# Bounded Rationality I: Consideration Sets 

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## Choice Problem 1



## Choice Problem 2



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Head Hunter

## Consideration Sets

- Choice Problem 1 and 2 are difficult
- Lots of available alternatives
- Understanding each available alternative takes time and effort
- Do people really think hard about each available alternative?
- The marketing literature thinks not
- Since the 1960s have made use of the concept of consideration (or evoked) set
- A subset of the available options from which the consumer makes their choice
- Alternatives outside the consideration set are ignored
- Some key references
- Hauser and Wernerfelt [1990]
- Roberts and Lattin [1991]


## Consideration Sets

- What was the evidence that convinced marketers that consideration sets played an important role in choice?
- Intuitive plausibility
- Verbal reports (e.g. Brown and Wildt 1992)
- Lurking around supermarkets and seeing what people look at (e.g. Hoyer 1984)
- More recently richer data has been used
- Eye tracking
- Internet search data


## De los Santos et al [2012]

- Use data from internet search engines on book purchases
- Makes visible what was searched not just what was chosen
- Dataset: 152,000 users from ComScore
- Company that records web browsing activity (!)
- Date
- Time
- Duration
- Purchase description, price and quantity
- Divide the internet into four 'bookshops'
- Amazon
- Barnes and Noble
- Book Clubs
- All other
- Looks at the search histories of people who bought books in the seven days prior to purchase


## De los Santos et al [2012]

Table 2-Descruptive Statistics of ComScone Book Sample

|  | 2002 |  | 2004 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Mean | Std. Dev. | Mean | Std. Dev. |
| Duration of each website visit (in minutes) |  |  |  |  |
| Visits not within 7 days of transaction | 8.89 | 13.03 | 7.69 | 12.36 |
| Visits within 7 days, excluding transactions | 12.72 | 15.83 | 11.02 | 15.00 |
| Visits within 7 days, including transactions | 19.04 | 18.26 | 15.74 | 17.37 |
| Transactions only | 28.06 | 17.69 | 26.08 | 17.71 |
| Total duration, excluding transaction visits | 32.47 | 49.80 | 38.41 | 78.33 |
| Total duration, including transaction visits | 43.88 | 43.27 | 47.43 | 66.11 |
| Number of stores searched | 1.27 | 0.54 | 1.30 | 0.56 |
| Number or Dooks per transuction | -100 | 2.10 | 2.20 | 1.95 |
| Transaction expenditures (books only) | 36.67 | 40.64 | 32.21 | 35.68 |
| Number of books purchased | 17,956 |  | 17,631 |  |
| Number of transaction sessions | 7,559 |  | 8,002 |  |
| Number of visits within 7 days | 18,350 |  | 25,556 |  |
| Number of visits not within 7 days | 94,011 |  | 189,157 |  |

- On average people don't go to all bookshops
- Also do not buy from the lowest priced store in $37 \%$ of observations


## A (Naive) Model of Choice with Consideration Sets

- So people don't think about all alternatives before making a choice
- What happens if we bake this into our standard model of choice?


## A (Naive) Model of Choice with Consideration Sets

- Let
- $u: X \rightarrow \mathbb{R}$ be a utility function
- $E: \mathcal{X} \rightarrow \mathcal{X}$ describe the evoked set
- $E(A) \subseteq A$ is the set of considered alternatives from choice problem $A$
- Choice is given by

$$
C(A)=\arg \max _{x \in E(A)} u(x)
$$

- What are the testable implications of this model?
- Nothing!
- Any data set can be rationalized by assuming utility is constant and setting $E(A)=C(A)$ for all $A$


## A Testable Model of Choice with Consideration Sets

- In order to be able to test the consideration set model we need to do (at least) one of two things
- Put more structure on the way consideration sets are formed
- Enrich the data we use to test the model
- First, let's look at at some approaches that have taken the former route


## Masatlioglou et. al. [2012]

- Model choice with consideration sets using standard choice data
- Add an additional assumption to make consideration set model testable

$$
E(S / x)=E(S) \text { if } x \notin E(S)
$$

- Removing an item that is not in the consideration set does not affect the consideration set
- This property is satisfied by several intuitively plausible procedures for constructing consideration sets
- The top $N$ according to some criterion
- Top on each criterion
- Most popular category
- But not all
- Salience?
- Masatlioglou at al. call the resulting model Choice with Limited Attention


## Masatlioglou et. al. [2012]

- This assumption also gives the consideration set model empirical bite
- For simplicity, work in a world of choice functions/no indifference
- Question: What observation 'reveals preference' in this model?
- Not $x \in C(A) y \in A / C(A):$ Maybe $y$ not in the consideration set
- How do we know that an alternative $y$ is in the consideration set?
- Obviously if it is chosen
- But for revealed preference we need to know if it was considered and not chosen
- Say $x \in C(A), y \in A / C(A)$ and $x \notin C(A / y)$
- As WARP is violated, $E$ must have changed
- So y must have been in $E(A)$


## Masatlioglou et. al. [2012]

$$
x \in C(A), y \in A / C(A) \text { and } x \notin C(A / y)
$$

- Same observation implies that $x$ is revealed preferred to $y$
- $x$ was chosen, and we know that $y$ was considered
- We write $x P y$
- Of course, if we saw $x P y$ and $y P z$ we would want to conclude that $x$ is preferred to $z$
- Let $P_{R}$ be the transitive closure of $P$
- Turns out that $P_{R}$ is the only revealed preference information on can extract from the data in the following sense
- Say $C$ is consistent with the model, but not $x P_{R} y$
- Then there exists a representation of the data in which $u(y)>u(x)$


## Masatlioglou et. al. [2012]

- A necessary condition for a choice function to have a CLA representation is that $P$ is acyclic
- Means that there exists a utility function that represents $P$
- Turns out that this is also a sufficient condition
- Construct a utility function that agrees with $P$
- Construct the 'minimal' consideration sets that are consistent with the model
- This is a trick that we will see again!


## Masatlioglou et. al. [2012]

- Turns out that the acyclicality of $P$ is equivalent to a weakening of WARP


## Definition

WARP: For every $A$ there exists an $x^{*}$ such that, for any $B$ including $x^{*}$, if $C(B) \in A$, then $C(B)=x^{*}$

## Definition

WARP with limited attention: For every $A$ there exists an $x^{*}$ such that, for any $B$ including $x^{*}$

$$
\text { if } C(B) \in A \text { and } C(B) \neq C\left(B \backslash x^{*}\right) \text { then } C(B)=x^{*}
$$

## Masatlioglou et. al. [2012]

## Lemma

$C$ satisfies WARP with limited inattention if and only if $P$ is acyclic
Theorem
C satisfies WARP with limited attention if and only if it has a CLA representation

## Masatlioglou et. al. [2012]

- So, do we like this paper?
- Yes?
- It derives a model of consideration sets that has testable implications
- Does so using 'natural' restrictions on the way in which consideration sets work
- But
- Testable implications may be very weak
- Note that if there are no violations of WARP we have no revealed preference information
- Similar techniques can be used for different assumptions about the way consideration sets work
- e.g. Lleras, J. S., Masatlioglu, Y., Nakajima, D., \& Ozbay, E. Y. (2017). When more is less: Limited consideration. Journal of Economic Theory, 170, 70-85.


## Stochastic Consideration Sets

- One problem with this approach is that it is deterministic
- Same consideration set and same choice made each time a decision problem is faced
- This
- May be intuitively implausible
- Limits applications
- Recent papers have extended the model to random consideration sets
- Typically
- Preferences are fixed
- Consideration sets are random
- These can be used as an alternative to random utility models


## Manzini and Mariotti [2014]

- Let $X$ be a finite set of alternatives
- Model choice with consideration sets using stochastic choice data
- $p(a, A)$ : probability of alternative a chosen from set $A$
- Assume that every alternative has a fixed, strictly positive probability that it will be included in the consideration set
- Is this a realistic assumption?
- There is a default alternative which is always considered
- As usual, chosen item is the highest utility alternative in the consideration set.


## Manzini and Mariotti [2014]

- We say that $p$ has a random consideration set representation if there exist a strict preference order $\succ$ and a probability $\gamma: X \rightarrow[0,1]$ such that

$$
p(a, A)=\gamma(a) \prod_{b \in A \mid b \succ a}(1-\gamma(b))
$$

- Probability that $a$ is chosen from $A$ is the probability that
- $a$ is considered
- Nothing better than $a$ is considered
- As the probability of any item being considered is independent, has a nice easy form


## Manzini and Mariotti [2014]

- Allows preferences to be identified

$$
\frac{p(a, A / b)}{p(a, A)}>1 \Leftrightarrow b \succ a
$$

- Provides testable predictions: I-Asymmetry

$$
\frac{p(a, A / b)}{p(a, A)}>1 \Rightarrow \frac{p(b, B / a)}{p(b, B)}=1
$$

- Also I-independence

$$
\frac{p(a, A / b)}{p(a, A)}=\frac{p(a, B / b)}{p(a, B)}
$$

- These two are necessary and sufficient for a random consideration set representation


## Manzini and Mariotti [2014]

- Do we like this paper?
- Yes?
- Nice clean axiomatization (certainly relative to RUM)
- Idea that consideration is random seems intuitively plausible
- No?
- Assumption that probability of consideration is set independent is weird
- Relaxed in Brady, Richard L., and John Rehbeck. "Menu-dependent stochastic feasibility." Econometrica 84.3 (2016): 1203-1223.


## Catteneo et al [2020]

- More recently "A Random Attention Model" takes an even more flexible approach
- Let $X$ be a finite set and $\mathcal{X}$ be the set of all non-empty subsets of $X$
- An Attention Rule is a function $\mu: \mathcal{X} \times \mathcal{X} \rightarrow[0,1]$ where $\mu(B \mid A)$ is the probability of using consideration set $B$ from decision problem $A$
- Apply the relevant conditions to $\mu$ for this to make sense
- A random consideration set model consists of a $\mu$ and a linear order $\succ$ on $X$ such that

$$
p(a, A)=\sum_{B \subseteq A} 1(a \text { is } \succ \text {-maximal in } B) \mu(B \mid A)
$$

## Catteneo et al [2020]

- Without further restrictions, this model is vacuous
- Catteneo et al assume Monotonic Attention
- Adding options cannot make any given consideration set more likely

$$
\text { For any } a \in A-B, \mu(B \mid A) \leq \mu(B \mid A / a)
$$

- This is a stochastic vers
- Note that this can allow for violations of monotonicity in choice
- MM does not


## Catteneo et al [2020]

- Revealed preference?
- If $p(a, A)>p(a, A / b)$ then $a$ is revealed preferred to $b$
- Why?
- Let $\mathcal{A} \subset \mathcal{X}$ be the subsets of $A / b$ in which $a$ is maximal
- We know $\mu(\mathcal{A} \mid A) \leq \mu(\mathcal{A} \mid A / b)$
- So if the probability of choosing $a$ is higher in $A$ than is $A \backslash b$ it must be that $a$ is maximal in some other subsets of $A$
- These contain $b$, so $a$ must be preferred to $b$
- Revealed preference from violations of monotonicity
- Similar to choice with limited attention
- Data has a representation of this type if and only if revealed preference relation is acyclic


## Abaluck and Adams-Prassi [2021]

- There is also a significant literature on this in consumer choice/IO
- Recent example is Abaluck and Adams-Prassi [2021]
- Also surveys previous literature
- They work with a different data set:
- Demand functions
- Consideration sets can lead to violations of Slutsky Symmetry
- Absent income effects the following should be equal
- The impact of a price change in good $j$ on demand for good $i$
- The impact of a price change of good $i$ on demand for good $j$


## Abaluck and Adams-Prassi [2021]

- Simple example:
- Two products, 0 and 1
- $x_{j}$ price of good $j$
- 0 is default - always observed
- 1 is alternative - whether it is looked at depends on the price of 0
- $\mu\left(x_{0}\right)$ probability that good 1 will be looked at given $x_{0}$


## Abaluck and Adams-Prassi [2021]

- $s_{i}^{*}\left(x_{0}, x_{1}\right)$ probability of buying good $i$ given prices if both are observed
- Derived from maximizing a quasilinear utility function
- Probabilistic due to some random utility component
- $s_{i}\left(x_{0}, x_{1}\right)$ probability that good $i$ is chosen:

$$
\begin{aligned}
& s_{0}\left(x_{0}, x_{1}\right)=\left(1-\mu\left(x_{0}\right)\right)+\mu\left(x_{0}\right) s_{0}^{*}\left(x_{0}, x_{1}\right) \\
& s_{1}\left(x_{0}, x_{1}\right)=\mu\left(x_{0}\right) s_{1}^{*}\left(x_{0}, x_{1}\right)
\end{aligned}
$$

- Claim: with quasi-linear utility and no outside option

$$
\frac{\partial s_{0}^{*}\left(x_{0}, x_{1}\right)}{\partial x_{1}}=\frac{\partial s_{1}^{*}\left(x_{0}, x_{1}\right)}{\partial x_{0}}
$$

## Abaluck and Adams-Prassi [2021]

- What if consideration is imperfect?

$$
\begin{aligned}
& \frac{\partial s_{0}\left(x_{0}, x_{1}\right)}{\partial x_{1}}=\mu\left(x_{0}\right) \frac{\partial s_{0}^{*}\left(x_{0}, x_{1}\right)}{\partial x_{1}} \\
& \frac{\partial s_{1}\left(x_{0}, x_{1}\right)}{\partial x_{0}}=\frac{\partial \mu\left(x_{0}\right)}{\partial x_{0}} s_{1}^{*}\left(x_{0}, x_{1}\right)+\mu\left(x_{0}\right) \frac{\partial s_{1}^{*}\left(x_{0}, x_{1}\right)}{\partial x_{0}}
\end{aligned}
$$

implying

$$
\begin{aligned}
\frac{\partial s_{1}\left(x_{0}, x_{1}\right)}{\partial x_{0}}-\frac{\partial s_{0}\left(x_{0}, x_{1}\right)}{\partial x_{1}} & =\frac{\partial \mu\left(x_{0}\right)}{\partial x_{0}} s_{1}^{*}=\frac{\partial \ln \mu\left(x_{0}\right)}{\partial x_{0}} s_{1} \\
\frac{\partial \ln \mu\left(x_{0}\right)}{\partial x_{0}} & =\frac{1}{s_{1}}\left[\frac{\partial s_{1}\left(x_{0}, x_{1}\right)}{\partial x_{0}}-\frac{\partial s_{0}\left(x_{0}, x_{1}\right)}{\partial x_{1}}\right]
\end{aligned}
$$

- Attention changes with prices if and only if Slutsky symmetry is violated
- Level of attention can be identified by integrating this expression


## Other Examples

- For another recent example on literature in this vein see Barseghyan et al [2021]
- Shows that you can get some identification of the distribution of preferences in a RUM with consideration sets
- If you observe the distribution of choices from a single set
- Know that individual choices came from a distribution of consideration sets with some minimum size
- Then you can still set identify some parameters
- For example say that there are 3 possible alternatives, and that $|E|>2$
- Probabiity that the worst alternative is chosen is zero
- So if an alternative $x$ is chose with positive probability, we can rule out parameters which say it is the worst option
- See also Dardanoni et al. [2020]


## Introduction

- So far we have talked about strategies for identifying whether people are using consideration sets
- And some of the properties they might have
- But not where they come from, or why
- i.e. we have not discussed procedures that might lead to the generation of consideration sets


## Satisficing as Optimal Stopping

- Satisficing model (Simon 1955) was an early model of consideration set formation
- Very simple model:
- Decision maker faced with a set of alternatives $A$
- Searches through this set one by one
- If they find alternative that is better than some threshold, stop search and choose that alternative
- If all objects are searched, choose best alternative
- Proved extremely influential in economics, psychology and ecology


## Satisficing as Optimal Stopping

- Usually presented as a compelling description of a 'choice procedure'
- Can also be derived as optimal behavior as a simple sequential search model with search costs
- Primitives
- A set $A$ containing $M$ items from a set $X$
- A utility function $u: X \rightarrow \mathbb{R}$
- A probability distribution $f$ : decision maker's beliefs about the value of each option
- A per object search cost $k$


## The Stopping Problem

- At any point DM has two options
(1) Stop searching, and choose the best alternative so far seen (search with recall)
(2) Search another item and pay the cost $k$
- Familiar problem from labor economics


## Optimal Stopping

- Can solve for the optimal strategy by backwards induction
- Choice when there is 1 more object to search and current best alternative has utility $\bar{u}$
(1) Stop searching: $\bar{u}-(M-1) k$
(2) Search the final item:

$$
\int_{-\infty}^{\bar{u}} \bar{u} f(u) d u+\int_{\bar{u}}^{\infty} u f(u) d u-M k
$$

## Optimal Stopping

- Stop searching if

$$
\bar{u}-(M-1) k \leq \int_{-\infty}^{\bar{u}} \bar{u} f(u) d u+\int_{\bar{u}}^{\infty} u f(u) d u-M k
$$

- Implying

$$
k \leq \int_{\bar{u}}^{\infty}(u-\bar{u}) f(u) d u
$$

- Value of RHS decreasing in $\bar{u}$
- Implies cutoff strategy: search continues if $\bar{u}>u^{*}$ solving

$$
k=\int_{u^{*}}^{\infty}\left(u-u^{*}\right) f(u) d u
$$

## Optimal Stopping

- Now consider behavior when there are 2 items remaining
- $\bar{u}<u^{*}$ Search will continue
- Search optimal if one object remaining
- Can always operate continuation strategy of stopping after searching only one more option
- $\bar{u}>u^{*}$ search will stop
- Not optimal to search one more item only
- Search will stop next period, as $\bar{u}>u^{*}$


## Optimal Stopping

- Optimal stopping strategy is satisficing!
- Find $u^{*}$ that solves

$$
k=\int_{u^{*}}^{\infty}\left(u-u^{*}\right) f(u) d u
$$

- Continue searching until find an object with $u>u^{*}$, then stop
- Model of underlying constrains allow us to make predictions about how reservation level changes with environment
- $u^{*}$ decreasing in $k$
- increasing in variance of $f$ (for well behaved distributions)
- Unaffected by the size of the choice set
- Comes from optimization, not reduced form satisficing model


## Optimal Stopping - Extensions and Notes

- Satisficing as Framing
- Imagine you are provided with some ranking of alternatives
- You believe that this ranking is correlated (arbitrarily weakly) with your preferences
- This is the only thing you know ex ante about each alternative. (e.g. Google searches)
- What should your search order be?
- Should search in the same order as the ranking
- If list is long and correlation is low
- Ex ante difference in quality between the first and last alternative is very low
- But you will never pick the last alternative!
- See for example Feenberg, Daniel, et al. "It's good to be first: Order bias in reading and citing NBER working papers." Review of Economics and Statistics 99.1 (2017): 32-39.


## Optimal Stopping - Extensions and Notes

- Satisficing is a knife edge case
- If one changes the problem
- Learning
- Varying information costs
- Then reservation level will change over time
- Testable prediction about the 'satisficing' model


## Optimal Stopping - Extensions and Notes

- Solubility
- The fact that we can solve this search problem depends on its simple structure
- Things can get hairy very quickly
- Explore/exploit
- Multiple attributes
- There are some mathematical tools that can help
- Gittens indicies
- But often have to rely on approximate solutions
- e.g. Gabaix et al [2006]


## Optimal Stopping - Extensions and Notes

- A broader class of models
- Clearly models of sequential search with a threshold are more general than either
- Satisficing (fixed threshold)
- Optimizing models
- More generally, one could think of the threshold as an 'aspiration' and consider how it adapts based on
- Environmental factors
- The history of search
- See Selten, Reinhard. "Aspiration adaptation theory." Journal of mathematical psychology 42.2-3 (1998): 191-214.


## Testing Satisficing: The Problem

- Satisficing models difficult to test using choice data alone
- If search order is fixed, behavior is indistinguishable from preference maximization
- Define the binary relation $\unrhd$ as $x \unrhd y$ if
- $x, y$ above satisficing level and $x$ is searched before $y$
- $x$ is above the satisficing level and $y$ below it
- $x, y$ both satisficing level and $u(x) \geq u(y)$
- Easy to show that $\unrhd$ is a complete preorder, and consumer chooses as if to maximize $\unrhd$
- If search order changes between choice sets, then any behavior can be rationalized
- Assume that all alternatives are above satisficing level
- Chosen alternative is then assumed to be the first alternative searched.


## Choice Process Data

- Need to either
- Add more assumptions
- Enrich the data
- Examples
- Search order observed from internet data [De los Santos, Hortacsu, and Wildenbeast 2012]
- Stochastic choice data [Aguiar, Boccardi and Dean 2016]


## Choice Process Data

- We will start by considering one possible data enrichment: 'choice process' data
- Records how choice changes with contemplation time
- $C(A)$ : Standard choice data - choice from set $A$
- $C_{A}(t)$ : Choice process data - choice made from set $A$ after contemplation time $t$
- Easy to collect such data in the lab
- Possible outside the lab using the internet?
- Has been used to
- Test satisficing model [Caplin, Dean, Martin 2012]
- Understand play in beauty contest game [Agranov, Caplin and Tergiman 2015]
- Understand fast and slow processes in generosity [Kessler, Kivimaki and Niederle 2016]
- In combination with mouselab [Geng 2015]


## Notation

- How can we use choice process data to test the satisficing model?
- First, introduce some notation:
- $X$ : Finite grand choice set
- $\mathcal{X}:$ Non-empty subsets of $X$
- $Z \in\left\{Z_{t}\right\}_{t}^{\infty}$ : Sequences of elements of $\mathcal{X}$
- $\mathcal{Z}$ set of sequences $Z$
- $\mathcal{Z}_{A} \subset \mathcal{Z}$ : set of sequences s.t. $Z_{t} \subset A \in \mathcal{X}$


## A Definition of Choice Process

Definition
A Choice Process Data Set $(X, C)$ comprises of:

- finite set $X$
- choice function $\mathcal{C}: \mathcal{X} \rightarrow \mathcal{Z}$
such that $C(A) \in \mathcal{Z}_{A} \forall A \in \mathcal{X}$
- $C_{A}(t)$ : choice made from set $A$ after contemplation time $t$


## Characterizing the Satisficing Model

- Two main assumptions of the satisficing model of consideration set formation
(1) Search is alternative-based
- DM searches through items in choice set sequentially
- Completely understands each item before moving on to the next
(2) Stopping is due to a fixed reservation rule
- Subjects have a fixed reservation utility level
- Stop searching if and only if find an item with utility above that level
- First think about testing (1), then add (2)


## Alternative-Based Search (ABS)

- DM has a fixed utility function
- Searches sequentially through the available options,
- Always chooses the best alternative of those searched
- May not search the entire choice set


## Alternative-Based Search

- DM is equipped with a utility function

$$
u: X \rightarrow \mathbb{R}
$$

- and a search correspondence

$$
S: \mathcal{X} \rightarrow \mathcal{Z}
$$

with $S_{A}(t) \subseteq S_{A}(t+s)$

- Such that the DM always chooses best option of those searched

$$
C_{A}(t)=\arg \max _{x \in S_{A}(t)} u(x)
$$

## Revealed Preference and ABS

- As we have seen with previous models, key to testing is identifying what revealed preference means in this setting
- What type of behavior reveals preference in the ABS model?
- Finally choosing $x$ over $y$ does not imply (strict) revealed preference
- DM may not know that $y$ was available
- Replacing $y$ with $x$ does imply (strict) revealed preference
- DM must know that $y$ is available, as previously chose it
- Now chooses $x$, so must prefer $x$ over $y$
- Choosing $x$ and $y$ at the same time reveals indifference
- Use $\succ^{A B S}$ to indicate ABS strict revealed preference
- Use $\sim^{A B S}$ to indicate revealed indifference


## Characterizing ABS

- Choice process data will have an ABS representation if and only if $\succ^{A B S}$ and $\sim^{A B S}$ can be represented by a utility function $u$

$$
\begin{aligned}
& x \succ A B S y \Rightarrow u(x)>u(y) \\
& x \sim A B S y \Rightarrow u(x)=u(y)
\end{aligned}
$$

- Necessary and sufficient conditions for utility representation GARP
- Let $\succeq^{A B S}=\succ^{A B S} \cup \sim^{A B S}$
- $x T\left(\succeq^{A B S}\right) y$ implies not $y \succ^{A B S} x$


## Theorem 1

Theorem
Choice process data admits an ABS representation if and only if $\succ^{A B S}$ and $\sim \sim^{A B S}$ satisfy GARP

Proof.
(Sketch of Sufficiency)
(1) Generate $U$ that represents $\succeq^{A B S}$
(2) Set $S_{A}(t)=\cup_{s=1}^{t} C_{A}(s)$

## Satisficing

- Choice process data admits an satisficing representation if we can find
- An ABS representation $(u, S)$
- A reservation level $\rho$
- Such that search stops if and only if an above reservation object is found
- If the highest utility object in $S_{A}(t)$ is above $\rho$, search stops
- If it is below $\rho$, then search continues
- Implies complete search of sets comprising only of below-reservation objects


## Revealed Preference and Satisficing

- Final choice can now contain revealed preference information
- If final choice is below-reservation utility
- How do we know if an object is below reservation?
- If they are non-terminal: Search continues after that object has been chosen


## Directly and Indirectly Non-Terminal Sets

- Directly Non-Terminal: $x \in X^{N}$ if
- $x \in C_{A}(t)$
- $C_{A}(t) \neq C_{A}(t+s)$
- Indirectly Non Terminal: $x \in X^{\prime}$ if
- for some $y \in X^{N}$
- $x, y \in A$ and $y \in \lim _{t \rightarrow \infty} C_{A}(t)$
- Let $X^{I N}=X^{\prime} \cup X^{N}$


## Add New Revealed Preference Information

- If
- one of $x, y \in A$ is in $X^{I N}$
- $x$ is finally chosen from some set $A$ when $y$ is not,
- then, $x \succ^{S} y$
- If $x$ is is in $X^{I N}$, then $A$ must have been fully searched, and so $x$ must be preferred to $y$
- If $y$ is in $X^{I N}$, then either $x$ is below reservation level, in which case the set is fully searched, or $x$ is above reservation utility
- Let $\succ=\succ^{S} \cup \succ^{A B S}$


## Theorem 2

Theorem
Choice process data admits an satisficing representation if and only if $\succ$ and $\sim{ }^{A B S}$ satisfy GARP

## Experiments and Bounded Rationality

- The experimental lab is often a good place to test models of bounded rationality
- Pros
- Easy to identify choice mistakes
- Can collect precisely the type of data you need
- Can control the parameters of the problem
- Cons
- Lack of external validity?
- A good approach (and good dissertation!) is to combine
- Theory
- Lab experiments
- Field experiments/non experimental data


## Experimental Design

- Experimental design has two aims
- Identify choice 'mistakes'
- Test satisficing model as an explanation for these mistakes
- Two design challenges
- Find a set of choice objects for which 'choice quality' is obvious but subjects do not always choose best option
- Find a way of eliciting 'choice process data'
- We first test for 'mistakes' in a standard choice task...
- ... then add choice process data in same environment
- Make life easier for ourselves by making preferences directly observable


## Choice Objects

- Subjects choose between 'sums'


## four plus eight minus four

- Value of option is the value of the sum
- 'Full information' ranking obvious, but uncovering value takes effort
- 6 treatments
- $2 \times$ complexity ( 3 and 7 operations)
- $3 \times$ choice set size ( 10,20 and 40 options)
- No time limit


## Size 20, Complexity 7

| zero |
| :---: |
| seven minus four minus two minus four minus two plus eleven minus four |
| six plus five minus eight plus two minus nine plus one plus four |
| seven minus two minus four plus three plus four minus three minus three |
| seven plus five minus two minus two minus three plus zero minus two |
| six plus seven plus six minus two minus six minus eight plus four |
| six plus two plus five minus four minus two minus seven plus three |
| six minus four minus one minus one plus five plus three minus six |
| two plus six plus seven minus two minus four minus two plus zero |
| two minus three minus five plus nine minus one plus five minus three |
| three plus zero plus two plus zero plus one minus three minus one |
| four plus three plus zero minus two plus three plus four minus ten |
| Seven plus two plus seven minus seven plus three minus two minus two |
| three plus three minus two plus zero plus zero minus four plus five |
| two minus two plus zero plus nine minus two minus one minus one |
| three plus four minus three plus three minus four plus three minus four |
| three plus five plus seven plus five minus two minus seven minus ten |
| three plus six minus eight plus one plus two minus two plus zero |
| three plus five plus zero plus four plus three minus four minus two |
| eight minus one plus one minus four minus four minus five plus six |
| four minus five plus four minus one minus four plus zero plus four |

# Results 

## Failure rates (\%) (22 subjects, 657 choices)

| Failure rate |  |  |
| :---: | :---: | :---: |
|  | Complexity |  |
| Set size | 3 | 7 |
| 10 | $7 \%$ | $24 \%$ |
| 20 | $22 \%$ | $56 \%$ |
| 40 | $29 \%$ | $65 \%$ |


| Average Loss (\$) |  |  |
| :---: | :---: | :---: |
|  | Complexity |  |
| Set size | 3 | 7 |
| 10 | 0.41 | 1.69 |
| 20 | 1.10 | 4.00 |
| 40 | 2.30 | 7.12 |

## Eliciting Choice Process Data

(1) Allow subjects to select any alternative at any time

- Can change selection as often as they like
(2) Choice will be recorded at a random time between 0 and 120 seconds unknown to subject
- Incentivizes subjects to always keep selected current best alternative
- Treat the sequence of selections as choice process data
(3) Round can end in two ways
- After 120 seconds has elapsed
- When subject presses the 'finish' button
- We discard any rounds in which subjects do not press 'finish'


## Stage 1: Selection

Round
2 of 30

## Stage 2: Choice Recorded

## $\%$ NEW YORK UNIVERSITY

## Choice Recorded

In this round, your choice was recorded after 9 seconds. At that time, you had selected:


## Do We Get Richer Data from Choice Process Methodology? <br> 978 Rounds, 76 Subjects

| 10 Options, Complexity 3 | 20 Options, Complexity 3 | 40 Options, Complexity 3 |
| :---: | :---: | :---: |
|  |  |  |
| 10 Options, Complexity 7 | 20 Options, Complexity 7 | 40 Options, Complexity 7 |
|  |  |  |

## Testing ABS

- Choice process data has ABS representation if $\succ^{A B S}$ is consistent
- Assume that more money is preferred to less
- Implies subjects must always switch to higher-valued objects (Condition 1)
- Calculate Houtman-Maks index for Condition 1
- Largest subset of choice data that is consistent with condition


## Houtman-Maks Measure for ABS

Actual data


Random data


## Traditional vs ABS Revealed Preference

Traditional


ABS


## Satisficing Behavior



## Estimating Reservation Levels

- Choice process data allows observation of subjects
- Stopping search
- Continuing to search
- Allows us to estimate reservation levels
- Assume that reservation level is calculated with some noise at each switch
- Can estimate reservation levels for each treatment using maximum likelihood


## Estimated Reservation Levels

|  | Complexity |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Set size | 3 |  | 7 |  |
| 10 | 9.54 | $(0.20)$ | 6.36 | $(0.13)$ |
| 20 | 11.18 | $(0.12)$ | 9.95 | $(0.10)$ |
| 40 | 15.54 | $(0.11)$ | 10.84 | $(0.10)$ |

## Estimating Reservation Levels

- Increase with 'Cost of Search'
- In line with model predictions
- Increase with size of choice set
- In violation of model predictions
- See Brown, Flinn and Schotter [2011] for further insights


## But....

- De los Santos et al. [2012] come to a different conclusion using their data
- If search is visible, Satisficing makes one strong prediction
- Should choose last object searched (unless search is complete)
- But this is not what they find
- Data more consistent with a model in which the consideration set is decided upon ahead of time
- For a more complete review see reading
- Honka, Elisabeth, Ali Hortaçsu, and Matthijs Wildenbeest. "Empirical search and consideration sets." Handbook of the Economics of Marketing. Vol. 1. North-Holland, 2019. 193-257.


## Summary

- There is good evidence that people do not look at all the available alternatives when making a choice
- Lab experiments
- Internet search
- Verbal reports
- Direct observation of search
- Pure consideration set models cannot be tested on choice data alone
- Need either more data or more assumptions
- A variety of both approaches have been applied in the literature
- Choice process
- Internet search
- Stochastic choice
- As yet, no real consensus on what is the correct model of consideration set formation
- Though we do have some hints.

