

Colouring graphs with no odd holes

Date Tuesday, September 16

Time 3 pm

Location 303 Mudd

Abstract:

The chromatic number $k(G)$ of a graph G is always at least the size of its largest clique (denoted by $w(G)$), and there are graphs with $w(G)=2$ and $k(G)$ arbitrarily large.

On the other hand, the perfect graph theorem asserts that if neither G nor its complement has an odd hole, then $k(G)=w(G)$. (An “odd hole” is an induced cycle of odd length at least five.) What happens in between? With Alex Scott, we have just proved the following, a 1985 conjecture of Gyarfás:

For graphs G with no odd hole, $k(G)$ is bounded by a function of $w(G)$.