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# A fiscal theory of sovereign risk

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### Abstract

Under certain monetary-fiscal regimes the risk of default and thus the emergence of sovereign risk premiums are inevitable. This paper argues that in this context even small differences in the specification of monetary policy can have enormous effects on the equilibrium behavior of default rates and risk premiums. Under some monetary policy rules studied, the conditional expectation of default rates and sovereign risk premiums are constant, so movements in these variables always arrive as a surprise. Under other monetary regimes considered, the equilibrium default rate and the sovereign risk premium are serially correlated and therefore forecastable. The paper also studies the consequences of delaying default. It characterizes environments under which procrastinating on default is counterproductive.

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## 1. Introduction

Certain monetary-fiscal arrangements are incompatible with price stability and government solvency. Consider, for example, the case of a country with a chronic fiscal deficit and an independent central bank. Suppose that the central bank's policy is to peg the price level or the nominal exchange rate. By sticking to its price level target, the consolidated government gives up its ability to inflate away the real value of

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noninterest-bearing nominal public liabilities. Under these circumstances, default on the public debt is inevitable.<sup>1</sup>

Policy regimes of this type under which debt repudiation is under certain states of the world the only possible outcome are not unheard of. A point in case is the Argentine debt crisis of 2001. Between 1991 and early 2002, Argentina pegged the domestic price of tradables to the US counterpart by fixing the peso/dollar exchange rate. Abandoning the exchange-rate peg was never an easy option for the Argentine government. For the peg was instituted by a law of Congress—the 1991 Convertibility Law—which required the enactment of another law to be deactivated. In 2001, in the midst of a prolonged recession, many began to doubt the government's ability to curb fiscal imbalances. These fears placed the country risk premium, measured by the interest-rate differential between Argentine and US dollar-denominated bonds of similar maturities, over 1,800 basis points, among the world's highest at the time. Eventually, the Argentine government defaulted. First on interest obligations, in December of 2001, and shortly thereafter on the principal.

Price level targeting is not the only monetary arrangement under which pressures for default can arise under certain fiscal scenarios. Consider the case of a central bank that aggressively pursues an inflation target by setting the nominal interest rate as an increasing function of inflation with a reaction coefficient larger than unity. This type of policy rule is often referred to as a Taylor rule after John Taylor's (1993) seminal paper. Suppose that, at the same time, the fiscal authority follows an active stance whereby it does not adjust the primary deficit to ensure intertemporal solvency. Under this policy mix, if the government refrains from defaulting, then price stability is in general unattainable. In particular, the equilibrium rate of inflation converges to either plus or minus infinity. Loyo (1999) refers to the latter equilibrium as a 'fiscalist hyperinflation.' Given this monetary-fiscal regime, default is a necessary consequence if price stability is to be preserved. An example of the policy regime described here is given by Brazil. Since mid-1999, the Brazilian central bank has been actively using the interest rate as an instrument to target inflation. Although in recent years fiscal discipline has been enhanced, the Brazilian Treasury is facing serious difficulties implementing additional fiscal reforms necessary to slowdown the rapid growth in public debt. Interestingly, a growing number of observers are beginning to consider a 'unilateral restructuring' of Brazil's public debt as a likely way out of hyperinflation.<sup>2</sup>

The fact that given a particular fiscal policy many different monetary regimes can inevitably be associated with default should not be surprising—for the same reasons why high-fiscal-deficit countries that do not default should be expected to suffer from habitual inflation. A less obvious question is how precisely the equilibrium distributions of default rates and country risk premiums are affected by the particular monetary policy in place. This paper argues that even small differences in the specification of monetary policy can have enormous effects on the equilibrium behavior of default rates and risk premiums.

The analysis is centered around two canonical policy arrangements. Under both environments fiscal policy is assumed to be 'active' in the sense of Leeper (1991). Specifically, real primary surpluses are assumed to be exogenous and random. In one of the policy regimes considered, the central bank pegs the price level. In the other, the monetary authority follows a Taylor-type interest-rate feedback rule.

<sup>&</sup>lt;sup>1</sup>Krugman's (1979) celebrated model of balance of payments crises is an example in which the aforementioned incompatibility is resolved by abandoning the price stability goal.

<sup>&</sup>lt;sup>2</sup>See, for example, the June 29, 2002 issue of *The Economist*.

Our characterization of equilibrium under default reveals that the properties of the equilibrium stochastic process followed by the default rate and the sovereign risk premium depend heavily upon the underlying monetary policy regime. For example, in the Taylor-rule economy, although the government defaults regularly, the expected default rate and the country risk premium are zero. This means that the default rate is unforecastable. By contrast, in the price-targeting economy the equilibrium default rate is serially correlated. Moreover, in this case current and past fiscal deficits predict future default rates.

But even within each of the classes of regimes described above variations in the precise description of the monetary policy can induce dramatic changes in the equilibrium behavior of default rates. For example, if the Taylor rule is assumed to respond to a measure of expected future inflation rather than current inflation, then the inflation target can be attained—i.e., inflationary expectations can be successfully anchored at the target level—without having to default. It is in this sense that we conclude that, the details of monetary policy appear to matter a great deal for default outcomes.

The paper also studies the consequences of delaying default. Understandably, having to default is a situation no policymaker wishes to be involved in. So procrastination is commonplace. Sometimes governments choose to let go of their price stability goal temporarily in the hopes of inflating their way out of default. A natural question, therefore, is what standard general equilibrium models tell us about the consequences of delaying default. We find that substituting a temporary increase in inflation for default is not always possible. Specifically, we identify environments in which postponing the decision to default leads to a hyperinflationary situation that in order to be stopped requires an eventual default of larger dimension than the one that would have taken place had the government not chosen to procrastinate.

The analysis in this paper departs from a large existing literature on sovereign debt in that here the government is assumed to be able to commit to its promises and, given the monetary and fiscal regimes, it always chooses to honor its financial obligations if it can.<sup>3</sup>

Throughout the paper, it is assumed that public debt is nonindexed. In practice, this is typically not the case. A large fraction of emerging market debt in the form of bonds is denominated in foreign currency or stipulates returns tied to some domestic price index. However, in many developing countries a large amount of nonbond government liabilities are not index. Examples of such obligations include social security debt and transfers related to entitlement programs, such as health and unemployment insurance. Moreover, in many of these countries public employment plays the role of a covered source of unemployment insurance. In conjunction these nondollarized, often implicit, public liabilities represent a quantitatively important part of the fiscal revenue associated with inflationary finance. In effect, Burnside et al. (2003), study government finance in the wake of currency crises. They analyze data from three recent episodes: Mexico, 1994; Korea, 1997; and Turkey, 2001. They find that for all three countries debt deflation is a more important source of government income than seignorage. Also, they report that declines in the dollar value of transfers were the single most significant source of government revenue in Mexico and Korea. In any event, introducing indexation does not affect the qualitative results of the paper. But it does introduce quantitative differences. This is because the more

<sup>&</sup>lt;sup>3</sup>The seminal work of Eaton and Gersovitz (1981) initiated a vast literature on sovereign debt with strategic default.

pervasive indexation is, the larger are the price level changes necessary to obtain a given decline in government's total liabilities.<sup>4</sup>

The remainder of the paper is organized in four sections. Section 2 presents the model. Section 3 characterizes the equilibrium behavior of default and sovereign risk when monetary policy takes the form of a Taylor rule. This section also studies the consequences of delaying default. Section 4 studies default and country risk under a price-level peg. Section 5 closes the paper.

## 2. The model

Consider an economy populated by a large number of identical households with preferences described by the utility function

$$\mathbf{E}_t \sum_{t=0}^{\infty} \beta^t U(c_t),\tag{1}$$

where  $c_t$  denotes consumption of a perishable good, U denotes the single-period utility function,  $\beta \in (0, 1)$  denotes the subjective discount factor, and  $E_t$  denotes the mathematical expectation operator conditional on information available in period t. The function U is assumed to be increasing, strictly concave, and continuously differentiable.

Each period, households are endowed with an exogenous and constant amount of perishable goods y and pay real lump-sum taxes in the amount  $\tau_t$ . Households have access to a complete set of nominal state-contingent claims. Specifically, let  $r_{t+1}$  denote the stochastic nominal discount factor such that the price in period t of a random nominal payment  $D_{t+1}$  in period t + 1 is  $E_t r_{t+1} D_{t+1}$ . The flow budget constraint of the household in period t is then given by

$$P_{t}c_{t} + E_{t}r_{t+1}D_{t+1} + P_{t}\tau_{t} \leqslant D_{t} + P_{t}y,$$
(2)

where  $P_t$  denotes the price level. The left-hand side of the budget constraint represents the uses of wealth: consumption spending, purchases of contingent claims, and tax payments. The right-hand side displays the sources of wealth: the payoff of contingent claims acquired in the previous period and the endowment. In addition, the household is subject to the following borrowing constraint that prevents it from engaging in Ponzi schemes:

$$\lim_{j \to \infty} \mathcal{E}_t q_{t+j} D_{t+j} \ge 0, \tag{3}$$

where  $q_t$  is given by

$$q_t = r_1 r_2 \dots r_t,$$

with  $q_0 \equiv 1$ .

The household chooses the set of processes  $\{c_t, D_{t+1}\}_{t=0}^{\infty}$ , so as to maximize (1) subject to (2) and (3), taking as given the set of processes  $\{P_t, r_{t+1}, \tau_t\}_{t=0}^{\infty}$  and the initial condition  $D_0$ . Let the Lagrange multiplier on the period-t budget constraint be  $\beta^t \lambda_t / P_t$ . Then the first-order conditions associated with the household's maximization problem are (2) and (3)

<sup>&</sup>lt;sup>4</sup>Even if the totality of public debt was indexed, changes in the price level would still introduce fiscal effects in the presence of fiat money. In this paper we do away with money for analytical simplicity.

holding with equality and

$$U_c(c_t) = \lambda_t,\tag{4}$$

$$\frac{\lambda_t}{P_t} r_{t+1} = \beta \frac{\lambda_{t+1}}{P_{t+1}}.$$
(5)

The interpretation of these optimality conditions is straightforward. Condition (4) states that the marginal utility of consumption must equal the marginal utility of wealth,  $\lambda_t$ , at all times. Eq. (5) represents a standard pricing equation for one-step-ahead nominal contingent claims. Note that  $E_t r_{t+1}$  is the period-*t* price of an asset that pays one unit of currency in every state of period t + 1. Thus,  $E_t r_{t+1}$  represents the inverse of the gross risk-free nominal interest rate. Formally, letting  $R_t^f$  denote the gross risk-free nominal interest rate between periods t and t + 1, we have

$$R_t^{\rm f} = \frac{1}{\mathrm{E}_t r_{t+1}}.\tag{6}$$

## 2.1. The fiscal authority

The government levies lump-sum taxes,  $\tau_t$ , which are assumed to follow an exogenous, stationary, stochastic process. At some points, for simplicity, we will further specialize the law of motion of  $\tau_t$  to an AR(1) process of the form

$$\tau_t - \bar{\tau} = \rho(\tau_{t-1} - \bar{\tau}) + \varepsilon_t,\tag{7}$$

where  $\bar{\tau}$  denotes the unconditional expectation of  $\tau_t$ , the parameter  $\rho \in [0, 1)$  denotes the serial correlation of  $\tau_t$ , and  $\varepsilon_t \sim N(0, \sigma_{\varepsilon}^2)$  is an i.i.d. random innovation. Alternatively, one could interpret  $\tau_t$  as denoting the primary fiscal surplus.

In period t, the government issues nominal bonds, denoted  $B_t$ , that pay a gross nominal interest rate  $R_t$  in period t + 1. The interest rate  $R_t$  is known in period t. Government bonds are risky assets. For each period the fiscal authority may default on a fraction  $\delta_t$  of its total liabilities. The government's sequential budget constraint is then given by

$$B_t = R_{t-1}B_{t-1}(1-\delta_t) - \tau_t P_t, \quad t \ge 0,$$

with  $R_{-1}B_{-1}$  given. A focal point of our analysis is the characterization of the equilibrium distribution of the default rate  $\delta_t$ .

#### 2.2. Equilibrium

In equilibrium the goods market must clear. That is,

 $c_t = y$ .

The fact that in equilibrium consumption is constant over time implies, by Eq. (4), that the marginal utility of wealth  $\lambda_t$  is also constant. In turn, the constancy of  $\lambda_t$  implies, by Eq. (5), that  $r_{t+1}$  collapses to

$$r_{t+1} = \beta \frac{P_t}{P_{t+1}}.$$

This expression and Eq. (6) then imply that in equilibrium the nominally risk-free interest rate  $R_t^f$  is given by

$$R_{t}^{f} = \beta^{-1} \left[ E_{t} \frac{P_{t}}{P_{t+1}} \right]^{-1}.$$
(8)

Because all households are assumed to be identical, in equilibrium there is no borrowing or lending among them. Thus, all asset holdings by private agents are in the form of government securities. That is,

$$D_t = R_{t-1}B_{t-1}(1-\delta_t),$$

at all dates  $t \ge 0$ .

Optimizing households must be indifferent between holding government bonds and state contingent bonds. This means that the following Euler equation must hold:

$$\lambda_t = \beta R_t \mathbf{E}_t \bigg\{ (1 - \delta_{t+1}) \frac{P_t}{P_{t+1}} \lambda_{t+1} \bigg\}.$$

We are now ready to define an equilibrium.

**Definition 1.** A rational expectations competitive equilibrium is a set of processes  $\{P_t, B_t, R_t, R_t^f, \delta_t\}_{t=0}^{\infty}$  satisfying

$$1 = \beta R_t^{\mathrm{f}} \mathrm{E}_t \frac{P_t}{P_{t+1}}, \quad R_t^{\mathrm{f}} \ge 1,$$
(9)

$$1 = \beta R_t E_t (1 - \delta_{t+1}) \frac{P_t}{P_{t+1}},$$
(10)

$$B_t = R_{t-1}B_{t-1}(1 - \delta_t) - P_t \tau_t,$$
(11)

$$\lim_{j \to \infty} \beta^{t+j+1} \mathbf{E}_t R_{t+j} (1 - \delta_{t+j+1}) \frac{B_{t+j}}{P_{t+j+1}} = 0,$$
(12)

and monetary and fiscal policies to be specified later, given  $R_{-1}B_{-1}$  and the exogenous process for lump-sum taxes  $\{\tau_t\}_{t=0}^{\infty}$ .

Multiplying the left- and right-hand sides of equilibrium condition (11) by  $R_t(1 - \delta_{t+1})$  and iterating forward *j* times one can write

$$R_{t+j}B_{t+j}(1-\delta_{t+j+1}) = \left(\prod_{h=0}^{j} R_{t+h}(1-\delta_{t+h+1})\right)R_{t-1}B_{t-1}(1-\delta_{t})$$
$$-\sum_{h=0}^{j} \left(\prod_{k=h}^{j} R_{t+k}(1-\delta_{t+k+1})\right)P_{t+h}\tau_{t+h}.$$

Dividing both sides by  $P_{t+i}$  one obtains

$$R_{t+j}\frac{B_{t+j}}{P_{t+j+1}}(1-\delta_{t+j+1}) = \left(\prod_{h=0}^{j} R_{t+h}(1-\delta_{t+h+1})\frac{P_{t+h}}{P_{t+h+1}}\right)R_{t-1}\frac{B_{t-1}}{P_{t}}(1-\delta_{t})$$
$$-\sum_{h=0}^{j}\left(\prod_{k=h}^{j} R_{t+k}(1-\delta_{t+k+1})\frac{P_{t+k}}{P_{t+k+1}}\right)\tau_{t+h}.$$

Applying the conditional expectations operator  $E_t$  on both sides of this expression, using the equilibrium condition (10), and applying the law of iterated expectations yields

$$\mathbf{E}_{t}R_{t+j}\frac{B_{t+j}}{P_{t+j+1}}(1-\delta_{t+j+1}) = \beta^{-j-1}R_{t-1}\frac{B_{t-1}}{P_{t}}(1-\delta_{t}) - \sum_{h=0}^{j}\beta^{h-j-1}\mathbf{E}_{t}\tau_{t+h}$$

Now multiplying both sides of this equation by  $\beta^{j}$ , taking the limit for  $j \to \infty$ , and using equilibrium condition (12) one obtains

$$\delta_t = 1 - \frac{\sum_{h=0}^{\infty} \beta^h \mathbf{E}_t \tau_{t+h}}{R_{t-1} B_{t-1} / P_t}, \quad t \ge 0.$$
(13)

This expression, describing the law of motion of the equilibrium default rate, is quite intuitive. It states that the default rate is zero—that is, the government honors its outstanding obligations in the full extent—when the present discounted value of primary surpluses is expected to be equal to the real value of total initial government liabilities. In this case, the government does not need to repudiate its commitments because it is able to raise enough surpluses in the future to pay the interest on its existing real obligations. The government defaults on its debt whenever the present discounted value of primary fiscal surpluses falls short of total real initial liabilities. The extent of the default—i.e., how close  $\delta_t$  is to one—depends on the gap between real government liabilities and the present value of future expected tax receipts. Note that in computing the present discounted value of fiscal surpluses the real risk-free interest rate is applied, which in equilibrium coincides with the inverse of the subjective rate of discount,  $1/\beta$ . In particular, the default rate  $\delta_t$  does not enter in discounting future real fiscal 'cash flows' because in order for the private sector to voluntarily hold public bonds, the expected real return on these assets must be equal to the expected return on real risk-free assets.

If one sets the default rate to zero, Eq. (13) collapses to the central equation of the fiscal theory of price level determination (Cochrane, 1998; Sims, 1994; Woodford, 1994) determining the equilibrium price level  $P_t$ . Inspection of Eq. (13) might lead one to believe that the task of characterizing the equilibrium behavior of the default rate  $\delta_t$  should be a trivial matter if one knows—from the fiscal theory of the price level, say—the equilibrium path of the price level when the default rate is set to zero at all times. That is, letting  $P_t^{\text{FTPL}}$  denote the equilibrium price level when  $\delta_t$  is restricted to be zero for all t, one might conclude that Eq. (13) implies that any path for  $P_t$  and  $\delta_t$  satisfying  $P_t/(1 - \delta_t) = P_t^{\text{FTPL}}$  could be supported as an equilibrium restriction that  $P_t$  and  $\delta_t$  must satisfy. The model features other equilibrium conditions where  $P_t$  and  $\delta_t$  do not enter in the precise way in which they appear in Eq. (13).

Using the AR(1) process assumed for  $\tau_t$  (Eq. (7)), the equilibrium condition (13) becomes

$$\delta_t = 1 - \frac{(1 - \beta)(\tau_t - \bar{\tau}) + (1 - \beta\rho)\bar{\tau}}{R_{t-1}B_{t-1}/P_t(1 - \beta)(1 - \beta\rho)}, \quad t \ge 0.$$
(14)

Intuitively, this expression shows that given the level of initial real government liabilities,  $R_{t-1}B_{t-1}/P_t$ , the more persistent is the tax process—i.e., the larger is  $\rho$ —the larger is the default on public debt triggered by a given decline in current tax revenues.

Neither Eq. (13) nor Eq. (14) represent a full characterization of the equilibrium default rate. For those equations also include the endogenous variable  $P_t$ , whose equilibrium behavior has not yet been worked out. Further analysis is therefore in order.

#### 3. Taylor rules and default

In the past two decades, monetary policy in industrialized countries has taken the form of an interest-rate feedback rule whereby the short-term nominal interest rate is set as a function of inflation and the output gap (Taylor, 1993). Moreover, estimates of this feedback rule feature a slope with respect to inflation that is significantly above unity, typically around 1.5. More recently, a number of developing countries, notably Brazil, have adopted similar active interest-rate rules with the objective of targeting inflation. We therefore wish to consider a monetary regime characterized by a linear feedback rule of the form<sup>5</sup>

$$R_{t} = R^{*} + \alpha \left(\frac{P_{t}}{P_{t-1}} - \pi^{*}\right).$$
(15)

We assume that monetary policy is active in the sense of Leeper (1991). Formally, we assume that  $\alpha\beta > 1$ . Given available estimates for  $\alpha$  and  $\beta$ , this restriction is empirically plausible.

### 3.1. Impossibility of achieving the inflation target without defaulting

Can the government ensure an inflation path equal or close to the target  $\pi^*$  without ever resorting to default? The answer to this question is no. To see why, suppose that the government sets

$$\delta_t = 0, \quad t \ge 0. \tag{16}$$

In this case, the complete set of equilibrium conditions is given by (15) and (16), and the equations contained in Definition 1. Eqs. (13) and (16) imply that  $P_0$  is given by

$$P_0 = \frac{R_{-1}B_{-1}}{\sum_{h=0}^{\infty} \beta^h E_0 \tau_h}.$$

On the right-hand side of this expression, the numerator is predetermined in period 0, and the denominator is exogenously given. This means that in general  $P_0/P_{-1}$  will be different from  $\pi^*$ ; that is, the equilibrium inflation rate in period zero will in general be off target.

 $<sup>^{5}</sup>$ Note that we do not include a term depending on the output gap because in the endowment economy considered here the output gap is nil at all times.

Furthermore, as time goes by, the deviation of inflation from its target level will grow without bounds. Specifically, the equilibrium features either hyperinflation or hyperdeflation. To establish this result, assume for simplicity that taxes are deterministic. Let  $\pi_t \equiv P_t/P_{t-1}$  denote the gross inflation rate in period *t*. Then combining Eqs. (10) and (15) we obtain the following difference equation in  $\pi_t$ :

$$\pi_{t+1} = \alpha \beta \pi_t + (1 - \alpha \beta) \pi^*.$$

In deriving this expression we set  $R^* = \pi^*/\beta$ , to ensure that the inflation target  $\pi^*$  is a steady-state solution to the above difference equation. It follows by the fact that  $\alpha\beta > 1$ , that if  $\pi_0 > \pi^*$  then  $\pi_t \to \infty$ . In this case, the economy embarks on a hyperinflation. Loyo (1999) refers to this equilibrium as a 'fiscalist hyperinflation,' and argues that the monetary/fiscal regime that gives rise to these dynamics was in place in Brazil during the high inflation episode of the early 1980s.

On the other hand, if  $\pi_0 < \pi^*$ , then  $\pi_t \to -\infty$ , and the economy falls into a hyperdeflation. Of course, the inflation rate cannot converge to minus infinity because in that case, according to the linear monetary policy rule (15), the nominal interest rate would reach a negative value in finite time, which is impossible. It can be shown that the zero bound on the nominal interest rate implies that when  $\pi_0 < \pi^*$ , the economy converges to a 'liquidity trap,' characterized by low and possibly negative inflation and low and possibly zero nominal interest rates (Schmitt-Grohé and Uribe, 2000; Benhabib et al., 2001, 2002).

## 3.2. Unforecastability of the default rate

It follows from the preceeding analysis that if the government is to preserve price stability (i.e., if it is to succeed in attaining the inflation target  $\pi^*$ ), then it must default sometimes. It turns out that if  $\delta_t$  is allowed to be different from zero, then the government can indeed ensure a constant rate of inflation equal to  $\pi^*$ . That is, the monetary authority can set

$$\frac{P_t}{P_{t-1}} = \pi^*, \quad t \ge 0.$$
(17)

This expression along with the Taylor rule (15) and the equations listed in Definition 1 represent the complete set of equilibrium conditions. Eqs. (15) and (17) imply that  $R_t = R^* = \pi^*/\beta$  for all  $t \ge 0$ . (We are again assuming that  $R^* = \pi^*/\beta$ .) The Euler Eq. (9) then implies that

$$\mathbf{E}_t \delta_{t+1} = 0, \quad t \ge 0.$$

This means that the equilibrium default rate in effect in period t + 1 is unforecastable in period t. The exact equilibrium process followed by  $\delta_t$  can be obtained with the help of Eq. (13). Evaluating that expression at t = 0, yields

$$\delta_0 = 1 - \frac{\pi^* \sum_{h=0}^{\infty} \beta^h \mathcal{E}_0 \tau_h}{R_{-1} B_{-1} / P_{-1}}.$$
(18)

On the right-hand side of this expression, the numerator is exogenously given, and the denominator is predetermined in period 0. It follows that the above equation fully characterizes the equilibrium default rate in period 0. The default rate is increasing in the

initial level of real government liabilities and decreasing in the expected present discounted value of future primary surpluses.

It is possible to show that in periods t > 0 the equilibrium default rate is given by

$$\delta_t = 1 - \frac{\sum_{h=0}^{\infty} \beta^h \mathbf{E}_t \tau_{t+h}}{\sum_{h=0}^{\infty} \beta^h \mathbf{E}_{t-1} \tau_{t+h}}, \quad t \ge 1$$

This equation states that in any period t > 0, the government defaults when the present discounted value of primary fiscal surpluses is below the value expected for this variable in period t - 1. That is, the government defaults in response to unanticipated deteriorations in expected future tax receipts. Note that the fact that  $\delta_t$  has mean zero implies that sometimes—when  $\delta_t < 0$ —the government subsidizes bond holders. Here, we allow for the variable  $\delta_t$  to take negative values for analytical convenience.<sup>6,7</sup> It is certainly more realistic to impose a nonnegativity constraint on the default rate. In Uribe (2003, Appendix) we impose a nonnegativity constraint on  $\delta_t$  and show how to construct a tax regime that supports a competitive equilibrium with price stability under a Taylor rule.

Because in this economy the inflation rate is constant over time, the Euler Eq. (9) implies that the risk-free nominal interest rate is constant and given by  $R_t^f = \pi^*/\beta$ . The equilibrium value of the rate of return on (risky) government bonds,  $R_t$ , is also given by  $\pi^*/\beta$  (to see this, set  $\pi_t = \pi^*$  in the Taylor rule). Therefore, the gross sovereign risk premium, given by the ratio  $R_t/R_t^f$ , is constant and equal to unity.

#### 3.3. A forward-looking Taylor rule

To illustrate the extent to which the equilibrium behavior of default rates depends upon the specifics of monetary policy, we now consider a variation of the Taylor-type interestrate feedback rule in which the central bank's objective is to anchor inflation expectations as opposed to current inflation. Specifically, we consider the following forward-looking Taylor rule:

$$R_{t} = R^{*} + \alpha \left( \frac{1}{E_{t} P_{t} / P_{t+1}} - \pi^{*} \right), \tag{19}$$

where, as before,  $R^* \equiv \pi^*/\beta$  and  $\alpha\beta > 1$ . This latter parameter restriction implies that the central bank mains an active stance. Note that the argument of the Taylor rule is taken to be  $1/E_t[P_t/P_{t+1}]$  rather than simply  $E_t[P_{t+1}/P_t]$ . The assumed specification allows us to

<sup>&</sup>lt;sup>6</sup>It is straightforward to show that if one departs from the assumption that  $R^* = \pi^*/\beta$  and assumes instead that  $R^* > \pi^*/\beta$ , then an equilibrium in which the inflation rate is always equal to the target  $(\pi_t = \pi^*)$  still exists and  $E_t \delta_{t+1} = 1 - \pi^*/(\beta R^*) > 0$ . The assumption  $R^* > \pi^*/\beta$  could capture a situation in which the government overestimates the real interest rate  $1/\beta$ . Of course, if one assumes that  $R^* < \pi^*/\beta$ , then the conditional expectation of the default rate is negative.

<sup>&</sup>lt;sup>7</sup>In this case, the Taylor rule (15) implies that the equilibrium interest rate is constant and equal to  $R^*$ . In turn, the Euler Eq. (10) implies that the conditional expectation of the default rate in period t + 1 > 0 given information available in t is given by  $E_t \delta_{t+1} = 1 - \pi^* / (\beta R^*) > 0$ . The equilibrium default rate in period 0 is still given by Eq. (18), while the default rate in periods t > 0 is given by  $\delta_t = 1 - (\pi^* / \beta R^*) (\sum_{n=0}^{\infty} \beta^h E_t \tau_{t+n} / \sum_{h=0}^{\infty} \beta^h E_{t-1} \tau_{t+h})$ . Ceteris paribus, the default rate is decreasing in the inflation target  $\pi^*$  and increasing in the interest rate target  $R^*$ . The intuition behind this result is straightforward. The ratio  $R^* / \pi^*$  denotes the real interest rate promised by the government. The higher is this interest rate, the higher is the cost of serving the debt without defaulting.

derive a closed form solution of the model. Both specifications deliver identical equilibrium dynamics up to first order.

Suppose now that the fiscal authority refrains from defaulting at all times, or

 $\delta_t = 0, \quad t \ge 0.$ 

We wish to establish that in equilibrium the central bank achieves its inflation target at all dates. This equilibrium is in sharp contrast to that obtained under the current-looking Taylor rule, which, in general features either a hyperinflation or a hyperdeflation. Combining the restriction  $\delta_t = 0$  for all t, with Eq. (10), and the forward-looking Taylor rule (19) yields

$$R_t = \frac{\pi^*}{\beta}$$

and

$$\frac{1}{\mathrm{E}_t[P_t/P_{t+1}]} = \pi^*$$

Therefore, the central bank attains its target at all times and the nominal interest rate is constant. These two expressions and Eqs. (11) and (13) imply that

$$P_0 = \frac{R_{-1}B_{-1}}{\sum_{h=0}^{\infty} \beta^h \mathcal{E}_0 \tau_h}$$

and

$$\frac{P_t}{P_{t-1}} = \pi^* \frac{\sum_{h=0}^{\infty} \beta^h \mathbf{E}_{t-1} \tau_{t+h}}{\sum_{h=0}^{\infty} \beta^h \mathbf{E}_t \tau_{t+h}}, \quad t \ge 1.$$

According to this formula, deviations of inflation from the target  $\pi^*$  are unforcastable and equal to the innovation in the present discounted value of primary surpluses.

## 3.4. The perils of delaying default: unpleasant default arithmetics

In practice, governments that follow unsustainable policies tend to procrastinate. Only when the economy is clearly embarked on an explosive path, such as a hyperinflation, do governments dare to make hard decisions, such as defaulting or introducing drastic spending cuts.

The focus of this subsection is to show that when a policy mix is incompatible with longrun price stability, unpleasant default arithmetics might arise. Specifically, delaying default may prove counterproductive for two reasons. First, the longer a government waits to default, the higher is the inflation rate the economy is exposed to. Second, the longer is the delay, the higher is the default rate required to stabilize prices. To illustrate this point, consider a perfect-foresight environment. The central bank adheres to the current-looking Taylor rule given in Eq. (15). Suppose that the fiscal authority decides to delay default for T > 0 periods. That is, it sets

$$\delta_t = 0, \quad 0 \leqslant t < T. \tag{20}$$

In period T, the fiscal authority decides to stop procrastinating and defaults in a magnitude sufficient to ensure price stability. Formally, in periods  $t \ge T$  the default rate is set so as to

guarantee that

$$\pi_t = \pi^*, \quad t \ge T. \tag{21}$$

A rational expectations equilibrium is given by Definition 1 and Eqs. (15), (20), and (21). Because the default rate is zero before period T, the Euler Eq. (10) implies that

$$R_t = \beta^{-1} \pi_{t+1}, \quad t \le T - 2.$$
(22)

Combining this expression with the Taylor rule (15) we get  $\pi_{t+1} = \pi^* + \alpha\beta(\pi_t - \pi^*)$  for  $0 \le t \le T - 2$ , where we are assuming that  $R^* \equiv \pi^*/\beta$ . This expression implies the following pre-default time path for inflation:

$$\pi_t = \pi^* + (\alpha \beta)^t (\pi_0 - \pi^*), \quad 0 \le t \le T - 1.$$
(23)

In turn, assuming that  $\tau_t = \bar{\tau}$  for all *t*, Eqs. (13) and (20) imply that the initial inflation rate is exogenously given by  $\pi_0 = R_{-1}B_{-1}(1-\beta)/(P_{-1}\bar{\tau})$ . We are interested in the case in which inherited fiscal imbalances, reflected in a large value of real outstanding initial government liabilities  $(B_{-1}/P_{-1})$ , cause the initial inflation rate to be larger than the central bank's target. That is, we assume that

$$\pi_0 > \pi^*$$
.

This assumption and Eq. (23) show that the longer the government waits to default, i.e., the larger is T, the higher is the inflation rate the public must endure.

In period T-1, the Taylor rule (15) states that  $\beta R_{T-1} = \pi^* + \alpha \beta (\pi_{T-1} - \pi^*)$ . Combining this expression with Eq. (23) yields

$$\beta R_{T-1} = \pi^* + (\alpha \beta)^T (\pi_0 - \pi^*).$$
(24)

Finally, in period T the stabilization policy kicks in, so  $\pi_T = \pi^*$ . The Euler Eq. (10) evaluated at t = T - 1 then implies that  $\delta_T = 1 - \pi^*/(\beta R_{T-1})$ . Combining this expression with Eq. (24) yields the following solution for the default rate in period T:

$$\delta_T = 1 - \frac{\pi^*}{\pi^* + (\alpha \beta)^T (\pi_0 - \pi^*)}$$

This expression shows that the longer the government procrastinates, the larger is the rate of default necessary to bring about price stability. In the limit, as  $T \to \infty$ , the government is forced to default on the entire stock of public debt. Note that the government defaults only once, in period *T*. In periods  $t \ge T$ , the Taylor rule (15) implies that  $R_t = \pi^*/\beta$ , so that, by the Euler Eq. (10),  $\delta_t = 0$ . Summarizing, we have that if the government default for *T* periods, then

$$\lim_{T\to\infty}\pi_{T-1}=\infty,$$

and

$$\lim_{T\to\infty}\delta_T=1.$$

The intuition why a government that procrastinates for too long ends up defaulting on its entire obligations is simple. If the government puts off default for a sufficiently long period of time, the inflation rate in period T - 1 climbs to a level far above its intended target  $\pi^*$ . As a result, the Taylor rule prescribes a very high nominal interest rate in that period. In period T, the inflation rate drops sharply to its target  $\pi^*$ . This means that the 'promised' (i.e., before default) real interest rate on government assets held between periods T - 1 and T, given by  $R_{T-1}/\pi^*$ ,

experiences a drastic hike, generating a severe solvency problem, which the government resolves by defaulting.

Surprisingly, in this economy the stock of real public debt provides no indication of worsening fundamentals as the economy approaches the default crisis. In effect, the stock of public real debt,  $b_t \equiv B_t/P_t$ , remains constant along the entire transition (for a derivation, see Uribe, 2003).

## 4. Price level targeting

We now turn our attention to another example of a monetary regime that, if not coupled with some sort of (intertemporal) balanced budget rule, can make default inevitable. Namely, price level pegs.<sup>8</sup> By pegging the price level, the government gives up its ability to inflate away part of the real value of its liabilities in response to negative fiscal shocks. It is therefore clear that short of endogenous regular fiscal instruments able to offset such exogenous fiscal innovations, default emerges as a necessary outcome. As in the previous section, we are interested in characterizing the equilibrium process of the default rate under these circumstances. It turns out that given the fiscal regime, the equilibrium default rate behaves quite differently under a price level peg than under a Taylor rule.

Formally, the monetary regime we wish to study in this section is given by

$$P_t = 1, \quad t \ge 0. \tag{25}$$

The constancy of the price level implies, by Eq. (9), that the risk-free interest rate is constant and equal to the inverse of the subjective rate of discount. That is,

$$R_t^{\rm f} = \beta^{-1}.\tag{26}$$

We can then formally define an equilibrium as follows:

**Definition 2** (*rational expectations equilibrium under price level targeting*). A rational expectations competitive equilibrium is a set of processes  $\{B_t, R_t, \delta_t\}_{t=0}^{\infty}$  satisfying

$$1 = \beta R_t E_t (1 - \delta_{t+1}), \tag{27}$$

$$B_t = R_{t-1}B_{t-1}(1 - \delta_t) - \tau_t,$$
(28)

$$\lim_{i \to \infty} E_t \beta^{t+j+1} R_{t+j} B_{t+j} (1 - \delta_{t+j+1}) = 0$$

and a fiscal-policy constraint further restricting the behavior of the default rate, given  $R_{-1}B_{-1}$  and the exogenous process for lump-sum taxes  $\{\tau_t\}_{t=0}^{\infty}$ .

### 4.1. The equilibrium stock of public debt

Setting  $P_t = 1$  in Eq. (13), we obtain the following expression for the equilibrium default rate:

$$\delta_t = 1 - \frac{\sum_{h=0}^{\infty} \beta^h \mathcal{E}_t \tau_{t+h}}{R_{t-1} B_{t-1}}.$$
(29)

<sup>&</sup>lt;sup>8</sup>In open economies, governments interested in pegging the price level typically resort to pegging the exchange rate between the domestic currency and that of a low-inflation country.

Because the price level is constant and normalized at one, the denominator on the righthand side,  $R_{t-1}B_{t-1}$ , represents both nominal and real total government liabilities. It will prove convenient to write the above expression using the specific AR(1) process assumed for taxes. This yields

$$\delta_t = 1 - \frac{(1 - \beta)(\tau_t - \bar{\tau}) + (1 - \beta\rho)\bar{\tau}}{R_{t-1}B_{t-1}(1 - \beta)(1 - \beta\rho)}.$$
(30)

To obtain the equilibrium level of public debt, evaluate Eq. (29) at time t + 1 and take expectations conditional on information available at time t. Then use Eq. (27) to eliminate  $E_t \delta_{t+1}$  to get

$$B_t = \sum_{h=1}^{\infty} \beta^h \mathcal{E}_t \tau_{t+h}.$$
(31)

According to this expression, the government's ability to absorb debt is dictated by the expected value of future tax receipts. Note that the level of debt is independent of the magnitude of liabilities assumed by the government in the past,  $R_{t-1}B_{t-1}$ . Under the assumed first-order autorregressive structure of taxes, the above expression becomes

$$B_{t} = \frac{\beta \rho (1 - \beta) (\tau_{t} - \bar{\tau}) + \beta (1 - \beta \rho) \bar{\tau}}{(1 - \beta) (1 - \beta \rho)}.$$
(32)

By this formula, a given decline in current tax revenues obliges the government to engineer a larger cut in public debt the more persistent is the tax process.

## 4.2. Impossibility of pegging the price level without defaulting

Evaluating Eq. (29), which describes the law of motion of the equilibrium default rate, at t = 0, we obtain

$$\delta_0 = 1 - \frac{\sum_{h=0}^{\infty} \beta^h E_0 \tau_h}{R_{-1} B_{-1}}.$$

In period 0, the government cannot affect any of the variables entering the right-hand side of this expression. In effect, taxes are assumed to be exogenous, and initial total public liabilities are pre-determined. Consequently, the government has no control over the initial rate of default  $\delta_0$ . A negative initial tax shock leads inevitably to default. It follows that it is impossible to fix  $\delta_0$  equal to zero.

A natural question is whether the government has the ability to arbitrarily fix the level of the default rate (at zero, say) in all periods following period 0. The answer to this question is no. To see why, assume, contrary to our contention, that the government is capable of setting  $\delta_t$  at a constant level  $\overline{\delta}$  for all t > 0. Then, evaluating (30) at t + 1 we have that  $R_t$  is implicitly given by

$$\bar{\delta} = 1 - \frac{(1-\beta)(\tau_{t+1}-\bar{\tau}) + (1-\beta\rho)\bar{\tau}}{R_t B_t (1-\beta)(1-\beta\rho)}.$$

On the right-hand side,  $\tau_{t+1}$  is measurable with respect to the information set available in period t + 1 and  $B_t$  is measurable with respect to information available in t. It follows that according to the above expression,  $R_t$  is measurable with respect to information available

in t + 1, which is a contradiction, because, by assumption, the government announces  $R_t$  in period t. It follows that the government cannot fix the rate of default for all t > 0.

Although the government is unable to perfectly control the dynamics of the default rate, it can affect it to a limited extent. This is the focus of what follows. We consider three alternative default rules. Under the first rule, the government defaults when the primary fiscal surplus as a fraction of the outstanding public debt falls below a certain threshold. The second default rule assumes that the government repudiates its debt obligations when the fiscal surplus falls below a predetermined acceptable level. These two rules capture the perception among observers that high levels of public debt and economic contraction played a significant role in the recent default rule emphasizes the control of inflationary expectations. It stipulates the use of the default rate as an instrument to ensure a constant nominal interest rate over time. We will establish that although all three of these rules are consistent with the same dynamics for the real value of public debt, rules 1 and 2 induce quite different adjustment in nominal interest rates and default rates from those implied by default rule 3.

## 4.3. Default rule 1

Consider a policy rule whereby in each period t > 0 the government does not default unless the tax-to-debt ratio falls below a certain threshold. Specifically, suppose that the government restricts  $\delta_t$  in the following way:

Default rule 1: 
$$\delta_t \begin{cases} >0 & \text{if } \tau_t / B_{t-1} < \alpha, \\ = 0 & \text{if } \tau_t / B_{t-1} = \alpha, \quad t = 1, 2, \dots, \\ < 0 & \text{if } \tau_t / B_{t-1} > \alpha, \end{cases}$$
 (33)

where the threshold  $\alpha$  is chosen arbitrarily by the fiscal authority. According to the above rule, the government defaults on part of the public debt when the tax-to-debt ratio  $\tau_t/B_{t-1}$  is below the announced threshold  $\alpha$ . This situation takes place in periods of relatively low tax realizations. On the other hand, when the tax-to-debt ratio exceeds the threshold  $\alpha$ , the government chooses to reward bond holders by implementing a subsidy proportional to the size of their portfolios.

A rational expectations equilibrium is given by Eq. (33) and Definition 2. It can be shown that in equilibrium the nominal interest rate is given by

$$R_t = \alpha + \frac{\beta \rho (1-\beta) (\alpha B_t - \bar{\tau}) + \beta (1-\beta \rho) \bar{\tau}}{B_t (1-\beta) (1-\beta \rho)}, \quad t = 0, 1, \dots$$

This expression and Eq. (32), which expresses  $B_t$  as a function of  $\tau_t$  only, jointly describe the equilibrium law of motion of the interest rate as a function of current taxes. Combining the above expression with Eq. (30) to eliminate  $R_t$ , we find that the equilibrium default rate in periods t > 0 is given by

$$\delta_t = 1 - \frac{(1-\beta)(\tau_t - \bar{\tau}) + (1-\beta\rho)\bar{\tau}}{\alpha(1-\beta)(1-\beta\rho)B_{t-1} + \beta\rho(1-\beta)(\alpha B_{t-1} - \bar{\tau}) + \beta(1-\beta\rho)\bar{\tau}}.$$

Fig. 1 depicts with solid lines the model's dynamics under default rule 1. It shows the equilibrium dynamics of taxes, public debt, the interest rate, and the default rate in



Fig. 1. Equilibrium dynamics under alternative default rules.

response to a negative tax innovation. The model is parameterized as follows. The time period is meant to be one quarter. The subjective discount factor  $\beta$  is set equal to 1/(1 + 0.06/4), which implies an annual real (and nominal) interest rate of 6%. Quarterly output, y, is normalized at unity. The initial level of government liabilities,  $R_{-1}B_{-1}$ , is set at 4, implying a debt-to-annual-GDP ratio of one. The average tax rate,  $\bar{\tau}$ , is set at  $(1 - \beta)R_{-1}B_{-1}$ , so that if the tax rate in period zero equals its unconditional expectation  $\bar{\tau}$ , then the equilibrium default rate in that period is zero. The serial correlation of taxes,  $\rho$ , is assumed to be 0.9. Finally, we set the threshold  $\alpha$  equal to  $(1 - \beta)/\beta$ . This value implies that the government chooses to default whenever the tax-to-debt ratio is below its long-run level,  $(1 - \beta)/\beta$ .

In the figure, prior to period 5 taxes are constant and equal to their long-run level  $\bar{\tau}$ . In period 5, the economy experiences a negative tax shock. Specifically, in that period taxes fall 20% below average; that is,  $\varepsilon_5 = -0.2\bar{\tau}$ , or  $\tau_5 = 0.8\bar{\tau}$ . Tax innovations after period 5 are nil (i.e.,  $\varepsilon_t = 0$  for t > 5). Note that the fact that the realizations of the tax innovation are zero in periods other than period 5 ( $\varepsilon_t = 0$  for  $t \neq 5$ ) does not mean that the economy operates under certainty for  $t \neq 5$ . This is because in any period  $t \ge 0$  agents are uncertain about future realizations of  $\varepsilon$ . Between periods 0 and 4, the tax-to-debt ratio is at

its long-run level. As a result, the government honors its obligations in full ( $\delta_t = 0$  for  $t \leq 4$ ). In period 5, in response to the 20% decline in tax revenue, the government defaults on about 2.5% of the public debt. Because the tax-to-debt ratio remains below its long-run level along the entire transition, the government continues to default after period 5. The cumulative default, given by  $\sum_{t=5}^{\infty} \delta_t$ , is about 23%. Before period 5, the interest rate on public debt equals the risk-free rate of 1.5% per quarter, reflecting no default expectations ( $E_t \delta_{t+1} = 0$ ). In period 5, the interest rate on government bonds jumps to 3.6% and then returns monotonically to its steady-state level of 1.5%. The fact that the risk-free interest rate is constant (Eq. (26)) implies that the sovereign risk premium,  $R_t/R_t^f$ , is proportional to  $R_t$ . Thus, a deterioration in fiscal conditions triggers a persistent increase in sovereign risk.

#### 4.4. Default rule 2

As a second example, consider a default rule whereby the government defaults only if the tax rate is below a certain fraction of output. Formally,

Default rule 2: 
$$\delta_t \begin{cases} >0 & \text{if } \tau_t < \alpha y, \\ = 0 & \text{if } \tau_t = \alpha y, \quad t = 1, 2, \dots, \\ <0 & \text{if } \tau_t > \alpha y, \end{cases}$$
 (34)

where  $\alpha$  is a parameter chosen by the government, and y is the constant endowment. The full set of equilibrium conditions is then given by the above rule and the equations listed in Definition 2. It is easy to show that under this rule the interest rate on public debt is given by

$$R_t = \frac{\alpha}{B_t} + \frac{\beta \rho (1-\beta)(\alpha y - \bar{\tau}) + \beta (1-\beta \rho) \bar{\tau}}{B_t (1-\beta)(1-\beta \rho)}, \quad t = 0, 1, \dots$$

Fig. 1displays with broken lines the model's dynamics under default rule 2. The parameterization of the model is identical to that used under default rule 1, except for  $\alpha$ , which is now set equal to  $\overline{\tau}/y$  so as to induce pre-shock dynamics identical to those associated with default rule 1. As in the case of rule 1, we consider an experiment in which taxes fall unexpectedly by 20% in period 5. The dynamics under default rules 1 and 2 are qualitatively identical. The interest rate and the default rate rise in period 5 and then converge monotonically to their respective steady states. However, the convergence is somewhat faster under default rule 1. To see why this is the case, note that in periods t > 5 the tax-to-output ratio  $\tau_t/y$  is relatively further below its steady state level than the tax-to-debt ratio,  $\tau_t/B_{t-1}$ . This is because the stock of public debt adjusts down in response to the tax cut, whereas output remains constant.

#### 4.5. Default rule 3: an interest-rate peg

As a final example, consider the case of a peg of the rate of return on public debt. Specifically, assume that the government sets the interest rate on public debt equal to the risk-free interest rate. That is,

$$R_t = R_t^{\rm f} = \beta^{-1}.\tag{35}$$

According to this policy, the government completely eliminates the sovereign risk premium. In this case the equilibrium is given by Definition 2 and the above rule.

Contrary to what happens under rules 1 and 2, under the interest-rate peg considered here the equilibrium default rate is an iid random variable with mean zero. That is, the default rate is completely unforecastable. To see this, combine the interest-rate rule (35) with the Euler Eq. (27) to get

 $\mathbf{E}_t \delta_{t+1} = \mathbf{0}.$ 

Fig. 1 depicts with dotted lines the model's dynamics under default rule 3. When the negative tax shock takes place (period 5), the default rate jumps up, but immediately returns to zero. Because the magnitude of the jump in the default rate in period 5 is about the same under rules 1 and 3 and because the default rate is serially uncorrelated under rule 3 but highly persistent under rule 1, the cumulative default is much larger under rule 1 than under rule 3. How can this be possible if the initial level of public debt as well as the path of taxes are the same in both economies? The reason is that under rule 3 the interest rate is lower than under rule 1, which makes the post-shock debt burden gross of interest also smaller under rule 3.

## 5. Conclusion

A number of emerging economies have or are facing the need to default. These countries display heterogeneous policy arrangements. A central aim of this paper is to characterize the precise way in which monetary policy affects the equilibrium behavior of default and sovereign risk premiums. We find that monetary policy indeed plays a significant role in shaping the equilibrium distribution of default and risk premiums. For example, in the economy analyzed in Section 3, where the government follows a Taylor-type interest rate feedback rule, price stability requires that the government defaults only by surprise. As a result, the country risk premium is nil at all times even though the fiscal authority reneges of its obligations from time to time. On the other hand, in an economy where the central bank pegs the price level, like the one studied in Section 4, both default and the country risk premium can be highly persistent. But the precise fiscal and monetary regime in place are not the only characteristics of policy behavior that contribute to giving form to the dynamics of default. An equally important role is played by the government's attitude toward making tough decisions. Some governments have a natural tendency to put off as much as possible unavoidable painful measures. This paper shows that in the case of default, procrastination can have unintended consequences. For instance, in the economy where the monetary authority follows a Taylor rule, postponing default leads not only to an explosive inflation path, but also to an eventual default that is larger than the one that would have taken place if the government had not tried to gain time. It is in this sense that we speak of an unpleasant arithmetics in attempting to substitute inflation for default.

The present study can be extended in a number of ways. For the sake of simplicity, the basic analytical framework leaves out a number of important aspects of actual emerging economies that would be worthwhile incorporating. First, it is assumed that the totality of public debt is nonindexed. In reality a significant fraction of government liabilities in developing countries is denominated in foreign currency, which is a form of indexation to a price index of traded goods. Clearly, the more widespread is indexation, the more limited is the ability of unexpected changes in the price level to act as a capital levy. Second, the

model abstracts from a demand for money. Relaxing this assumption would introduce fiscal effects stemming from changes in the price level even if public debt was fully indexed. Finally, the simple model economy we consider is closed to international trade in goods and financial assets. Allowing for international transactions would enrich the analysis in a number of relevant dimensions. Of particular interest is the characterization of default and sovereign risk under alternative exchange rate arrangements and of the role played by foreign investors' holdings of public debt.

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## References

- Benhabib, J., Schmitt-Grohé, S., Uribe, M., 2001. The perils of Taylor rules. Journal of Economic Theory 96, 40–69.
- Benhabib, J., Schmitt-Grohé, S., Uribe, M., 2002. Avoiding liquidity traps. Journal of Political Economy 110, 535–563.
- Burnside, C., Martin, E., Sergio, R., 2003. Government finance in the wake of currency crises. Manuscript, Northwestern University.
- Cochrane, J.H., 1998. A frictionless view of U.S. inflation. National Bureau of Economic Research Macroeconomics Annual 13, 323–384.
- Eaton, J., Gersovitz, M., 1981. Debt with potential repudiation: theoretical and empirical analysis. Review of Economic Studies 48, 289–309.
- Krugman, P.R., 1979. A model of balance of payments crises. Journal of Money, Credit and Banking 11, 311–325.
- Leeper, E., 1991. Equilibria under 'active' and 'passive' monetary and fiscal policies. Journal of Monetary Economics 27, 129–147.
- Loyo, E., 1999. Tight money paradox on the loose: a fiscalist hyperinflation, Manuscript, Harvard University.
- Schmitt-Grohé, S., Uribe, M., 2000. Price level determinacy and monetary policy under a balanced-budget requirement. Journal of Monetary Economics 45, 211–246.
- Sims, C., 1994. A simple model for the study of the determination of the price level and the interaction of monetary and fiscal policy. Economic Theory 4, 381–399.
- Taylor, J.B., 1993. Discretion versus policy rules in practice. Carnegie-Rochester Series on Public Policy 39, 195–214.
- Uribe, M., 2003. A fiscal theory of sovereign risk: expanded version, Manuscript, Duke University.
- Woodford, M., 1994. Monetary policy and price level determinacy in a cash-in-advance economy. Economic Theory 4, 345–380.