Preference for Commitment

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- In order to discuss preference for commitment we need to be able to discuss **preferences over menus**
- Interpretation: choosing a set of alternatives from which you will make a choice at a later date.
- What would be the standard way of assessing a menu of options A = {a₁, a₂, a₃, ...}?
- Assume that you will choose the best option from the menu at the later date
- Then a menu A is preferred to menu B if the best option in A is better than the best option in B
- i.e.

$$A \succeq B$$
 if and only if
 $\max_{a \in A} u(a) \geq \max_{b \in B} u(b)$

- For a 'standard' decision maker, more options to choose from is always (weakly) better
- Add alternative *a* to a choice set *A*
 - Either a is preferred to all the options already in A
 - a will be chosen from the expanded choice set
 - $\{a\} \cup A$ is better than A
 - Or there is some b in A which is preferred to a
 - a will not be chosen from the expanded choice set
 - $\{a\} \cup A$ is no better, and no worse than A
- DM will always prefer to have a bigger menu to choose from

$$\begin{array}{rcl} \mathsf{B} & \subset & \mathsf{A} \\ & \Rightarrow & \mathsf{A} \succeq \mathsf{B} \end{array}$$

- This may not be the case if the DM suffers from problems of temptation:
- Classic example: A dieter might prefer to a restaurant with the menu



rather than one with the menu



- Why?
- (At least) two possible reasons
 - Would prefer to not eat the burger, but worries they will succumb to temptation if the burger is available
 - 2 Thinks they will be able to overcome the temptation to eat the burger, but it will be costly to do so

- We are going to discuss a model of menu preferences and choice that captures both these forces
- Based on the classic work of Gul and Pesendorfer [2001]
- Updated (and better explained) by Lipman and Pesendorfer [2013]

- Let C be a compact metric space
- $\Delta(C)$ set of all measures on the Borel σ -algebra of C (i.e. all lotteries)
 - Use lotteries because it means set of choice objects is convex
- Endow $\Delta(C)$ with topology of weak convergence
- Z all non empty compact subsets of $\Delta(C)$ (Hausdorff topology)
- Let \succeq be a preference relation on Z
 - Interpretation: preference over menus from which you will later get to choose
- Let \supseteq be a preference relation on $\Delta(C)$
 - Interpretation: preferences when asked to choose from a menu



• For $x, y \in Z$ and $\alpha \in (0, 1)$ define

$$\alpha x + (1 - \alpha)y$$

= { $p = \alpha q + (1 - \alpha)r | q \in x, r \in y,$ }

• E.g. if $x = \{\delta_a\}$, $y = \{\delta_b, \delta_c\}$ the

$$= \begin{cases} \alpha x + (1-\alpha)y \\ \alpha a + (1-\alpha)b \\ \alpha a + (1-\alpha)c \end{cases}$$

• Mixture of all elements in menu x with all elements in menu y

Modelling Preference over Menus

- Using this set up we will place axioms on \succeq and \trianglerighteq
- First, we will consider conditions which are necessary and sufficient for the standard model
 - Single utility function
 - Represents ⊵ (choice from menus)
 - \succeq (choice between menus) represented using largest utility in the set
- Next, consider how to alter these axioms in order to generate the 'Gul Pesendorfer' model
 - Allows for both 'temptation' and 'self control' to be expressed in menu preferences

Axiom 1 (Preference Relations) \succeq , \succeq are complete preference relations

Axiom 2 (Independence) $x \succeq y$ implies $\alpha x + (1 - \alpha)z \succeq \alpha y + (1 - \alpha)z \forall x, y, z \in Z,$ $\alpha \in (0, 1)$

- Notice that this is not the same as 'standard' independence
- Mixing operation is different
- Need to think a bit about how to interpret it

- Interpretation of independence: Standard Independence + Indifference to Timing of Uncertainty
 - Imagine we extended \succeq to preferences over lotteries over menus
 - Independence would now say that, if we prefer choosing from x to choosing from y then we prefer choosing from x α% of the time (and z (1 α)% of the time) to choosing from y α% of the time (and z (1 α)% of the time)
 - Randomization occurs before choosing at second stage
- Claim: choosing contingent plans in this set up gives rise to the same probability distribution over outcomes as come about from 'Gul Pesendorfer' mixing

Basic Axioms

• Example

$$\frac{1}{2}x + \frac{1}{2}z$$

x = {x₁, x₂}, z = {z₁, z₂}

• Gul-Pesendorfer mixing: a menu of

$$\left\{\begin{array}{c}\frac{1}{2}x_{1}+\frac{1}{2}z_{1}\\\frac{1}{2}x_{2}+\frac{1}{2}z_{1}\\\frac{1}{2}x_{1}+\frac{1}{2}z_{2}\\\frac{1}{2}x_{2}+\frac{1}{2}z_{2}\end{array}\right\}$$

- 'Standard' Mixing: 50% chance of menu x, 50% chance of menu y
 - Contingent plan: choose either x₁ or x₂ from x and either y₁ or y₂ from y
 - Uncertainty decided before second stage choice
 - Set of contingent plans gives rise to same menu of lotteries over outcomes as does GP mixing

- If timing of resolution of uncertainty is not important there is an equivalence between
 - Choosing a contingent plan for a lottery over menus
 - Choosing from a menu of lotteries generated by 'Gul Pesendorfer' mixing
- Thus, 'standard' independence and indifference to timing of uncertainty give rise to GP independence

Axiom 3 (Sophistication) $x \cup \{p\} \succ x \Leftrightarrow p \rhd q \ \forall q \in x$

- This is the axiom that links together first and second stage choice.
- Whether or not people are sophisticated is going to be an important empirical question
 - Do they understand the choices they will make from a given menu?
 - If not, may underestimate their degree of self control
 - e.g. sign up for gym memberships they do not use
 - or make costly commitments which they subsequently do not stick to.

Axiom 4 (Continuity) Three continuity conditions:

- (Upper Semi Continuity): The sets $\{z \in Z | z \succeq x\}$ and $\{p \in \Delta(C) | p \trianglerighteq q\}$ are closed for all x and q
- ② (Lower vNM Continuity): $x \succ y \succ z$ implies $\alpha x + (1 a)z \succ y$ for some $\alpha \in (0, 1)$
- **③** (Lower Singleton Continuity): The sets $\{p : \{q\} \succeq \{p\}\}$ are closed for every q

• The Standard Model of preference over menus

$$U(z) = \max_{p \in z} u(p)$$

for some linear, continuous utility $u: \Delta(C) \to \mathbb{R}$ such that

- U represents ∠
- u represents \geq

Standard Model

Equivalent to axioms 1-4 and

$$x \succeq y \Rightarrow x \cup y \sim x$$

- x ≽ y implies that the best alternative in x is weakly better than the best alternative in y
- The best alternative in *x* ∪ *y* is the same as the best alternative in *x*
- Thus $x \cup y \sim x$
- Note that this implies

$$x \supset y \Rightarrow x \succeq y$$

• Say $y \succ x$

• either $x/y \succeq y$ in which case

• or
$$y \succeq x/y$$

 $x = x/y \cup y \sim x/y \succeq y \succ x$
 $x = x/y \cup y \sim y \succ x$

The Gul Pesendorfer Model

• Preference over menus given by

$$U(x) = \max_{p \in x} \left[u(p) + v(p) \right] - \max_{q \in x} v(q)$$

- *u* : 'long run' utility
- v : 'temptation' utility
- Interpretation:
 - Choose p to maximize u(p) + v(p)
 - Suffer temptation cost v(p) v(q)
- Unlike the standard model, the Gul Pesendorfer model can lead to strict preference for smaller choice sets

$$x \supset y$$
 but $x \prec y$

Case 1: Commitment

Object	и	V
Salad	4	0
Fish	2	1
Burger	1	4

• Which menu would the DM prefer? $\{s\}$ or $\{s, b\}$?

$$U(\{s\}) = \max_{x \in \{s\}} (u(x) + v(x)) - \max_{y \in \{s\}} v(y)$$

= 4+0-0
= 4

$$U(\{s, b\}) = \max_{x \in \{s, b\}} (u(x) + v(x)) - \max_{y \in \{s, b\}} v(y)$$

= 1+4-4
= 1

Case 1: Commitment

Object	и	v
Salad	4	0
Fish	2	1
Burger	1	4

- Menu $\{s\}$ preferred to $\{s.b\}$
- Interpretation: *b* would be chosen from the latter menu
 - u(b) + v(b) > u(s) + v(s)
- But s has higher long run utility
 - u(s) > u(b)
- The DM would rather not have *b* in their menu, because if it is available they will choose it.

Case 1: Commitment

• More generally, consider p, q, such that

$$u(p) > u(q)$$

$$u(q) + v(q) > u(p) + v(p)$$

Then

$$U(\{p\}) = u(p) U(\{p,q\}) = u(q) + v(q) - v(q) = u(q) U(\{q\}\} = u(q)$$

- Interpretation: give in to temptation and choose q
- 'Weak set betweenness'

$$\{p\} \succ \{p,q\} \sim \{q\}$$

Case 2: Avoid 'Willpower Costs'

Object	и	V
Salad	4	0
Fish	2	1
Burger	1	4

• Which menu would the DM prefer? $\{s\}$ or $\{s, f\}$?

$$U(\{s\}) = \max_{x \in \{s\}} (u(x) + v(x)) - \max_{y \in \{s\}} v(y)$$

= 4+0-0
= 4

$$U(\{s, f\}) = \max_{x \in \{s, f\}} (u(x) + v(x)) - \max_{y \in \{s, f\}} v(y)$$

= 4 + 0 - 1
= 3

Case 2: Avoid 'Willpower Costs'

Object	и	V
Salad	4	0
Fish	2	1
Burger	1	4

- Menu $\{s\}$ is preferred to menu $\{s, f\}$
- However, this time, s would be chosen from both menus, as

$$u(s) + v(s) > u(f) + v(f)$$

- The DM still prefers to have f removed from the menu because it is more tempting: v(f) > v(s)
- The DM is able to exert self control if both options are on the menu, but it is costly to do so

Case 2: Avoid 'Willpower Costs'

• More generally, consider p, q, such that

$$u(p) > u(q)$$

 $v(q) > v(p)$
 $u(p) + v(p) > u(q) + v(q)$

Then

$$U(\{p\}) = u(p) U(\{p,q\}) = u(p) + v(p) - v(q) U(\{q\}\} = u(q)$$

- Interpretation: fight temptation, but this is costly
- 'Strict set betweenness'

$$\{p\} \succ \{p,q\} \succ \{q\}$$

Temptation and Self Control

- We say that q tempts p if $\{p\} \succ \{p, q\}$
- We say that a decision maker exhibits self control at y if there exists x, z such that x ∪ z = y and

$$\{x\} \succ \{y\} \succ \{z\}$$

- {x} ≻ {y} implies there exists something in z which is tempting relative to items in x
- $\{y\} \succ \{z\}$ implies tempting item not chosen
- if it were then

$$\max_{p \in y} u(p) + v(p) = \max_{p \in z} u(p) + v(p) \Rightarrow$$
$$U(y) = \max_{p \in y} (u(p) + v(p)) - \max_{q \in y} v(q)$$
$$\leq \max_{p \in z} (u(p) + v(p)) - \max_{q \in z} v(q)$$
$$= U(z)$$

Why 'Long Run' and 'Temptation' Utilities?

- So far we have described *u* as 'long run' utility and *v* as 'temptation' utility
- Why is this a behaviorally appropriate description?
- *u* describes choices over singleton menus:

$$U(\{p\}) = u(p) + v(p) - v(p) = u(p)$$

and so describes preferences when the DM is not tempted

• v leads to temptation: q tempts p only if v(q) > v(p)

• Case 1:
$$u(p) + v(p) \ge u(q) + v(q)$$

$$U(\{p\}) > u(\{p,q\})$$

$$\Rightarrow u(p) > u(p) + v(p) - \max_{r \in \{p,q\}} v(r)$$

$$\Rightarrow \max_{r \in \{p,q\}} v(r) > v(p)$$

$$\Rightarrow v(q) = \max_{r \in \{p,q\}} v(r) > v(p)$$

• v leads to temptation: q tempts p only if v(q) > v(p)

• Case 2:
$$u(q) + v(q) > u(p) + v(p)$$

$$U(\{p\}) > u(\{p,q\})$$

$$\Rightarrow u(p) > u(q) + v(q) - \max_{r \in \{p,q\}} v(r)$$

$$\Rightarrow u(p) + \max_{r \in \{p,q\}} v(r) > u(q) + v(q)$$

$$\Rightarrow \max_{r \in \{p,q\}} v(r) = v(q) > v(p)$$

• Last line follows from assumption u(q) + v(q) > u(p) + v(p)

- Imagine that differences in v are large relative to differences in u
- In the limit, model reduces to

$$U(x) = \max_{p \in x} u(p) \text{ s.t. } v(p) \ge v(q) \ \forall \ q \in x$$

- This is the 'Strolz' model
- Implies no strict set betweenness, and not self control
- $\beta \delta$ model is of this class

• Set Betweenness: for any x, y s.t $x \succeq y$

 $x \succeq x \cup y \succeq y$

• Notice the difference to the 'standard' model

$$x \succeq y \Rightarrow x \cup y \sim x$$

• Smaller sets can be strictly preferred

• Set Betweenness: for any x, y s.t $x \succeq y$

$$x \succeq x \cup y \succeq y$$

- Necessity:
 - x ≽ y implies that

$$u(p^{x}) + v(p^{x}) - v(q^{x}) \ge u(p^{y}) + v(p^{y}) - v(q^{y})$$

where

$$p^i = rg\max_{p \in i} u(p) + v(p)$$

and

$$q^i = rg\max_{q \in i} v(q)$$

• NTS $x \succeq x \cup y$

- Two cases:
- Case 1: $u(p^{x}) + v(p^{x}) \ge u(p^{y}) + v(p^{y})$

$$\begin{array}{rcl} u(p^{x})+v(p^{x}) & \geq & u(p^{y})+v(p^{y}) \Rightarrow \\ u(p^{x})+v(p^{x}) & = & u(p^{x\cup y})+v(p^{x\cup y}) \Rightarrow \\ u(p^{x})+v(p^{x})-v(q^{x}) & \geq & u(p^{x\cup y})+v(p^{x\cup y})-v(q^{x\cup y}) \end{array}$$

• Case 2:
$$u(p^x) + v(p^x) < u(p^y) + v(p^y)$$

• implies $v(q^x) \leq v(q^y)$ as x is preferred to y

$$u(p^{y}) + v(p^{y}) = u(p^{x \cup y}) + v(p^{x \cup y})$$
$$v(q^{x \cup y}) = v(q^{y}) \Rightarrow$$
$$u(p^{x \cup y}) + v(p^{x \cup y}) - v(q^{x \cup y}) = u(p^{y}) + v(p^{y}) - v(q^{y})$$
$$\leq u(p^{x}) + v(p^{x}) - v(q^{x})$$

Theorem

 \succeq satisfies Axioms 1, 2, 4 and set betweenness if and only if it has

a Strolz representation or a G-P representation

Theorem

The proper relation \succeq and \trianglerighteq satisfy Axioms 1-4 and set betweenness if and only if

- \succeq has a Stroltz representation and $p \trianglerighteq q$ if and only if v(p) > v(q) or v(p) = v(q) and $u(p) \ge u(q)$
- or \succeq has a G-P representation and u(p) + v(p) represents \trianglerighteq

Sketch of Proof that Axioms Imply Representation

- Lemma 1: Axioms 1, 2, 4 imply a linear $U: Z \rightarrow \mathbb{R}$ that represents \succeq and is continuous on singleton sets
 - This is standard, and makes use of the mixture space axioms

Sketch of Proof that Axioms Imply Representation

• Lemma 2: Show that

$$U(x) = \max_{p \in x} \min_{q \in x} U(\{p, q\})$$
$$= \min_{q \in x} \max_{p \in x} U(\{p, q\})$$

- Utility depends only on 'chosen element', and 'most tempting element
- Proof: Let $\bar{u} = \max_{p \in x} \min_{q \in x} U(\{p, q\}) = U(\{p^*, q^*\})$
- Note that $U(\{p^*,q\}) \geq U(\{p^*,q^*\}) = ar{u} \ orall \ q \in A$
- Set betweenness implies $ar{u} \leq U(\cup_{q \in x} \{p^*, q\}) = U(x)$
- Also, for every $p \in A$, $\exists q_p \in A$ such that $U(\{p, q_p\}) \leq \bar{u}$
- By set betweenness $ar{u} \geq U(\cup_{p\in A} \{p,q_p\}) = U(x)$

Sketch of Proof that Axioms Imply Representation

• Lemma 3: Show that

$$\begin{array}{lll} U(\{x\}) &> & U(\{x,y\}) > U(\{y\}) \\ U(\{a\}) &> & U(\{a,b\}) > U(\{b\}) \end{array}$$

implies

$$U(\alpha \{x, y\} + (1 - \alpha) \{a, b\}) = U(\{\alpha x + (1 - \alpha)a), \alpha y + (1 - \alpha)b)\})$$

 This comes straight from super independence and the fact that αx + (1 - α)a is the best and αy + (1 - α)b the most tempting element

Define

$$u(p) = U(\{p\})$$

$$v(s; p, q, \delta) = \frac{U(\{p, q\}) - U(\{p, (1-\delta)q + \delta s\})}{\delta}$$

- *u* is the long run utility
- v is a measure of how tempting s is relative to p and q (under the assumption p is chosen)

• Lemma 4: Show that, if

$$U(\{p\}) > U(\{p, (1-\delta)r + \delta s\}) > U(\{(1-\delta)r + \delta s\})$$

for all $s \in \Delta(C)$, then

1
$$U(\{p\}) > U(\{p,s\}) > U(s) \Rightarrow v(s; p, q, \delta) = U(\{p,q\}) - U(\{p,s\})$$

2 $v(p; p, q, \delta) = U(\{p,q\}) - U(\{p\})$

• Follows from Lemma 3

• Lemma 5: Show that, if

$$U(\{p\}) \ge U(\{p,q\}) \ge U(\{q\})$$

and for some r and δ

$$U(\{p\}) > U(\{p, (1-\delta)r + \delta s\}) > U(\{(1-\delta)r + \delta s\})$$

for all $s \in \Delta(C)$, then

$$U(\{p,q\}) = \max_{w \in \{p,q\}} [u(w) + v(w; p, r, \delta)] - \max_{z \in \{p,q\}} [v(z; p, r, \delta)]$$

• **Proof** (assuming)

$$U(\{p\}) > U(\{p,q\}) > U(\{q\})$$

• By previous lemma

$$v(q; p, r, \delta) = U(\{p, r\}) - U(\{p, q\})$$

$$\geq U(\{p, r\}) - U(\{p\})$$

$$= v(p; p, r, \delta)$$

and so

$$\max_{z \in \{p,q\}} \left[v(z; p, r, \delta) \right] = v(q; p, r, \delta)$$

Also

$$u(p) + v(p; p, r, \delta) = U(\{p\}) + U(\{p, r\}) - U(\{p\}) = U(\{p, r\})$$

$$u(q) + v(q; p, r, \delta) = U(\{q\}) + U(\{p, r\}) - U(\{p, q\})$$

and so

$$\max_{w \in \{p,q\}} [u(w) + v(w; p, r, \delta)] = u(p) + v(p; p, r, \delta)$$

• This then implies

$$\max_{w \in \{p,q\}} [u(w) + v(w; p, r, \delta)] - \max_{z \in \{p,q\}} [v(z; p, r, \delta)]$$

$$= u(p) + v(p; p, r, \delta) - v(q; p, r, \delta)$$
(1)
$$= U(\{p\}) + U(\{p, r\}) - U(\{p\}) - U(\{p, r\}) + U(\{p, q\})$$

$$= U(\{p, q\})$$
(2)

• Finally, pick p, q such that

$$U(\{p\}) > U(\{p,q\}) > U(\{q\})$$

(if such exists) and pick δ such that

 $U(\{p\}) > U(\{p, (1-\delta)q + \delta s\}) > U(\{(1-\delta)q + \delta s\})$

for all s (which we can do by continuity)

- Define v(s) as v(s; p, q, δ), and show that v(s; p, q, δ) doesn't depend on the specifics of the last three parameters.
- Lemma 5 therefore gives

$$U(\{p,q\}) = \max_{w \in \{p,q\}} [u(w) + v(w)] - \max_{z \in \{p,q\}} [v(z)]$$

• Lemma 2 then extends this result to an arbitrary set A

Discussion: Linearity

Imagine

$$\{p\} \succ \{p,q\} \succ \{q\} \succ \{q,r\} \succ \{r\}$$

- DM can resist q for p and resist r for q.
 - Can they resist r for p?
- Under the GP model, the above implies

$$u(p) > u(q) > u(r) v(r) > v(q) > v(p) u(p) + v(p) > u(q) + v(q) > u(r) + v(r)$$

• Which in turn implies

$$\{p\} \succ \{p,r\} \succ \{r\}$$

'Self Control is Linear'

- It seems that the following statement is meaningful:
 - Person A has the same long run preferences as person B
 - Person A has the same temptation as person B
 - Person A has more willpower than person B
- Yet this is not possible in the GP model
- Alternative: Masatlioglu, Nakajima and Ozdenoren [2013]

$$U(z) = \max_{p \in z} u(p)$$

subject to $\max_{q \in z} v(q) - v(p) \leq w$

Discussion: Strict Set Betweenness and Random Strolz

- Does $\{p\} \succ \{p, q\} \succ \{q\}$ imply self control?
- Imagine that you are a Strolz guy with u(p) > u(q), but are not sure that you will be tempted
- Half the time

$$v(p) = v(q)$$

half the time

Implies

$$U(\{p\}) = u(p) \\ U(\{p,q\}) = \frac{u(p) + u(q)}{2} \\ U(\{q\}) = u(q)$$

• Strict set betweenness without self control

Discussion: Optimism

• Say with probability ε won't be tempted so

$$\hat{U}(z) = (1-\varepsilon)U(z) + \varepsilon \max_{p \in z} u(p)$$

- Can lead to violations of set betweenness.
- Let g = gym, j = jog, t = tv

$$\begin{array}{rcl} u(g) &> & u(j) > u(t) \\ v(g) &< & v(j) < v(t) \\ u(j) + v(j) &> & u(t) + v(t) > u(g) + v(g) \end{array}$$

Discussion: Optimism

• For ε small

$$\{t,j\} \succ \{t,g\}$$

as

$$U(\{t, j\}) = u(j) + v(j) - v(t)$$

$$U(\{t, g\}) = u(t)$$

• but

$$\{t, j, g\} \succ \{t, j\}$$

as with probability ε no temptation and will go to the gym

- Consider choice between menus of drinks cocoa or lemonade
- Must choose between menus now, but your choice from those menus will occur on March 1st
- Which would you prefer?

 $\{c\}, \{I\} \text{ or } \{c, I\}?$

• Choice of {c, l} over both {c} and {l} is a violation of set betweenness

Discussion: Preference for Flexibility

- X : set of alternatives
- S : set of states
- $\mu \in \Delta(S)$: probability distribution over states
- $u: X \times S \rightarrow \mathbb{R}$: utility function
 - u(x, s) utility of alternative x in state s
- Preference uncertainty driven by uncertainty about s

Discussion: Preference for Flexibility

- Let A be a menu of alternatives
- Choice from A will take place after the state is known
- Value of A before the state is known given by

$$U(A) = \sum_{s \in S} \mu(s) \max_{x \in A} u(x, s)$$

• U represents choice between menus

Discussion: Preference for Flexibility

• The 'preference uncertainty' model implies a (potentially strict) preference for larger choice sets

$$A \succeq B \Rightarrow A \cup B \succeq A$$

Compare to 'standard' model

$$A \succeq B \Rightarrow A \cup B \sim A$$

And Set Betweenness

$$A \succeq B \Rightarrow A \cup B \preceq A$$

- Preference uncertainty can provide a powerful force that works against a preference for commitment
 - See Amador, Werning and Angeletos [2006]

Discussion: Sophistication

- So far, we have assumed that a DM is sophisticated
 - They understand their second stage choice
 - Implemented by the axiom $x \cup \{p\} \succ x \Leftrightarrow p \vartriangleright q \ \forall \ q \in x$
- What about a DM who is not sophisticated?

• Example 1: A DM who ignores temptation

Object	и	V
Salad	4	0
Fish	2	1
Burger	1	4

- Assume these preferences represent choices that the DM will make from the menu
- But they believe that their choices will be governed by u
- Such a DM will prefer {s, b} to {s}, but when faced with the choice from {s, b} will choose b
- Such a DM will violate sophistication
 - Never exhibit a preference for commitment

• Example 2: A DM who underestimates temptation

Object	и	v	v'
Salad	5	0	0
Fish	2	1	1
Burger	1	9	5

- Assume that a DM has temptation driven by v, but believes that they have temptation driven by v'
- They are offered the chance to buy a 'commitment contract' where they have to pay \$2 if they eat the burger
- Assume that u(2) = 2, v(2) = 2 the *u* of money is additive with *u* of consumption and the *v* of money is additive with the *v* of consumption
- Let b + c be the burger with the commitment contract

Discussion: Sophistication

• Example 2: A DM who underestimates temptation

Object	и	v	<i>v</i> ′
Salad	5	0	0
Fish	2	1	1
Burger	1	9	5
B+C	-1	7	3

The DM will have preferences

$$\{b+c,s\} \succ \{b,s\}$$

as

$$U(\{b+c,s\}) = u(s) + v'(s) - v'(b+c) = 2$$

> 1 = u(b) = U(\{b,s\})

 But the DM will actually choose b + c over s at the second stage as

$$u(b+c) + v(b+c) = 6 > 5 = u(s) + v(s)$$

• Example 2: A DM who underestimates temptation

Object	и	V	v'
Salad	5	0	0
Fish	2	1	1
Burger	1	9	5
B+C	-1	7	3

- End up with lower 'long run' utility
- Also a violation of sophistication as

$$\{b+c,s\} \succ \{b+c\}$$

but b + c will be chosen from the former menu



- Menu preferences allow us to formalize a model of preference for commitment
- We argued that this is a sign that people have problems with temptation
 - Temptation: Preference for Commitment

 $A \succeq B \Rightarrow A \cup B \preceq A$

• Preference uncertainty: Preference for Flexibility

 $A \succeq B \Rightarrow A \cup B \succeq A$

• Compare to 'standard' model

$$A \succeq B \Rightarrow A \cup B \sim A$$

• Gul and Pesendorfer provide a model which allows for both temptation and self control

$$U(x) = \max_{p \in x} \left[u(p) + v(p) \right] - \max_{q \in x} v(q)$$

• Characterized by set betweenness: $x \succeq y \Rightarrow x \succeq x \cup y \succeq y$