenders in Regime III appropriately account for the reallocation of risky borrowers, the interest rates of all contracts rise. This brings the average interest rate from 12.1 to 12.7 percent. As a result, the average borrower has a final balance that is more than \$1000 larger under Regime III than Regime II. The reduction in loan size and increased borrower balance combine to generate a welfare loss that is approximately \$1,100 larger relative to that expected by a naive lender.

Optimal regulation involves balancing reductions in defaults with the welfare loss that results from borrowers facing higher interest rates and taking smaller loans. In the simulations provided here, a naive regulator overstates the reduction in defaults by close to 7 percent and underestimates the welfare loss due to reductions in loan size (and higher interest rate schedules) by approximately \$1,100 per borrower. While our model is highly stylized, the fundamental intuition is clear: when adverse selection is present, policy makers must weight the benefits of preventing defaults against the knock-on effects that impact all borrowers when risky types are forced to choose new contracts.

# 8 Conclusion

In this paper, we empirically separate moral hazard from adverse selection in the mortgage market. We do so by exploiting a natural experiment resulting from two features of Option ARMs: fixed payments and variable interest rates. Because monthly payments do not change, the balances borrowers owe are a direct function of market interest rates. This creates a distinction between borrower's initial leverage choices and the balances they owe ex-post. To isolate plausibly exogenous variation in balances, we focus on difference-in-difference variation in interest rates that comes as the result of the financial index used to determine rate adjustments. Because of the unexpected divergence between LIBOR and Treasury rates during the crisis, borrowers experienced substantially different balances as a function of the loan's index and origination month.

This variation in borrower's balances allows us to construct a series of instruments to identify the causal effect of home equity on default—the moral hazard effect—and subsequently to back out the role of adverse selection. We find significant evidence of both information asymmetries. Moral hazard is responsible for 60-70 percent of the baseline correlation between leverage and default, while adverse selection is responsible for the remaining 30-40 percent. The estimated moral hazard effect at 24 months suggests that a policy that reduced all borrower's loan-to-values by 10 points at 24 months would have reduced defaults by over 4 percentage points.

To analyze the implications of adverse selection for ex-ante macroprodential policy, we construct and simulate a simple model of borrowers leverage choice and default using our estimated parameters. We show that, in the presence of adverse selection, policies such as loan-to-value caps may have knock-on-effects that impact *all* borrowers in equilibrium. Such regulations will cause all borrowers to face higher interest rates and choose smaller loans. Optimal mortgage policies must factor in this adverse impact on borrowers.

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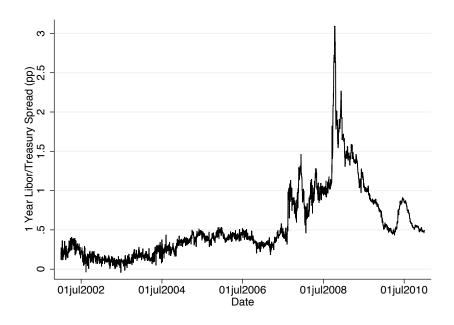
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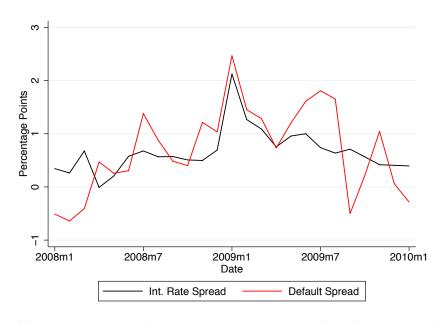
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FIGURE I
PANEL A: SPREAD BETWEEN LIBOR AND TREASURY INCREASED DRAMATICALLY DURING CRISIS



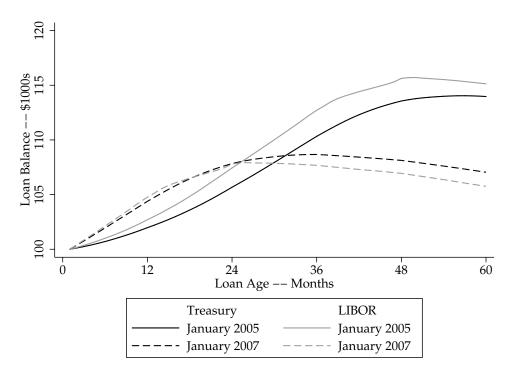
PANEL B: SPREAD IS MIRRORED IN INTEREST RATES AND DEFAULT PATTERNS FOR ARMS



Top panel shows spread between 1-year LIBOR and 1-year Constant Maturity Treasury (CMT) between 2002 and 2010. The black line in the bottom panel shows the difference in (reset) rates between LIBOR-indexed loans and Treasury-indexed loans resetting in the corresponding month. The lighter line shows the difference in the one year default probability between LIBOR and Treasury indexed 5/1 ARM loans resetting in that month.

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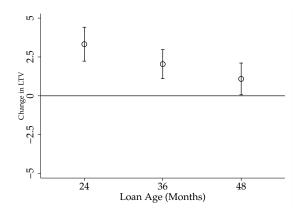
 $FIGURE\ II \\ Index \times Origination\ Month\ Generates\ Difference-in-Difference\\ Variation\ in\ Balance\ Trajectories\ for\ Option\ ARMs$ 



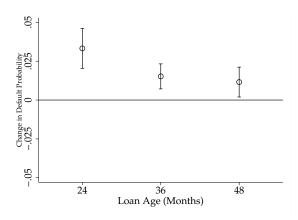
Simulated balance trajectories for \$100,000 LIBOR- and Treasury-indexed loans originated in January 2005 or January 2007. Trajectories assume margin of 3.5 percent and initial payment based on 1.75 percent teaser. Treasury refers to 1-year MTA, LIBOR refers to 3-month duration.

# FIGURE III REGRESSIONS OF DEFAULT AND CREDIT SCORE ON INSTRUMENT FOR HOME EQUITY

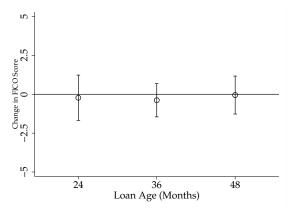
### PANEL A: INSTRUMENT RELEVANCE—INSTRUMENT PREDICTS CURRENT LOAN-TO-VALUE



PANEL B: REDUCED FORM—INSTRUMENT PREDICTS DEFAULT ACROSS LIFECYCLE

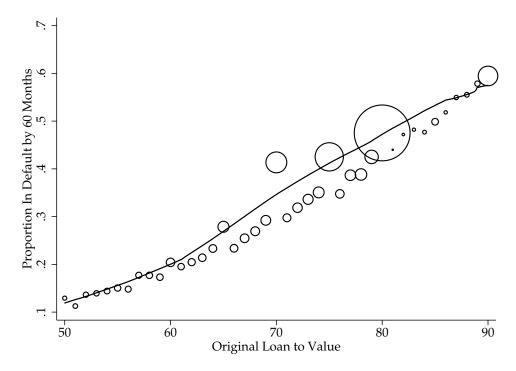


PANEL C: INSTRUMENT EXOGENEITY—INSTRUMENT DOES NOT PREDICT CREDIT SCORE



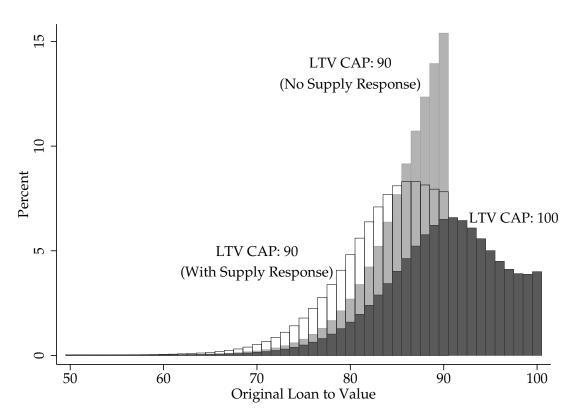
OLS regressions of outcomes on simulated instrument including origination month and index fixed effects. The simulated instrument is the mechanical calculation of balance based upon the borrowers' index choice and origination month. Margin is fixed to 3.5 for all borrowers, original loan to \$100,000 and initial monthly payment is based on 1.75 percent teaser rate. Top panel shows the outcome of default within one year at 24, 36, and 48 months, where default is defined as being 60 or more days past due. Bottom panel shows the outcome of borrowers FICO scores for those remaining at 24, 36 and 48 months.

FIGURE IV
ORIGINAL LTV IS POSITIVELY CORRELATED WITH DEFAULT WITHIN 60 MONTHS



Hollow dots show the average proportion of loans defaulting within the first 60 months for each 1-point bin of original loan-to-value. Size of dots is proportional to number of borrowers within each bin. Default is defined as 60 or more days past due. The solid line shows a local linear smoothing of the raw data. The full sample of Option ARMs is included.

FIGURE V
EFFECT OF LTV CAP OF 90 ON LEVERAGE: WITH AND WITHOUT SUPPLY RESPONSE



Bars show simulated proportion of borrowers choosing each original LTV under three regimes. The dark gray bars show equilibrium LTV choices at an LTV cap of 100, the light gray show borrowers' LTV choices after a reduction in the LTV cap to 90, but allowing no changes in contracts below 90. White bars show equilibrium LTV choices with an LTV cap of 90 allowing for the supply response. Figure is based on exaggerated level of adverse selection. Table VI shows appropriately calibrated results.

# **Tables**

TABLE I
SUMMARY STATISTICS: BALANCE ACROSS INDICES

	Par	nel A: Option	n ARM Samp	ole
	Treas	ury	LIB	OR
	Mean	SD	Mean	SD
FICO Score	706.1	45.9	713.8	45.1
Original Balance	370.5	264.4	346.1	282.1
Loan for Purchase	0.33		0.42	
No/Low Documentation	0.79		0.77	
Primary Residence	0.77		0.68	
Condo, Co-op or Multifamily	0.14		0.16	
Prepayment Penalty	0.99		0.94	
Margin	3.21	0.53	2.85	0.51
Original LTV	76.6	8.40	77.0	8.30
State:				
- California	0.46		0.35	
- Florida	0.14		0.16	
- Arizona	0.043		0.040	
- Nevada	0.037		0.054	
Origination Year:				
- 2004	0.081		0.31	
- 2005	0.41		0.35	
- 2006	0.43		0.24	
- 2007	0.082		0.089	
Observations	490,132		45,199	
	P	anel B: 5/1	ARM Sample	
	Treas	ury	LIBO	OR
	Mean	SD	Mean	SD
FICO Score	728.7	50.8	718.1	52.3
Origination Balance	483.6	302.7	439.0	313.6
Loan for Purchase	0.24		0.20	
No/Low Documentation	0.52		0.70	
Primary Residence	0.87		0.84	
D ' , D 1,			4.00	

	Treas	ury	LH	BOR
	Mean	SD	Mean	SD
FICO Score	728.7	50.8	718.1	52.3
Origination Balance	483.6	302.7	439.0	313.6
Loan for Purchase	0.24		0.20	
No/Low Documentation	0.52		0.70	
Primary Residence	0.87		0.84	
Prepayment Penalty	1		1.00	
Margin	2.77	0.31	2.36	0.39
Original LTV	74.3	9.02	76.2	8.37
State:				
- California	0.48		0.40	
- Florida	0.063		0.093	
- Arizona	0.032		0.041	
- Nevada	0.021		0.029	
Origination Year:				
- 2002	0.029		0.0072	
- 2003	0.16		0.058	
- 2004	0.25		0.16	
- 2005	0.37		0.25	
- 2006	0.12		0.34	
- 2007	0.051		0.17	
Observations	109,214		344,594	

Summary statistics for full sample of Option ARMs (Panel A) and 5/1 ARMs (Panel B). Treasury refers to loans indexed to Treasury rates, LIBOR refers to those indexed to LIBOR.

FIRST STAGE: INSTRUMENTS PREDICT REALIZED NEGATIVE EQUITY, LOAN-TO-VALUE, INTEREST RATES, AND PAYMENTS TABLE II

	1	Panel A: Option ARMs—Observed / Imputed Equity on Simulated Instruments	on ARMs—O	bserved/Imp	uted Equity	on Simulated	Instruments	
	Condi	Conditional on Survival to 24 Months	vival to 24 Ma	onths	Full Sa	mple (Impute	Full Sample (Imputed Current Equity)	uity)
	Home Equity	dunty	Loan-to-Value	-Value	Home Equity	equity	Loan-to-Value	Value
Simulated Home Equity (\$100,000s)	1.345*** (0.214)	$0.795^{***}$ (0.197)			1.349*** $(0.226)$	0.339** (0.164)		
Simulated Loan-To-Value			3.559*** (0.621)	$1.736^{***}$ $(0.471)$			2.632*** (0.463)	0.545 (0.363)
F (Simulated Instrument) F (Fixed Effects) N	39.5 10.3 265134	16.3 7.1 265134	32.8 5.0 268364	13.6 11.3 268364	35.7 11.3 443600	4.2 6.8 443600	32.3 8.1 443600	2.3 8.5 443600
Orig. Month/Index FEs MSA FEs First Controls	Yes No	Yes Yes	Yes	Yes Yes	Yes	Yes Yes	Yes No	Yes Yes
ruli Colludis	ב ב	ies	INC	Ico	DNI INC	ICS		S

month to determine interest rates but fixing all other loan terms to standard values: a margin of 3.5%, an initial minimum payment based upon a 1.75% teaser rate, home price appreciation equal to the national average, and the assumption that the borrower always makes minimum payments. With these terms, home equity can be calculated mechanically. The F(simulated instrument) is the F-statistic from this regression, while F(Fixed effects) is the F-statistic from regressions that include the full set of interactions between origination month and index type as instruments. Full controls refers to fixed effects for is the coefficient from regressing borrower's true equity value, measured either as the loan-to-value ratio (in percentage terms) or as the level of negative equity in \$100,000s, on the simulated instrument for that equity. The simulated instrument is calculated using the borrowers true index and origination index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrower's FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* First stage regressions of measures of borrower equity on instruments for equity based on borrower's index and month of origin. Displayed in each column denotes 1% significance.

TABLE III
SEPARATING ADVERSE SELECTION AND MORAL HAZARD:
THE IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON 1 YEAR DEFAULT PROBABILITIES

	Panel A: OL	S and IV Reg	ressions at 24	Months Inclu	ding Current N	legative Equit
	Baseline	OLS	IV	Baseline	OLS	IV
Original Loan-to-Value	0.586***	0.252***	0.331***	0.721***	0.407***	0.260***
· ·	(0.046)	(0.054)	(0.118)	(0.026)	(0.037)	(0.047)
Current Negative Equity in		0.059***	0.045**		0.061***	0.089***
\$100,000s		(0.006)	(0.021)		(0.005)	(0.010)
Mean of Dep. Var	0.264	0.264	0.264	0.264	0.264	0.264
N	265134	265134	265134	265134	265134	265134
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	No	No	No	Yes	Yes	Yes
Full Controls	No	No	No	Yes	Yes	Yes
	Panel B: O	LS and IV Re	gressions at 2	4 Months Incl	uding Current I	Loan-to-Value
	Baseline	OLS	IV	Baseline	OLS	IV
Original Loan-to-Value	0.586***	-0.059	-0.241	0.721***	0.244***	0.229***
	(0.046)	(0.056)	(0.234)	(0.026)	(0.053)	(0.050)
Current Loan-to-Value		0.573***	0.735***		0.402***	0.415***
		(0.029)	(0.212)		(0.037)	(0.041)
Mean of Dep. Var	0.264	0.264	0.264	0.264	0.264	0.264
N	265134	265134	265134	265134	265134	265134
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	No	No	No	Yes	Yes	Yes
Full Controls	No	No	No	Yes	Yes	Yes

OLS and IV regressions of default between 24 and 36 months on borrowers original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,000s (Panel A), or current loan-to-value (Panel B). Default is defined as 60 or more days past due. Baseline refers to OLS regressions omitting current equity. IV regressions include the full set of interactions between index and origination month as instruments for current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrower's FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE IV

JOINT ESTIMATES OF THE IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON
1 YEAR DEFAULT PROBABILITIES AND LEVERAGE DEMAND

		Negative Equity			Loan-to-Value	
	24 Months	36 Months	48 Months	24 Months	36 Months	48 Months
Current Negative Equity in \$100,000s	0.529*** (0.048)	0.371*** (0.058)	0.232* (0.136)			
Current Loan-To-Value				1.811*** (0.194)	1.046*** (0.199)	0.420 (0.358)
ρ: Correlation of Errors in Default and Leverage Choice	0.036** (0.017)	0.048** (0.020)	0.050 (0.044)	0.067*** (0.016)	0.071*** (0.019)	0.078** (0.037)
Default Threshold S.D. of Default Error N	0.906 1.890 263177	1.707 2.697 162103	3.822 4.313 106921	1.338 0.552 263177	1.681 0.956 162103	3.144 2.378 106921
Origination Quarter FEs Index FEs State FEs Full Controls	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes

Estimates from joint model of leverage demand and default choice. Table shows coefficient on current equity at 24, 36 and 48 months, where current equity is defined as either the level of negative equity in \$100,000s (or current loan-to-value). \$\rho\$ displays the estimated correlation between the errors in the leverage and default equations, capturing adverse selection. Also shown are the default threshold for a borrower at the mean covariate level, and the standard deviation of the error in the default choice in units of current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrower's FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \*denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE V
IDENTIFYING THE IMPACT OF PAYMENTS:
INTEREST RATE SHOCKS AND DEFAULT

	Panel A:	Decomposition—Effect	ts on Age 24–36 Montl	n Sample
	OLS	OLS	OLS	Bias Correction
Original Loan-to-Value	0.781*** (0.033)	0.480*** (0.041)	0.482*** (0.041)	0.195
Current Loan-to-Value		0.257*** (0.018)	0.257*** (0.018)	0.257
Monthly Payment (\$1000)			-0.000473** (0.000)	0.285
Mean of Dep. Var. N	0.27 254845	0.27 254845	0.27 254845	
Coefficient of Orig. LTV on Monthly Payment	5.02 (0.644)			
Origination Month FEs	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes
MSA FEs	Yes	Yes	Yes	Yes
Full Controls	Yes	Yes	Yes	Yes
	Panel B: Caus	sal Effect of Reset Inter	est Rates on One Year	Default Rate
	OLS	IV	OLS	IV
Monthly Payment (\$1000)	-0.00148* (0.001)	0.0246** (0.010)	-0.00571*** (0.002)	0.0567** (0.026)
Mean of Dep. Var. N	0.070 100200	0.070 100189	0.070 100200	0.070 100189
Origination Month FEs	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes
Servicer	No	No	Yes	Yes
MSA FEs	No	No	Yes	Yes
Full Controls	No	No	Yes	Yes

Panels A and B display results from OLS and IV regressions with the binary outcome of default for 5/1 ARM. Default is defined as 60 or more days past due. Panel A focuses on loans after reset, between 60 and 72 months for borrowers. OLS specifications, in columns (1), (2), (4), and (5) includes regressions of default on monthly payments as well as leverage features (original and current LTV), and contract terms at origination (the original interest rate and margin). IV specifications instrument for monthly payments or reset rates with a difference-in-difference interaction of origination month and index type. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance. We also include indicators for each 20-point bin of borrower's FICO credit scores, loan originator and servicer fixed effects, and controls for 5-point bins of current CLTV. Standard errors are clustered at the MSA level. Panels B displays results from a sample of borrowers taken from 24–36 months, to illustrate leverage correlations on a sample for which the initial rate is still applicable. These specifications do not include instruments. Column 1 includes only original LTV, as well as origination month and index type. Column 2 adds current LTV, while column 3 includes monthly payment as well. Columns 4–6 add the usual set of full controls. Additional coefficients capture the in-sample relationship between origination LTV on monthly payment, either with minimal or the full set of controls. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 1% significance.

 $TABLE\ VI$  Simulation Results: The Impact of a Reduction in the LTV Cap From 100 to 90

	Col. 1: LTV Cap of 100	Col. 2: LTV Cap of 90 No Supply Response	Col. 3: LTV Cap of 90 With Supply Response
Average Loan Size (Thousands)	\$278.2	\$260.6	\$260.4
Average Interest Rate	14.8%	12.1%	12.7%
Average Balance (Thousands)	\$319.3	\$292.1	\$293.4
Defaults	11.05%	9.57%	9.64%
Naive Defaults	-	8.88%	-
Additional Welfare Loss Due to Su	pply Response (Col. 2 vs. Col 3, in Thousan	nds)	\$1.1
		Parameters	
	Initial Price: $H_0 = $370.5$ CARA Coefficient: $a=0.0005$	Final Value: $H \sim N(\mu_1 = 617.5, \sigma_1 = 200)$ Viscosity: $\gamma = 0.0793$	Proportion Behavioral: 1% $\beta = \frac{1}{1+r_f} = 0.95$
	Prop. Recovered in Default: $\delta = 0.25$	$C_i \sim N(0.338\mu_1, 0.552\mu_1)$	Borrowers: $N = 1000$

Simulations from structural model described in Section 7. CARA utility assumed, 1000 simulated borrowers, with 1% behavioral. Viscosity set to match estimated  $\rho=0.067$ . The first column shows equilibrium outcomes with an LTV cap of 100. The second column shows borrower responses to the removal of all contracts with initial LTV between 90 and 100, holding fixed all contracts with initial LTV less than 90. Naive defaults refer to expected defaults calculated ignoring borrower heterogeneity and extrapolating from default probabilities at each LTV with an LTV cap of 100. The third column shows equilibrium outcomes with an LTV cap of 90. CV calculated based on expected utility prior to realization of EV1 error.

# **Internet Appendix: For Online Publication**

### A Model

We propose a two-period model of borrower's leverage demand and default choice, following Brueckner (2000). Borrowers differ in a single dimension, which we refer to as the private default cost. This black box parameter represents all factors that influence the borrower's default decision at a given level of home equity. There are two primary takeaways from the model. First, the distribution of private default costs in the population determines the magnitude of the moral hazard effect, i.e., the increase in defaults generated by a given change in the loan balance. Second, a Spence-Mirrlees single crossing condition holds: borrowers with lower private default costs (i.e. risky borrowers) are relatively more willing to accept large balances.

In period 0, borrowers choose what portion of a risky housing purchase to finance. In period 1, the value of the home is realized, and borrowers choose whether to pay off their loan or to default. Mortgage contracts have two dimensions: the period 0 loan and the period 1 balance. We consider a non-recourse environment: in default, the borrower cedes the right to the home and is relieved of the loan balance.

Formally, let time be indexed by  $t \in \{0,1\}$  and borrowers be indexed by i. Borrowers must purchase a home with initial price  $H_0$  and uncertain period 1 price  $H_1$  distributed on support  $[\underline{h}, \overline{h}]$  according to CDF  $F(H_1)$ . Lenders offer contracts of the form  $\{L, B(L)\}$ , where L is the value of the loan provided to the borrower in period 0, and B(L) is the balance due on the loan in period 1.<sup>44</sup> In general B(L) is increasing in L, that is, lenders demand higher balances for larger loans. A high leverage mortgage is one with a large L and correspondingly, a large B(L).

Borrowers have per-period utility of consumption  $u(\cdot)$ , which is increasing and concave, receive income  $y_t$  in each period, which is not stochastic, and discount the future according to  $\beta$ . Each borrower i has privately known costs associated with defaulting,  $C_i$ , which captures the difference in dollar terms between defaulting and not defaulting.

#### **Default Choice**

In period 1, borrowers realize the value of their home and choose between repaying and defaulting. A borrower who repays retains the value of the home for net income  $y_1 + H_1 - B$ , while a borrower who defaults avoids paying the mortgage balance but incurs the default cost:  $y_1 - C_i$ . Borrowers choose to default

<sup>&</sup>lt;sup>44</sup>While other terms are often used to define mortgage contracts, these are usually equivalent to simple transformations of L and B in the two-period case. We could alternatively speak of the down payment  $(H_0 - L)$ , the interest rate  $(\frac{B}{L} = 1 + r)$ , and the original loan-to-value  $\frac{L}{H_0}$ .

when

$$H_1 - B < -C_i$$
.

Borrowers with a low  $C_i$  are quicker to default, that is, for the same B they will default at higher home values.

This default rule demonstrates the importance of private default costs in determining the strength of the moral hazard effect. For a given  $C_i$ , the expected fraction of borrowers defaulting at balance B is  $F(B - C_i)$ , and the marginal effect of an increase in B is  $f(B - C_i)$ . The calculation becomes even more complicated with heterogeneity in  $C_i$ , as one must integrate over the set of borrowers at a given B.

#### **Contract Choice**

In period 0, borrowers know  $C_i$  but face uncertainty about the period 1 home value. As a result, they choose  $\{L, B\}$  to maximize

$$U(L,B;C_i) = u(y_0 - (H_0 - L)) + \beta \left[ \int_{\underline{h}}^{B - C_i} u(y_1 - C_i) dF(H_1) + \int_{B - C_i}^{\overline{h}} u(y_1 + H_1 - B) dF(H_1) \right].$$

The term in brackets represents the expected period one utility, with the first term giving utility in the case of default and the second utility with repayment.

Note that the borrower's overall utility is increasing in the loan size *L*:

$$U_L(L, B; C_i) = u'(y_0 - H_0 + L) \ge 0.$$

Additionally, borrower utility is decreasing in the balance:

$$U_B(L, B; C_i) = -\beta \int_{B-C_i}^{\bar{h}} u'(y_1 + H_1 - B) dF(H_1) < 0.$$

This result is unsurprising. Holding the balance fixed, borrowers prefer larger loans, and holding the loan size fixed, borrowers prefer a smaller balance.

There are a variety of reasons why borrowers prefer to take out large loans. In the presence of credit constraints, L provides a method of smoothing consumption over time, so borrowers can consume period 1 income and the expected gains from the home in period 0. However, even if it is possible to borrow at the risk free rate, borrowers still value mortgage loans because they provide a form of insurance against low realizations of  $H_1$ .<sup>45</sup> An increased B effectively allows borrowers to give up consumption when  $H_1$  is high

<sup>&</sup>lt;sup>45</sup>Assuming mortgage debt is non-recourse, but other debt cannot be forgiven.

in exchange for sure consumption (in the form of L) even when  $H_1$  is low.<sup>46</sup>

At actuarily fair prices, borrowers prefer to take advantage of the insurance provided by a mortgage. In a totally frictionless context,<sup>47</sup> borrowers will choose an extreme form of full insurance when offered a fair price. In particular, they will take out as large a loan as possible and default on the loan in all states of the world. While this may seem surprising, it is a standard result: a risk averse agent will be willing to sell a risky asset for its expected value.

Yet borrowers with different values of  $C_i$  do not value this insurance equally. In fact, a Spence-Mirrlees single crossing condition holds:

$$\frac{\partial \left(\frac{U_B}{U_L}\right)}{\partial C_i} = \frac{-\beta u'(y_1 - C_i)f(B - C_i)}{u'(y_0 - H_0 + L)} < 0.$$

Because low  $C_i$  are more likely to default, all else equal, they are more likely to take advantage of the insurance provided by the mortgage. As a result, they are willing to accept smaller increases in the loan size L in exchange for the same increase in the balance B.

If borrowers with different levels of  $C_i$ , say  $C_R < C_S$  (where R and S denote risky and safe borrowers), are offered the same menu of contracts, the single crossing condition constrains the set of contracts chosen. In particular, if these types buy contracts  $\{L_R, B_R\}$  and  $\{L_S, B_S\}$ , respectively, it must be the case that  $L_R \ge L_S$ . Of course, for borrower  $C_S$  to be willing to accept a smaller loan, it must also be the case that  $B_R \ge B_S$ . Further, if  $C_R$  and  $C_S$  buy different contracts along one dimension, both inequalities must hold strictly.

<sup>&</sup>lt;sup>46</sup>The mortgage literature refers to this as the put option contained in a mortgage: the borrower retains the right to sell the home to the bank in exchange for the balance on the mortgage.

<sup>&</sup>lt;sup>47</sup>By totally frictionless, we mean a context with (i) borrowing and lending at the risk free rate, (ii) no default costs to the borrower, and (iii) lenders who can perfectly recover the home value after a default.

## **B** Robustness

In this appendix, we describe a series of robustness checks intended to supplement the primary analysis.

Table A.II considers how the results in Table III change across three relevant subgroups: (i) in states with full recourse versus those with limited recourse, (ii) for borrowers providing full documentation versus those providing limited or no documentation, and (iii) for home purchases versus refinances. In each panel, we show the baseline relationship between original LTV and default for the relevant subgroup, then IV regressions with  $E_{ijt}$  defined first as negative equity and next as current LTV. All specifications include the full set of controls.

#### **State Recourse Status**

The most notable difference between states with full versus limited recourse<sup>48</sup> is in the strength of the estimated moral hazard effect. Both categories show a significant baseline correlation between original LTV and default. However, the impact of  $E_{ijt}$  on default—defined either as current negative equity or LTV—is large and statistically significant in limited recourse states, and near zero in full recourse states. This pattern is intuitive: in states where borrowers are responsible for the loan balance even in default, the marginal incentive to default generated by an increase in the current balance is low. Perhaps more surprising is that both types of states show strong evidence of adverse selection across OLS and IV specifications. In both cases, original LTV is strongly associated with default, controlling for current incentives to default. It should be noted that the sample size is much smaller in full recourse states, and the estimates are correspondingly less precise.

#### Documentation

Dividing borrowers by documentation provided, shown in Panel B of Table A.II, suggests that income verification may be an important factor in screening borrowers. The results for the low or no documentation sample largely match the full sample. In contrast, in the sample providing full documentation, the entirety of the raw correlation between leverage and default is explained by moral hazard. The optimistic view of this result is that documentation solves the adverse selection problem: the additional information on income allows lenders to distinguish an individual's riskiness before offering a set of contracts. However, because we do not observe income, we are also not perfectly able to control for the information set of the lender in

<sup>&</sup>lt;sup>48</sup>By state recourse status, we refer to a state's provisions regarding a lender's ability to recover any balance that exceeds the value of the home in the case of default. We categorize states as full or limited recourse on the basis of that in Rao and Walsh (2009), with full recourse referring to states with strong provisions regarding deficiency judgments and limited recourse referring to those with mixed, weak, or nonexistent provisions.

the full documentation sample. As a result, the coefficient on original LTV in the full documentation sample pools an adverse selection effect with any steering of borrowers by lenders on the basis of income.

#### Purchases vs. Refinances

The differences between those purchasing homes versus those refinancing existing mortgages, shown in Panel C of Table A.II, are less severe than those in Panels A and B. While the baseline correlation between original LTV and default is higher in the refinance sample, both show comparable moral hazard effects: a 10 point increase in the current LTV causes an average of just over 4 percent more defaults within a year on average in both samples. However, the estimated adverse selection effects are slightly smaller in the purchase sample and only significant when  $E_{ijt}$  is defined as current negative equity.

#### Loans at 48 Months

The results for loans at 48 are similar to those at 24 months, if somewhat muted. Appendix Table A.III presents identical regressions to those in Table III, except with current  $E_{ijt}$  defined at 48 months and the dependent variable defined to be default between 48 and 60 months. With full controls, the baseline relationship between original LTV and default is somewhat lower than at 24 months, and the proportion of the correlation due to adverse selection somewhat higher (greater than 50 percent in the IV specifications). Further, the estimated moral hazard effects are smaller, and insignificant when  $E_{ijt}$  is defined to be current LTV. Given the weakness of the instrument at 48 months, these estimates should be interpreted cautiously, but they largely support the results found in Table III. Results at other cross-sections are similar.

#### **Cumulative Default Probabilities**

The regressions in Table III take an indicator for default within one year as the dependent variable. Doing so poses two potential issues. First, considering the default probability between 24 and 36 months limits the sample to borrowers who are still active at 24 months. This generates a potential source of bias, as borrowers who default or prepay in the early years of the loan may differ from the larger population, or may be responding endogenously to new knowledge of their anticipated future balance. Second, lenders may be more concerned with whether a borrower defaults at all, rather than a borrower's hazard rate, particularly with loans that feature negative amortization.

To address these issues, Appendix Table A.IV considers the impact of the original LTV and current  $E_{ijt}$  on cumulative default outcomes in the full sample. This approach avoids sample selection issues, but requires a slight reinterpretation of the treatment. The moral hazard effect no longer captures a response to

the realized balance but rather the borrower's response to the anticipated balance trajectory. Furthermore, because  $E_{ijt}$  is not observed directly for those defaulting prior to t, we use the imputed version of the  $E_{ijt}$ , based on original contract terms and realized interest rates.

I first estimate specifications meant to mimic those in Table III, this time utilizing the outcome of cumulative default by 36 months. These are shown on the left-hand side of Appendix Table A.IV. We include imputed  $E_{ijt}$  measured at 36 months. For these estimates the baseline relationship between the original LTV and default is higher than in Table III. However, the portion owing to adverse selection—approximately 17 percent when  $E_{ijt}$  is defined as current negative equity, and 29 percent when defined as current LTV—is somewhat lower. Regardless, there is strong evidence that both moral hazard and adverse selection are present.

As a more robust test of the adverse selection effect, the right-hand side of Appendix Table A.IV considers the outcome of default by 60 months. For these regressions, we include a comprehensive set of controls for  $E_{ijt}$ , not just at a given point in time, but across the life of the loan. These controls are meant to account for the full impact of the non-linear loan trajectory throughout the first 60 months. Even controlling for the full trajectory of  $E_{ijt}$ , the initial leverage choice is strongly predictive of default. In these specifications, adverse selection remains responsible for approximately 30 percent of the baseline relationship between original LTV and default.

#### **Alternate Functional Forms**

A potential concern is that the observed effect of original LTV on default when controlling for  $E_{ijt}$  does not truly reflect selection, but rather some more complicated functional form relating  $E_{ijt}$  to default that is not captured by a linear specification. Appendix Table A.V examines whether there is still evidence of adverse selection across three more complex specifications: (i) including a cubic specification in current  $E_{ijt}$ , (ii) controlling for current and past minimum payments and interest rates, and (iii) interacting  $E_{ijt}$  with covariates.<sup>49</sup> The estimated adverse selection effect is persistent across all specifications.

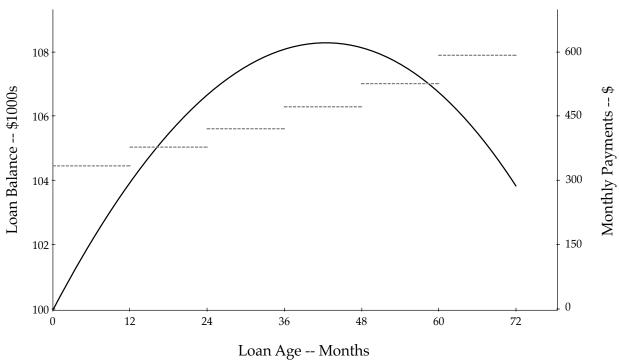
### **Further Robustness**

Appendix Tables A.VI and A.VII explore further robustness. The results are robust to (i) probit and control function specifications, which are potentially more realistic than the linear probability model, (ii) the use of the simulated instrument rather than the full set of fixed effects, and (iii) alternative definitions of default, ranging from mild (30 days past due) to extreme (foreclosure).

 $<sup>^{49}</sup>$ In column 5 of Appendix Table A.V, the OLS specification, we fully interact  $E_{ijt}$  with all covariates. However, because we do not have sufficient instruments to do so in an IV specification, in column 6 we simply interact  $E_{ijt}$  with two covariates: the borrower's credit score and whether the loan was to purchase a home or refinance an existing mortgage.

# C Appendix Tables and Figures

FIGURE A.I STYLIZED MONTHLY PAYMENT AND BALANCE TRAJECTORY FOR OPTION ARM

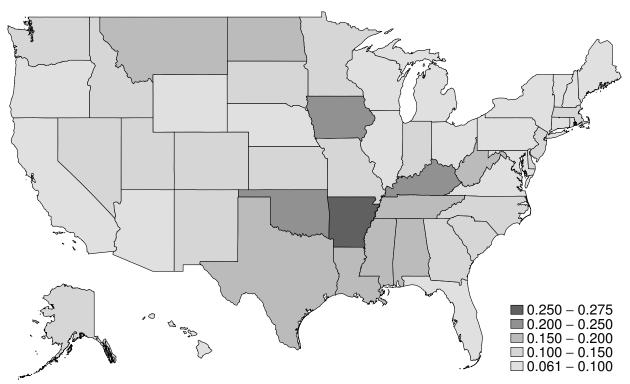


The solid line shows the balance trajectory for a stylized Option ARM with an initial loan of \$100,000. The balance is initially increasing, demonstrating negative amortization. Monthly payments, shown by the dashed lines, increase by 7.5% per year regardless of balance. As payments grow, the balance begins to decrease, as shown by the parabolic shape of the balance trajectory. At 5 years the monthly payment jumps to the fully amortizing amount.

FIGURE A.II
STYLIZED EXAMPLE OF IMPACT OF INTEREST RATE VARIATION ON OPTION ARM BALANCE

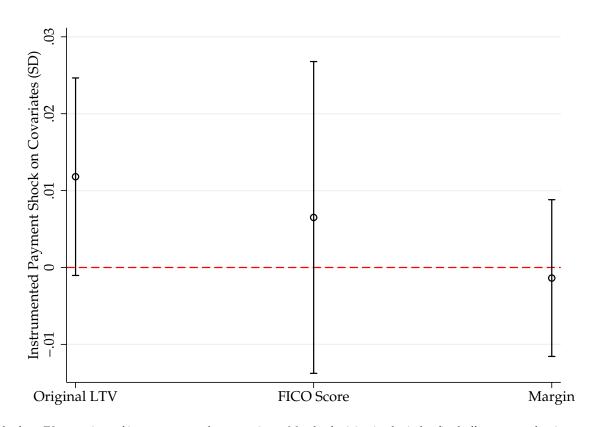
#### Origination 24 Months Borrower A: Borrower A: Loan: \$100,000 High Realization of Index Balance: \$107,000 Margin: 3.5% Payment: \$376 Index: LIBOR Initial Payment: \$325 Borrower B: Borrower B: Low Realization of Index Loan: \$100,000 Balance: \$104,000 Margin: 3.5% Payment: \$376 Index: Treasury Initial Payment: \$325

FIGURE A.III
UNIFORM DENSITY OF LIBOR INDEXED OPTION ARMS ACROSS STATES



Plot shows number of LIBOR indexed Option ARMs as a proportion of all LIBOR- or Treasury-indexed Option ARMs. The minimum is 6.1 percent, while the max is 27.5 percent. In the majority of states, between 5 and 15 percent of Option ARMs are indexed to LIBOR.

FIGURE A.IV EXOGENEITY OF INSTRUMENT FOR 5/1 ARMS



Results from IV regressions of interest rates on loan covariates. Month of origination-by-index fixed effects are used to instrument for loan-level interest rates after initial reset of 5/1 ARMs. The standard set of covariates are included, but in each specification one coefficient is left out. The first line illustrates the effect of a one percent increase in instrumented interest rates on the standard deviation of original LTV; the second shows the instrumented effect on a standard deviation of origination FICO score; the third show the predicted instrumented effect on the standard deviation of initial margin.

TABLE A.I FRACTION OF LIBOR-INDEXED LOANS BY LENDER

Originator	Percent of Loans Indexed to LIBOR
American Home Mortgage	< 1%
Bank United	< 1%
Bank of America	85%
Countrywide	3%
Downey	0%
EMC	0%
Greenpoint	91%
IndyMac	< 1%
MortgageIT	5%
Residential Funding	9%
Servicer	Percent of Loans Indexed to LIBOR
American Home Mortgage	< 1%
Bank of America	10%
Control Montaga	
Central Mortgage	1%
Countrywide	1% 15%
0 0	-,-
Countrywide	15%
Countrywide EMC	15% 7%
Countrywide EMC IndyMac	15% 7% < 1%
Countrywide EMC IndyMac JP Morgan Chase	15% 7% < 1% 2%

Table displays percent of LIBOR-indexed loans for the top 10 originators and servicer in the sample. Servicer is available for 99 percent of loans, while originator is only available for 27 percent of loans.

TABLE A.II
HETEROGENEITY IN THE IMPACT OF ORIGINAL AND CURRENT LEVERAGE
ON 1 YEAR DEFAULT PROBABILITY (OPTION ARM)

					e Recourse St	
		full Recourse		Lir	nited Recours	se
Original Loan-to-Value	0.546*** (0.044)	0.530*** (0.116)	0.494*** (0.179)	0.741*** (0.025)	0.276*** (0.045)	0.239*** (0.057)
Current Negative Equity in \$100,000s		0.003 $(0.034)$			0.089*** (0.009)	
Current Loan-to-Value			0.044 $(0.189)$			0.421** (0.044)
Mean of Dep. Var N	0.198 28565	0.198 28565	0.198 28565	0.272 236569	0.272 236569	0.272 236569
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	Yes	Yes	Yes	Yes	Yes	Yes
Full Controls	Yes	Yes	Yes	Yes	Yes	Yes
	Panel B	3: IV Regressi	ons at 24 Moi	nths by Origi	nal Documen	tation
	No/Lo	ow Document	tation	Full	Documentati	on
Original Loan-to-Value	0.766*** (0.026)	0.355*** (0.056)	0.336*** (0.058)	0.492*** (0.031)	-0.017 (0.067)	-0.095* (0.057)
Current Negative Equity in \$100,000s		0.077*** (0.010)			0.113*** (0.015)	
Current Loan-to-Value			0.356*** (0.045)			0.538*** (0.052)
Mean of Dep. Var N	0.286 215366	0.286 215366	0.286 215366	0.166 49768	0.166 49768	0.166 49768
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	Yes	Yes	Yes	Yes	Yes	Yes
Full Controls	Yes	Yes	Yes	Yes	Yes	Yes
	Pa	anel C: IV Re	gressions at 2	4 Months by	Loan Purpose	9
		Purchase			Refinance	
Original Loan-to-Value	0.587*** (0.033)	0.119** (0.056)	0.076 (0.050)	0.762*** (0.026)	0.313*** (0.050)	0.277** (0.059)
Current Negative Equity in \$100,000s		0.101*** (0.013)			0.084*** (0.009)	
Current Loan-to-Value			0.452*** (0.042)			0.405** (0.048)
Mean of Dep. Var N	0.252 93226	0.252 93226	0.252 93226	0.270 171908	0.270 171908	0.270 171908
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	Yes	Yes	Yes	Yes	Yes	Yes
Full Controls	Yes	Yes	Yes	Yes	Yes	Yes

OLS and IV regressions of default between 24 and 36 months on borrowers original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,000s (or current loan-to-value). Baseline refers to OLS regressions omitting current equity, all other specifications are IV regressions including the full set interactions between index and origination month as instruments for current equity. States are categorized as full recourse if they are considered to have strong provisions regarding deficiency judgments in Rao and Walsh (2009). Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers' FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE A.III
IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON
1 YEAR DEFAULT PROBABILITY AT 48 MONTHS

	Panel A:	OLS and IV l	Regressions I	ncluding Curre	ent Negative 1	Equity
	Baseline	OLS	IV	Baseline	OLS	IV
Original Loan-to-Value	0.283***	-0.005	-0.136	0.452***	0.187***	0.231***
	(0.038)	(0.025)	(0.219)	(0.028)	(0.021)	(0.074)
Current Negative Equity in \$100,000s		0.073*** (0.004)	0.106** (0.053)		0.054*** (0.002)	0.045*** (0.015)
Mean of Dep. Var	0.213	0.213	0.213	0.213	0.213	0.213
N	107917	107917	107917	107917	107917	107917
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	No	No	No	Yes	Yes	Yes
Full Controls	No	No	No	Yes	Yes	Yes
	Panel B	: OLS and IV	Regressions	Including Curr	ent Loan-to-V	Value
	Baseline	OLS	IV	Baseline	OLS	IV
Original Loan-to-Value	0.283***	0.027	-0.067	0.452***	0.165***	0.371***
	(0.038)	(0.028)	(0.160)	(0.028)	(0.026)	(0.068)
Current Loan-to-Value		0.195*** (0.008)	0.266** (0.122)		0.180*** (0.010)	$0.050 \\ (0.038)$
Mean of Dep. Var	0.213	0.213	0.213	0.213	0.213	0.213
N	107917	107917	107917	107917	107917	107917
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs	No	No	No	Yes	Yes	Yes
Full Controls	No	No	No	Yes	Yes	Yes

OLS and IV regressions of default between 48 and 60 months on borrowers' original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,000s (Panel A), or current loan-to-value (Panel B). Default is defined as 60 or more days past due. Baseline refers to OLS regressions omitting current equity. IV regressions include the full set of interactions between index and origination month as instruments for current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE A.IV IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON CUMULATIVE DEFAULT PROBABILITIES

		Par	nel A: Curren	t Negative Eq	uity		
		36 Months		60 Months:	Controlling fo	r Trajectory	
	Baseline	OLS	IV	Baseline	OLS	IV	
Original Loan-to-Value	0.857*** (0.030)	0.712*** (0.034)	0.148** (0.064)	1.041*** (0.037)	0.892*** (0.032)	0.338** (0.127)	
Imputed Negative Equity at 36 Months in \$100,000s		0.026*** (0.004)	0.128*** (0.016)		$0.004 \\ (0.005)$	$-0.157^* \ (0.081)$	
Imputed Negative Equity at 24 Months in \$100,000s					$-0.006^* \ (0.004)$	0.174** (0.050)	
Imputed Negative Equity at 48 Months in \$100,000s					0.012 (0.008)	0.174** (0.089)	
Imputed Negative Equity at 60 Months in \$100,000s					0.016** (0.007)	-0.060 $(0.054)$	
Mean of Dep. Var N	0.310 443600	0.310 443600	0.310 443600	0.454 443600	0.454 443600	0.454 443600	
Origination Month FEs Index FEs MSA FEs Full Controls	Yes Yes No No	Yes Yes No No	Yes Yes No No	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	
	Panel B: Current Loan-to-Value						
		36 Months		60 Months:	Controlling fo	r Trajectory	
	Baseline	OLS	IV	Baseline	OLS	IV	
Original Loan-to-Value	0.857*** (0.030)	0.509*** (0.037)	0.255*** (0.066)	1.041*** (0.037)	0.583*** (0.049)	0.299** (0.124)	
Imputed Loan-to-Value at 36 Months		0.231*** (0.016)	0.402*** (0.043)		0.006 (0.022)	-0.341 (0.228)	
Imputed Loan-to-Value at 24 Months					0.217*** (0.048)	0.806** (0.187)	
Imputed Loan-to-Value at 48 Months					0.088*** (0.032)	-0.109 $(0.356)$	
Imputed Loan-to-Value at 60 Months					0.019 (0.024)	0.263 (0.292)	
Mean of Dep. Var N	0.310 443600	0.310 443600	0.310 443600	0.454 443600	0.454 443600	0.454 443600	
Origination Month FEs Index FEs MSA FEs	Yes Yes No	Yes Yes No	Yes Yes No	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes	

The left columns show OLS and IV regressions of default by 36 months on borrowers' original loan-to-value and imputed current equity at 36 months, defined as either the level of negative equity in \$100,000s (Panel A) or current loan-to-value (Panel B) at 36 months. Right columns show OLS and IV regressions of default by 60 months on borrowers' original loan-to-value and imputed current equity at 24 months, 36 months, 48 months and 60 months, defined as either the level of negative equity in \$100,000s (Panel A) or current loan-to-value (Panel B). Default is defined as 60 or more days past due. Baseline refers to OLS regressions omitting current equity. IV regressions include the full set of interactions between index and origination month as instruments for current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\*\* denotes 5% significance, \*\*\* denotes 5% significance, \*\*\* denotes 5% significance.

No

No

Yes

Yes

No

Full Controls

TABLE A.V
IMPACT OF ORIGINAL LEVERAGE WITH FLEXIBLE CONTROLS FOR
CURRENT LEVERAGE AND TIME-VARYING COVARIATES

			Panel A: Cur	rent Negative Equi	ity	
	Cubic in N	eg. Equity	Current Rate	s and Payments	Neg. Equity	× Covariate
	OLS	IV	OLS	IV	OLS	IV
Original Loan-to-Value	0.332*** (0.041)	0.296*** (0.053)	0.339*** (0.035)	0.204*** (0.050)	0.372*** (0.040)	0.309*** (0.055)
Current Negative Equity in \$100,000s	0.107*** (0.008)	0.146*** (0.015)	0.061*** (0.005)	0.089*** (0.010)	0.413** (0.171)	-0.082 $(0.064)$
Current Negative Equity <sup>2</sup>	0.016*** (0.002)	-0.016 $(0.019)$				
Current Negative Equity <sup>3</sup>	0.001*** (0.000)	$-0.010^{***} (0.003)$				
Minimum Payment in \$			0.000*** (0.000)	0.000*** (0.000)		
Interest Rate			0.047*** (0.003)	0.047*** (0.003)		
Current Negative Equity × Fico Score						-0.000 $(0.000)$
Current Negative Equity × Purchase						0.086*** (0.028)
Mean of Dep. Var N	0.264 265134	0.264 265134	0.275 240189	0.275 240189	0.264 265134	0.264 265134
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
Index FEs	Yes	Yes	Yes	Yes	Yes	Yes
MSA FEs Full Controls	No No	No No	No No	Yes Yes	Yes Yes	Yes Yes
Full Controls	110	140		rrent Loan-to-Valu		105
	Cubic i			s and Payments		Covariates
	OLS	IV	OLS	IV	OLS	IV
Original Loan-to-Value	0.168*** (0.055)	0.175*** (0.060)	0.157*** (0.054)	0.127** (0.058)	0.241*** (0.054)	0.229*** (0.070)
Current Loan-to-Value	$-0.542^{***} $ $(0.144)$	0.556*** (0.067)	0.389*** (0.038)	0.414*** (0.043)	-0.033 $(0.751)$	0.308*** (0.049)
Current Loan-to-Value <sup>2</sup>	1.128*** (0.176)	0.000 (1.866)				
Current Loan-to-Value <sup>3</sup>	$-0.391^{***} (0.059)$	-0.038 (0.170)				
Minimum Payment in \$			0.000*** (0.000)	0.000*** (0.000)		
Interest Rate			0.043*** (0.003)	0.043*** (0.003)		
Current Loan-to-Value × Fico Score						$0.000 \\ (0.001)$
Current Loan-to-Value × Purchase						0.001 (0.189)
Mean of Dep. Var	0.264 265134	0.264 265134	0.275 240189	0.275 240189	0.264 265134	0.264 265134
N					2.4	3.4
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes
N Origination Month FEs Index FEs MSA FEs	Yes Yes No	Yes Yes No	Yes Yes No	Yes Yes Yes	Yes Yes Yes	Yes Yes Yes

OLS and IV regressions of default between 24 and 36 months on borrowers' original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,000s (Panel A), or current loan-to-value (Panel B). The first two columns include a cubic in current equity. The third and fourth columns include current and original minimum payments, as well as the current interest rate. The 5th column interacts current equity with all control variables in an OLS specification. The final column includes current equity interacted with each borrowers FICO score and an indicator equal to one if the loan was used to purchase a home. Default is defined as 60 or more days past due. IV regressions include the full set of interactions between index and origination month as instruments for all terms including current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE A.VI
IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON 1 YEAR DEFAULT PROBABILITY:
PROBIT ESTIMATES AND ALTERNATIVE INSTRUMENTS

		Par	nel A: Probit and Contr	ol Function	
	Baseline	Probit	Control Function	Probit	Control Function
Original Loan-to-Value	3.282*** (0.100)	2.028*** (0.134)	0.556** (0.260)	1.602*** (0.169)	1.047*** (0.296)
Current Negative Equity in \$100,000s		0.251*** (0.020)	0.529*** (0.051)		
Current Loan-to-Value				1.347*** (0.111)	1.808*** (0.216)
Mean of Dep. Var N	0.264 265128	0.264 265128	0.264 265128	0.264 265128	0.264 265128
Origination Month FEs Index FEs State FEs Full Controls	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes
		Panel B: OLS	and IV Incorporating	Simulated Inst	rument
	Baseline	OLS	IV	OLS	IV
Original Loan-to-Value	0.721*** (0.026)	-0.641* (0.339)	0.256*** (0.047)	-0.541 (0.348)	0.229*** (0.050)
Current Negative Equity in \$100,000s		0.216*** (0.060)	0.090*** (0.010)		
Current Loan-to-Value				1.002*** (0.314)	0.415*** (0.041)
Mean of Dep. Var N	0.264 265134	0.264 265134	0.264 265134	0.264 265134	0.264 265134
Origination Month FEs Index FEs State FEs Full Controls	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes	Yes Yes Yes Yes

Top panel shows probit and control function specifications of default between 24 and 36 months on borrowers' original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,000s or current loan-to-value. Default is defined as 60 or more days past due. Baseline refers to probit regressions omitting current equity. Control Function regressions include the full set of interactions between index and origination month as instruments for current equity, and are estimated following Blundell and Powell (2004). The bottom panel includes OLS regressions as in Table III, but uses the simulated instrument. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. Standard errors are clustered at the MSA level. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 1% significance.

TABLE A.VII IMPACT OF ORIGINAL AND CURRENT LEVERAGE ON ONE YEAR DELINQUENCY, DEFAULT, AND FORECLOSURE RATES

		30 Days Past Due	Due		90 Days Past Due	Due		Foreclosure	.e
	Baseline	Equity	Loan-to-Value	Baseline	Equity	Loan-to-Value	Baseline	Equity	Loan-to-Value
Original Loan-to-Value	0.688***	0.379***	0.211*** (0.049)	0.710*** (0.026)	0.407***	0.256*** (0.051)	0.494***	0.315*** (0.029)	0.213*** (0.038)
Current Negative Equity in \$100,000s		$0.060^{***}$ $(0.005)$			0.059*** (0.005)			0.035*** (0.004)	
Current Loan-to-Value			$0.404^{***}$ (0.034)			$0.381^{***}$ $(0.035)$			0.234*** (0.022)
Mean of Dep. Var N	0.304 213535	0.304 213535	0.304 213535	0.248 278761	0.248 278761	0.248 278761	0.177 294636	0.177 294636	0.177 294636
Origination Month FEs	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes
INGEX FES MSA FES	Yes	Yes	Yes	Xes	Yes	Yes	Yes	Xes Xes	Yes
Full Controls	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes	Yes

OLS and IV regressions of default between 24 and 36 months on borrowers' original loan-to-value and current equity at 24 months, defined as either the level of negative equity in \$100,0006 (Panel A), or current loan-to-value (Panel B). Default is defined as 30/90 or more days past due or as foreclosure. Baseline refers to OLS regressions omitting current equity. IV regressions include the full set of interactions between index and origination month as instruments for current equity. Full controls refers to fixed effects for index type, documentation, the loans purpose and occupancy, the existence of prepayment penalties and private mortgage insurance, and single family homes. We also include indicators for each 20-point bin of borrowers FICO credit scores, loan originator and servicer fixed effects, and controls for second liens. We allow individual state time trends. \* denotes 10% significance, \*\* denotes 5% significance, \*\*\* denotes 18% significance, \*\* den