Reference Dependence In the Brain

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- So far we have presented some evidence that sensory coding may be reference dependent
- In this lecture we will present evidence that important value systems in the brain are also reference dependent
- Will also show how neuroscientific measurement and economic theory can be merged to answer interesting questions

The Reward Prediction Error Hypothesis

- *Dopamine* is a neurotransmitter
 - Transmits information between brain cells
- Until relatively recently, assumed to be the brain's 'happy place'
- Turns out to be more complicated that that
- Now hypothesized to encode *Reward Prediction Error (RPE)*
 - Difference between experienced and predicted rewards
- If true, lots of interesting implications
 - RPE used in AI learning
 - Explicit reference dependence
 - Makes reference point observable

Early Evidence for RPE - Monkeys Schultz et al. [1997]

- Dopamine fires only on receipt of *unpredicted* rewards
- Otherwise will fire at *first* predictor of reward
- If an expected reward is not received, dopamine firing will pause



- Thirsty human subjects placed in fMRI scanner
- Shown novel visual symbols, which signalled 'neutral' and 'tasty' juice rewards
- Assumptions made to operationalize RPE
 - Reward: values of juice
 - Learning: through TD algorithm
- Resulting RPE signal then correlated with brain activity
- Positive correlation with activity in Ventral Striatum taken as supporting RPE hypothesis
 - Ventral Striatum rich in dopaminergic neurons

Problems with the Current Tests

- Several other theories for the role of dopamine
 - Salience hypothesis (e.g. Zink et al. 2003)
 - Incentive salience hypothesis (Berridge and Robinson, 1998)
 - Agency hypothesis (Redgrave and Gurney, 2006)
- These theories have been hard to differentiate
- Couched in terms of latent variable
 - 'Rewards', 'Beliefs', 'Salience', 'Valence' not directly observable
- Tests rely on 'auxiliary assumptions' not central to the underlying theory
 - Experiments test both underlying theory *and* auxiliary assumptions
- Also different models tend to lead to very highly correlated predictions

An Axiomatic Approach

- Alternative: take an axiomatic approach to testing RPE hypothesis
 - A set of necessary and sufficient conditions on dopamine activity
 - Equivalent to the RPE model
 - Easily testable
- Similar to Samuelson's approach to testing utility maximization
 - Equivalent to the Weak Axiom of Revealed Preference
- Has several advantages
 - Provide a complete list of testable predictions of the RPE model
 - Non-parametric
 - Failure of particular axioms will aid model development

- Subjects receive prizes from lotteries:
 - Z: A space of prizes
 - Λ : Set of all lotteries on Z
- $\Lambda(z)$: Set of all lotteries whose support includes z
- e_z : Lottery that gives prize z with certainty

• Observable data is a Dopamine Release Function

$$\delta : M \to \mathbb{R}$$
$$M = \{(z, p) | z \in Z, p \in \Delta(z)\}$$

 $\delta(\textbf{z},\textbf{p})$ is dopamine activity when prize z is obtained from a lottery p

A Graphical Representation



Dopamine Release

A Formal Model of RPE

The difference between how good an event was expected to be and how good it turned out to be

- Under what conditions can we find
 - A Predicted reward function: $b: \Lambda \to \mathbb{R}$
 - An Experienced reward function: $r: Z \to \mathbb{R}$
- Such that there is an aggregator function E
 - Represents the dopamine release function

$$\delta(z,p) = E(r(z),b(p))$$

- Is increasing in experienced and decreasing in predicted reward.
- Obeys basic consistency

$$r(z) = b(e_z)$$

• Treats 'no surprise' consistently:

$$E(x,x)=E(y,y)$$

• Special case:

$$\delta(z,p)=r(z)-b(p)$$

Necessary Condition 1: Consistent Prize Ordering



Necessary Condition 1: Consistent Prize Ordering

- Consider two prizes, z and w
- Say that, when z is received from some lottery p, more dopamine is released than when w is received from p
- Implies higher 'reward' for z than w
- Implies that z should give more dopamine than w when received for any lottery q
- Axiom A1: Coherent Prize Dominance

for all
$$(z, p), (w, p), (z, q), (w, q) \in M$$

 $\delta(z, p) > \delta(w, p) \Rightarrow \delta(z, q) > \delta(w, q)$

Necessary Condition 2: Coherent Lottery Dominance



Necessary Condition 2: Consistent Lottery Ordering

- Consider two lotteries *p* and *q* and a prize *z* which is in the support of *p* and *q*
- Say that more dopamine is released when z is obtained from p that when it is obtained from q
- Implies that predicted reward of p must be *lower* that that of q
- Implies that whenever the same prize is obtained from p and q the dopamine released should be higher from lottery p than from lottery q
- Axiom A2: Coherent Lottery Dominance

for all
$$(z, p), (w, p), (z, q), (w, q) \in M$$

 $\delta(z, p) > \delta(z, q) \Rightarrow \delta(w, p) > \delta(w, q)$

Necessary Condition 3: No Surprise Equivalence

Necessary Condition 3: Equivalence of Certainty

- 'Reward Prediction Error' is a comparison between predicted reward and actual reward
- If you know exactly what you are going to get, then there is no reward prediction error
- This is true whatever the prize we are talking about
- Thus, the reward prediction error of any prize should be zero when received for sure:
- Axiom A3: No Surprise Equivalence

$$\delta(\mathbf{z}, \mathbf{e}_{\mathbf{z}}) = \delta(\mathbf{w}, \mathbf{e}_{\mathbf{w}}) \; \forall \; \mathbf{z}, \mathbf{w} \in Z$$

- In general, these conditions are necessary, but not sufficient for an RPE representation
- However, in the special case where we look only at lotteries with two prizes they are
- Theorem 1:
 - If |Z| = 2, a dopamine release function δ satisfies axioms A1-A3 if and only if it admits an RPE representation
- Thus, in order to test RPE in case of two prizes, we need only to test A1-A3

- Generate observations of δ in order to test axioms
- Use a data set containing:
 - Two prizes: win \$5, lose \$5
 - Five lotteries: $p \in \{0, 0.25, 0.5, 0.75.1\}$
- Do not observe dopamine directly
 - Use fMRI to observe activity in the Nucleus Accumbens
 - Brain area rich in dopaminergic neurons

Experimental Design

- 14 subjects (2 dropped for excess movement)
- 'Practice Session' (outside scanner) of 4 blocks of 16 trials
- 2 'Scanner Sessions' of 8 blocks of 16 trials
- For Scanner Sessions, subjects paid \$35 show up fee, + \$100 endowment + outcome of each trial
- In each trial, subject offered one option from 'Observation Set' and one from a 'Decoy Set'

Constructing Delta Defining Regions of Interest

- Need to determine which area of the brain is the Nucleus Accumbens
- Two ways of doing so:
 - Anatomical ROIs: Defined by location
 - Functional ROIs: Defined by response to a particular stimulus
- We concentrate on anatomical ROI, but use functional ROIs to test results

Constructing Delta

Anatomical Regions of Interest [Neto et al. 2008]

- We now need to estimate the function $ar{\delta}$ using the data
- Use a between-subject design
 - Treat all data as coming from a single subject
- Create a single time series for an ROI
 - Average across voxels
 - Convert to percentage change from session baseline
- Regress time series on dummies for the revelation of each prize/lottery pair
 - $\bar{\delta}(x,p)$ is the estimated coefficient on the dummy which takes the value 1 when prize x is obtained from lottery p

Results

Prob of winning \$5

Results

- Axioms hold
- Nucleus Accumbens activity in line with RPE model
- Experienced and predicted reward 'sensible'

Time Paths

Early Period

Prob of winning \$5

Late Period

Prob of winning \$5

Two Different Signals?

Starting TR

- fMRI activity in Nucleus Accumbens does satisfy the necessary conditions for an RPE encoder
- However, this aggregate result may be the amalgamation of two separate signals
 - Vary in temporal lag
 - Vary in magnitude

Observing 'beliefs' and 'rewards'?

- Axioms + experimental results tell us we can assign numbers to events such that NAcc activity encodes RPE according to those numbers
- Can we use these numbers to make inferences about beliefs and rewards?
 - Are they 'beliefs' and 'rewards' in the sense that people usually use the words?
 - Can we find any 'external validity' with respect to other observables?
 - Behavior?
 - Obviously rewarding events?
 - Can we then generalize to other situations?

Economic Applications

- New way of observing beliefs
- Makes 'surprise' directly observable
- Insights into mechanisms underlying learning
- Building blocks of 'utility'

- We provide evidence that NAcc activity encodes RPE
- Can recover consistent dopaminergic 'beliefs' and 'rewards'
- Potential for important new insights into human behavior and 'state of mind'

What about other brain areas?

Anterior Insula seems to record magnitude of RPE