

# Large cliques or stable sets in graphs with no $P_4$ and no $P_5^c$

*Date* Tuesday, April 21

*Time* 5:30 pm

*Location* 507 Math

*Abstract:* Erdos and Hajnal conjectured that, for any graph  $H$ , every graph on  $n$  vertices that does not have  $H$  as an induced subgraph contains a clique or a stable set of size  $n^{e(H)}$  for some  $e(H) > 0$ . The conjecture is known to be true for graphs  $H$  on at most four vertices. One of the two remaining open cases on five vertices is the case where  $H$  is a four-edge path, the other case being a cycle of length five. In this paper we prove that every graph on  $n$  vertices that does not contain a four-edge-path or the complement of a five-edge-path as an induced subgraph contains either a clique or a stable set of size at least  $n^{1/8}$ . This is joint work with Maria Chudnovsky.