slides

chapter 8

Nontradable Goods And

The Real Exchange Rate
Introduction

The **MX** model of Chapter 7 overestimates the role of terms-of-trade shocks as drivers of the business cycles: they explain 20% of the variance of output and other macro indicators in the MX model versus only 10% in an estimated SVAR model.

One possible explanation is that the MX model unrealistically assumes that all goods are internationally traded (either importable or exportable).

In reality, the bulk of goods falls into a third category: nontradables.

Nontradable goods are goods that are exclusively produced and absorbed domestically. Reasons for nontradability include transportation costs and trade barriers.

In this chapter we study open economies with nontradable goods and explore the role of this type of goods in transmitting aggregate disturbances.
The Real Exchange Rate

The real exchange rate, denoted $RER_t$, is the relative price of consumption goods baskets across countries. Formally,

$$RER_t \equiv \frac{\mathcal{E}_t P_t^*}{P_t},$$  \hspace{1cm} (1)

where $P_t^*$ is the nominal price of consumption in the foreign country in units of foreign currency, $P_t$ is the nominal price of consumption in the domestic country in units of domestic currency, and $\mathcal{E}_t$ is the nominal exchange rate, defined as the price of one unit of foreign currency in terms of domestic currency.

- When $RER_t$ increases, the domestic economy becomes cheaper relative to the foreign economy, and we say that the real exchange rate depreciates.

- When $RER_t$ falls, the domestic economy becomes more expensive relative to the foreign economy, and we say that the real exchange rate appreciates.
The TNT Model

The tradable-nontradable (TNT) model is an endowment open economy model with one good that is fully imported (not domestically produced), one good that is fully exported (not domestically consumed), and one nontradable good.

It is a useful structure because it allows us to understand in a simple environment how different disturbances affect the real exchange rate.

The predictions of the TNT model extend to more complex environments, which adds to its theoretical appeal.
The Representative Household

Households are infinitely lived and choose sequences $\{c^m_t, c^n_t, d_{t+1}\}_{t=0}^{\infty}$ to maximize

$$\sum_{t=0}^{\infty} \beta^t U(c_t),$$

subject to

$$c_t = A(c^m_t, c^n_t),$$

$$c^m_t + p^nc^n_t + d_t = \frac{d_t+1}{1+r} + tot_t y^x + p^n_t y^n,$$

$$\lim_{j \to \infty} (1+r)^{-j} d_{t+j} \leq 0,$$

where $c_t$ is consumption; $c^m_t$ and $c^n_t$ are consumption of importables and nontradables, respectively and $A(\cdot, \cdot)$ is increasing, concave, and HD1; $d_t$ is external debt maturing in $t$; $r > 0$ is the interest rate; $tot_t$ is the terms of trade; $y^x$ and $y^n$ are constant endowments of exportables and nontradables, respectively.

Note that $c^m_t$ is fully imported and $y^x$ is fully exported.
Optimality Conditions

The FOCs are the sequential budget constraint and

\[ U'(c_t)A_1(c^m_t, c^n_t) = \lambda_t, \]  

\[ \lambda_t = \beta(1 + r)\lambda_{t+1}, \]  

\[ p^n_t = \frac{A_2(c^m_t, c^n_t)}{A_1(c^m_t, c^n_t)}, \]

\[ \lim_{j \to \infty} (1 + r)^{-j}d_{t+j} = 0. \]

Because \( A(\cdot, \cdot) \) is increasing, HD1, and concave, we can rewrite the optimality condition (4) as

\[ p^n_t = P\left(\frac{c^m_t}{c^n_t}\right); \quad \text{with } P'(\cdot) > 0. \]

This expression is intuitive. It says that if nontradables become more expensive relative to importables, households consume relatively less nontradables and more importables.
The Real Exchange Rate and the Relative Price of Nontradables

In the present model there is a one-to-one relationship between the relative price of nontradables, $p^n_t$, and the real exchange rate, $RER_t$. To see this, divide the numerator and denominator of the RHS of (1) by the nominal price of the importable good, denoted $P^m_t$, to obtain

$$RER_t = \frac{\varepsilon_t P^*_t / P^m_t}{P_t / P^m_t}.$$

Assume that the law of one price holds for importable goods

$$P^m_t = \varepsilon_t P^m_t^*.$$

Then, letting $p^c_t \equiv P_t / P^m_t$ and $p^c_t^* \equiv P^*_t / P^m_t^*$ denote the relative prices of consumption domestically and abroad, we can write $RER_t = p^c_t^* / p^c_t$. Note that $p^c_t^*$ is exogenously determined; assume that it is constant and normalized to unity, $p^c_t^* = 1$. Then we have

$$RER_t = \frac{1}{p^c_t}.$$  \hspace{1cm} (7)

(The argument continues on the next slide.)
It remains to link \( p^c_t \) to \( p^n_t \). To this end, let’s **decentralize the market for final consumption goods**. Firms producing \( c_t, c^m_t \) and \( c^n_t \) to maximize profits

\[
p^c_t A(c^m_t, c^n_t) - c^m_t - p^n_t c^n_t.
\]

The FOC with respect to \( c^m_t \) is

\[
p^c_t A_1(c^m_t, c^n_t) = 1.
\]

Finally, combine this with (6) and (7) to get \( RER_t = A_1 \left( P^{-1}(p^n_t), 1 \right) \).

So we can write

\[
RER_t = e(p^n_t); \quad \text{with } e'(\cdot) < 0.
\]

This expression says that

- The real exchange rate appreciates if and only if the relative price of nontradables increases. And
- The real exchange rate depreciates if and only if the relative price of nontradables decreases.

For this reason, many economists use the terms real exchange rate and relative price of nontradables interchangeably.
Market Clearing

The quintessential property of nontradable goods is that they are produced and consumed domestically:

\[ c^n_t = y^n, \]  

(8)

By contrast, the gap between production and consumption of tradables is bridged by foreign trade in goods and assets:

\[ c^m_t + d_t = \frac{d_{t+1}}{1+r} + tot_t y^x. \]  

(9)
The Equilibrium Real Exchange Rate

Iterating the resource constraint (8) forward ad infinitum and using the transversality condition (5) yields

\[ c^m = -\frac{r}{1 + r}d_0 + \frac{r}{1 + r} \sum_{t=0}^{\infty} \frac{t o t y^x}{(1 + r)^t}. \]  

(10)

Finally, assume that \( \beta(1 + r) = 1 \). Then, (2), (3), and (8) imply that importable consumption is constant, \( c^m_t = c^m \). Thus we can write

\[ p^n = P \left( \frac{c^m}{y^n} \right) \]  

(11)

Taken together, (10) and (11) say that the equilibrium real exchange rate appreciates (i.e., the economy becomes more expensive vis-à-vis the rest of the world) when: (a) The supply of nontradables falls; (b) The current terms of trade improve or the current supply of tradables increases; (c) The terms of trade are expected to improve or the supply of tradables expected to increase in the future.
Adjustment of the Real Exchange Rate to Temporary Terms-of-Trade Shocks

Assume that $\text{tot}_0$ increases, while $\text{tot}_t$ remains unchanged for all $t > 0$. From (10) and (11) we have that

$$\frac{\partial p^m}{\partial \text{tot}}\bigg|_{\text{temporary}} = \frac{r y^x}{1 + r y^n} P' \left( \frac{c^m}{y^n} \right) > 0.$$  

**Intuition:** the increase in the relative price of the exportable endowment creates a positive income effect $\Rightarrow$ households increase their demand for all consumption goods, importables and nontradables. But the supply of nontradables is fixed at $y^n$ $\Rightarrow$ $p^n$ increases to eliminate the excess demand.

Because the relative price of nontradables increases, the real exchange rate, $\text{RER}_t$, appreciates in response to the temporary improvement in the terms of trade (i.e., the domestic economy becomes more expensive relative to the rest of the world).
Adjustment of the Real Exchange Rate to Permanent Terms-of-Trade Shocks

Assume now that $\text{tot}_t$ increases for all $t \geq 0$. Then equilibrium conditions (10) and (11) imply that

$$\left. \frac{\partial p^n}{\partial \text{tot}} \right|_{\text{permanent}} = \frac{y^x}{y^n} P'(\frac{c^m}{y^n}) > 0.$$ 

The intuition is the same as with temporary shocks. However, permanent changes in the terms of trade have a larger effect on the relative price of nontradables than temporary ones

$$\left. \frac{\partial p^n}{\partial \text{tot}} \right|_{\text{permanent}} > \left. \frac{\partial p^n}{\partial \text{tot}} \right|_{\text{temporary}} > 0.$$

**Intuition:** The more permanent is the increase in the terms of trade, the larger the income effect it generates will be, and therefore the larger the increase will be in the desired demand for nontradables, which in turn requires a larger increase in the relative price of nontradables to clear the market.
Adjustment of the Real Exchange Rate to Interest-Rate Shocks

Suppose that at time 0 the interest rate experiences a one-time increase to $r_0 > r$ and then returns to its normal value $r$. It can be shown that this shock causes a contraction in consumption of importables,

$$\frac{\partial c_m^0}{\partial r_0} < 0.$$ 

This is intuitive. When the interest rate is high it is a good time to save more and consume less. This expression together with (6) and (8) implies that

$$\frac{\partial p^n_0}{\partial r_0} = P' \left( \frac{c_m^0}{y^n} \right) \frac{1}{y^n} \frac{\partial c_m^0}{\partial r_0} < 0.$$ 

$\Rightarrow$ the real exchange rate depreciates in response to a temporary increase in the interest rate. Intuitively, households want to consume less of all goods. But because the supply of nontradables is fixed, the price of nontradables must fall to clear the market.
Adjustment of Output to Terms-of-Trade Shocks

Chapter 7 shows that the MX model overestimates the role of TOT shocks as drivers of output movements. Can introducing nontradables ameliorate this problem? Output, denoted $y_t$, is given by

$$y_t = \frac{P_t^x y^x + P_t^n y^n}{P_t} ,$$

where $P_t^x$, $P_t^n$, and $P_t$ denote, respectively, the nominal prices of exportables, nontradables, and final goods. Divide the numerator and denominator by the nominal price of importables to get

$$y_t = \frac{\text{tot}_t y^x + p^n_t y^n}{p^c_t} .$$

Recalling that $p^c_t = 1/A_1(c^m_t, y^n)$ and that $p^n_t = A_2(c^m_t, y^n)/A_1(c^m_t, y^n)$, we can write

$$y_t = A_1(c^m_t, y^n)\text{tot}_t y^x + A_2(c^m_t, y^n)y^n. \quad (12)$$

(The argument continues in the next slide.)
Adjustment of Output to Terms-of-Trade Shocks (continued)

Assume that there is an unexpected permanent increase in the terms of trade in period 0.

Assume that the aggregator function takes the Cobb-Douglas form

\[ A(c^m, y^n) = (c^m)\alpha (y^n)^{1-\alpha}, \] with \( \alpha \in (0, 1) \). Then equation (12) becomes

\[ y_t = c_t \left[ \frac{\alpha \text{tot}_t y^x}{c_t^m} + (1 - \alpha) \right] \]

which implies that

\[ \frac{\partial y_0}{\partial \text{tot}} \bigg|_{1-\alpha=0} = y^x > 0 \quad \text{and} \quad \frac{\partial y_0}{\partial \text{tot}} \bigg|_{1-\alpha=1} = 0, \]

\( \Rightarrow \) as the share of nontradables in total expenditure increases from zero to 100 percent, the output effect of an improvement in the terms of trade falls from a positive value to zero. The relationship between the share of nontradables in consumption and the effect in the terms of trade is in general nonmonotonic.
Empirical Evidence on the Effects of Terms-of-Trade Shocks on the Real Exchange Rate and Aggregate Activity
A Structural Vector Autoregressive (SVAR) Model

- Let $x_t = [\hat{\text{tot}}_t, \hat{\text{tb}}_t, \hat{\text{y}}_t, \hat{\text{c}}_t, \hat{\text{i}}_t, \hat{\text{RER}}_t]'$.

- VAR: $x_t = h_x x_{t-1} + u_t$

- Identification of TOT shocks:
  
  \begin{align*}
  u_t &= \Pi \epsilon_t \\
  \epsilon_t &\sim (0, I) \\
  \Pi_{1,j} &= 0 \text{ for } j = 2, \ldots, 6
  \end{align*}

- ToT process is univariate: $h_{x,1,j} = 0$ for $j = 2, \ldots, 6$

- All variables (except $\text{tb}_t$) are log-quadratically detrended.

- Estimate the SVAR country-by-country using OLS.

- This is the natural extension of the SVAR model of Chapter 7, to include the real exchange rate.
Data:

- Include all poor and emerging countries that have at least 30 consecutive annual observations of output, consumption, investment, net exports, the terms of trade, and the real exchange rate in the World Bank’s WDI database.

- Poor and emerging countries are defined as countries with average PPP-converted GDP per capita in U.S. dollars of 2005 over the period 1990 to 2009 below 25,000 dollars.

- 38 countries satisfy both criteria.
• Sample period: 1980-2011 (32 years).

• Our sample of 38 countries.

\[
\hat{\text{tot}}_t = \rho \hat{\text{tot}}_{t-1} + \sigma_{\text{tot}} \epsilon^\text{tot}_t; \quad \epsilon^\text{tot}_t \sim (0, 1)
\]

Estimate \( \rho \) and \( \sigma_{\text{tot}} \) country by country

<table>
<thead>
<tr>
<th></th>
<th>( \rho )</th>
<th>( \frac{\sigma_{\text{tot}}}{\sqrt{1-\rho^2}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Median</td>
<td>0.52</td>
<td>0.10</td>
</tr>
<tr>
<td>Interquartile Range</td>
<td>[0.41, 0.61]</td>
<td>[0.09, 0.13]</td>
</tr>
</tbody>
</table>
Impulse Response to A 10% Increase in the Terms of Trade
SVAR Evidence, Median across 38 countries

Terms of Trade
Trade Balance
Output
Consumption
Investment
Real Exchange Rate
Observations on the Estimation Results

- TOT shocks are short lived: half-life of TOT shock is just 1 year.

- $R^2$ of tot equations is modest on average, 30 percent.

- The trade balance improves in response to a TOT shock (i.e. the data lends support to the Harberger-Metzler-Laursen (HLM) effect).

- Terms-of-trade improvements are expansionary: On average, a 10% increase in the TOT causes a 0.4% increase in GDP.

- On average, $c$ and $i$ increase, but with a one-year delay. It is puzzling—and indeed an issue worth exploring both empirically and theoretically.

- A TOT improvement leads to an appreciation of the real exchange rate. That is, when $tot_t$ ↑⇒ the country becomes more expensive vis-à-vis the rest of the world. Thus the SVAR model lends support to the predictions of the TNT model.
Share of Variance Explained by Terms of Trade Shocks: SVAR Evidence

<table>
<thead>
<tr>
<th></th>
<th>tot</th>
<th>tb</th>
<th>y</th>
<th>c</th>
<th>i</th>
<th>RER</th>
</tr>
</thead>
<tbody>
<tr>
<td>Median</td>
<td>100</td>
<td>12</td>
<td>10</td>
<td>9</td>
<td>10</td>
<td>14</td>
</tr>
<tr>
<td>Median Absolute Deviation</td>
<td>0</td>
<td>7</td>
<td>7</td>
<td>6</td>
<td>7</td>
<td>11</td>
</tr>
</tbody>
</table>
Country-Level Shares of Variance of Output Explained by Terms of Trade Shocks

Number of Countries

Share of Variance Explained by TOT Shocks (percent)
Summary of Variance Decomposition

- On average, TOT shocks explain 10 percent of the variance of output in poor and emerging countries.

- In only 5 countries (Botswana, Egypt, Cote d’Ivoire, Sudan, and Uruguay) do ToT shocks explain more than 30 percent of the variance of output.

- Thus, the SVAR evidence is at odds with the conventional wisdom according to which ToT shocks account for a large share of output variability in poor and emerging markets.
The MXN Model
Elements of the MXN Model

• small open economy that takes terms of trade as given.

• Three sectors of production: exportable goods, importable goods, nontradable goods ⇒ Natural extension of the MX model to include nontradable sector.

• All goods are produced and consumed (difference with the TNT model).

• All goods are produced using capital and labor.

• Sector specificity of capital and labor.
The Household Problem: Maximize

\[ E_0 \sum_{t=0}^{\infty} \beta^t U(c_t, h_t^m, h_t^x, h_t^n) \]

subject to the period budget constraint

\[ c_t + i_t^m + i_t^x + i_t^n + p_t^r d_t + \Phi_m(k_{t+1}^m - k_t^m) + \Phi_x(k_{t+1}^x - k_t^x) + \Phi_n(k_{t+1}^n - k_t^n) = \frac{p_t^r d_{t+1}}{1+r_t} + w_t^m h_t^m + w_t^x h_t^x + w_t^n h_t^n + u_t^m k_t^m + u_t^x k_t^x + u_t^n k_t^n, \]

and to the laws of motion for physical capital

\[ k_{t+1}^m = (1-\delta)k_t^m + i_t^m; \quad k_{t+1}^x = (1-\delta)k_t^x + i_t^x; \quad k_{t+1}^n = (1-\delta)k_t^n + i_t^n. \]

Notation: \( c_t \) consumption; \( h_t^i, k_t^i, i_t^i, w_t^i, u_t^i \) hours, capital, investment, wages, rental rates of capital in sector \( i = m, x, n \) (importable, exportable, and nontradable sector); \( d_t \) debt due in \( t \); \( p_t^r \) relative price of tradables in terms of final goods. All terms in the budget constraint are expressed in units of final goods. Parameter \( \delta \in (0, 1) \) is the deprecation rate of capital. Functions \( \Phi_j(x) = \frac{\phi_j}{2}x^2; \quad j = m, x, n \) introduce capital adjustment costs.
Firms Producing Final Goods

\[
\max\{a_t - p_t^T a_t^T - p_t^n a_t^n\}
\]

subject to

\[
a_t = \left[ \chi_{\tau} (a_t^T)^{1-\frac{1}{\mu_{\tau n}}} + (1 - \chi_{\tau}) (a_t^n)^{1-\frac{1}{\mu_{\tau n}}} \right]^{\frac{1}{1-\frac{1}{\mu_{\tau n}}}},
\]

Notation:

\(a_t\) = domestic absorption of final goods a.
\(a_t^T\) = domestic absorption of a composite of traded goods.
\(a_t^n\) = (domestic) absorption of nontraded goods.
\(\mu_{\tau n}\) = elasticity of substitution between T and N goods.
\(\chi_{\tau}\) = expenditure share on tradables if \(\mu_{\tau n}\).
Production of the Tradable Composite Good

Firms producing tradable goods solve the problem

$$\max \{ p_t a_t^\tau - p_t^m a_t^m - p_t^x a_t^x \}$$

$$a_t^\tau = \left[ \chi_m (a_t^m)^{1 - \frac{1}{\mu_{mx}}} + (1 - \chi_m) (a_t^x)^{1 - \frac{1}{\mu_{mx}}} \right]^{1 - \frac{1}{\mu_{mx}}}$$

Notation:

- $a_t^\tau$ = domestic absorption of tradable goods.
- $a_t^m$ = domestic absorption of importable goods.
- $a_t^x$ = domestic absorption exportable goods.
- $\mu_{mx}$ = elasticity of substitution between importables and exportables.
- $\chi_m$ = expenditure share if $\mu_{mx} = 1.$
Production of Importable Goods

Firms producing importable goods solve the problem

$$\max \{ p_t^m y_t^m - w_t^m h_t^m - u_t^m k_t^m \}$$

subject to the production technology

$$y_t^m = A^m (k_t^m)^{\alpha_m} (h_t^m)^{1-\alpha_m}$$

Notation:

- $y_t^m =$ quantity of importable goods produced domestically.
- $A^m =$ level of productivity in the importable sector.
- $k_t^m =$ capital input in the importable sector.
- $h_t^m =$ labor input in the importable sector.
- $w_t^m =$ wage rate in the importable sector.
- $u_t^m =$ rental rate of capital in the importable sector.
- $1 - \alpha_m =$ labor share in the importable sector.
Production of Exportable Goods

Firms producing exportable goods solve the problem

$$\max \{ p_t^x y_t^x - w_t^x h_t^x - u_t^x k_t^x \}$$

subject to the production technology

$$y_t^x = A^x (k_t^x)^{\alpha^x} (h_t^x)^{1-\alpha^x}$$

Notation:

- $y_t^x =$ quantity of exportable goods produced.
- $A^x =$ level of productivity in the exportable sector.
- $k_t^x =$ capital input in the exportable sector.
- $h_t^x =$ labor input in the exportable sector.
- $w_t^x =$ wage rate in the exportable sector.
- $u_t^x =$ rental rate of capital in the exportable sector.
- $1 - \alpha^x =$ labor share in the exportable sector.
Production of Nontradable Goods

Firms producing nontradable goods solve the problem

$$\max \{ p_t^n y^n_t - w^n_t h^n_t - u^n_t k^n_t \}$$

subject to the production technology

$$y^n_t = A^n (k^n_t)^{\alpha_n} (h^n_t)^{1-\alpha_n}$$

$y^n_t$ = quantity of nontraded goods produced.
$A^n$ = level of productivity in the nontradable sector.
$k^n_t$ = capital input in the nontradable sector.
$h^n_t$ = labor input in the nontradable sector.
$w^n_t$ = wage rate in the nontradable sector.
$u^n_t$ = rental rate of capital in the nontradable sector.
$1 - \alpha_n$ = labor share in the nontraded sector.
Debt Elastic Interest-Rate Premium

To ensure a stationary equilibrium process for external debt, we assume that the country interest-rate premium is debt elastic,

\[ r_t = r^* + p(d_{t+1}) \]

where \( p(\cdot) \) is assumed to be increasing taking the form

\[ p(d) = \psi (e^{d-\bar{d}} - 1) \]
The Terms of Trade Process

As in the empirical SVAR analysis, we assume that the terms of trade follow a univariate first-order autoregressive (AR(1)) process of the form

\[
\ln \left( \frac{\text{tot}_t}{\text{tot}} \right) = \rho \ln \left( \frac{\text{tot}_{t-1}}{\text{tot}} \right) + \sigma_{\text{tot}} \epsilon_{t, \text{tot}}, \quad \epsilon_{t, \text{tot}} \sim (0, 1)
\]

where \( \text{tot} > 0 \) is the deterministic level of the terms of trade. \( \rho \in (-1, 1) \) is the serial correlation. \( \sigma_{\text{tot}} > 0 \) is the standard deviation of the innovation to the terms of trade.
Calibrated and Estimated Parameters

<table>
<thead>
<tr>
<th>Calibrated Structural Parameters</th>
<th>ρ</th>
<th>σ_{tot}</th>
<th>α_m, α_x</th>
<th>α_n</th>
<th>ω_m, ω_x, ω_n</th>
<th>μ_{mx}</th>
<th>μ_{τn}</th>
<th>μ_{tot}</th>
<th>A^m, A^n</th>
<th>β</th>
<th>σ</th>
<th>δ</th>
<th>r^*</th>
</tr>
</thead>
<tbody>
<tr>
<td>*</td>
<td>*</td>
<td>0.35</td>
<td>0.25</td>
<td>1.455</td>
<td>1</td>
<td>0.5</td>
<td>1</td>
<td>1</td>
<td>1/(1 + r^*)</td>
<td>2</td>
<td>0.1</td>
<td>0.11</td>
<td></td>
</tr>
</tbody>
</table>

Moment Restrictions

<table>
<thead>
<tr>
<th>Moment Restrictions</th>
<th>σ_{i}</th>
<th>σ_{tb}</th>
<th>σ_{im+ix}</th>
<th>s_n</th>
<th>s_x</th>
<th>s_{tb}</th>
<th>\frac{p^m y^m}{p^x y^x}</th>
</tr>
</thead>
<tbody>
<tr>
<td>*</td>
<td>*</td>
<td>1.5</td>
<td>0.5</td>
<td>0.2</td>
<td>0.01</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

Implied Structural Parameter Values

<table>
<thead>
<tr>
<th>Implied Structural Parameter Values</th>
<th>φ_m</th>
<th>φ_x</th>
<th>φ_n</th>
<th>ψ</th>
<th>χ_m</th>
<th>χ_τ</th>
<th>\overline{d}</th>
<th>A^x</th>
<th>β</th>
</tr>
</thead>
<tbody>
<tr>
<td>*</td>
<td>*</td>
<td>*</td>
<td>*</td>
<td>0.8980</td>
<td>0.4360</td>
<td>0.0078</td>
<td>1</td>
<td>0.9009</td>
<td></td>
</tr>
</tbody>
</table>

Notes.

*Country-specific estimates.

\frac{σ_i}{σ_y} and \frac{σ_{tb}}{σ_y} are conditional on tot shocks

s_n \equiv p^n y^n / y,

s_x \equiv x / y,

s_{tb} \equiv (x - m) / y, where y \equiv p^m y^m + p^x y^x + p^n y^n.
Key parameters determining the importance of terms of trade shocks:

- $\rho$ and $\sigma_{tot}$, the more volatile and the more persistent are terms of trade shocks, the more volatile is output.

- The size of the nontraded sector: $\frac{p^n y^n}{y} (= 50\%)$. The larger the nontraded sector, the smaller the output effects of tot shocks.

- The steady-state trade share: $\frac{x+m}{y} (= 39\%)$. The larger the trade share, the larger the output effects of tot shocks.
Estimate capital adjustment cost parameters and the debt elasticity of the interest rate, $\phi_m, \phi_x, \phi_n, \psi, \chi_m$, to match country-by-country the relative standard deviations

$$\frac{\sigma_i}{\sigma_y} \quad \text{and} \quad \frac{\sigma_{tb}}{\sigma_y}$$

conditional on terms of trade shocks and $\frac{\sigma_{ix+i_m}}{\sigma_{i_n}} = 1.5$. 
Medians of Country-Specific Estimates of the Capital Adjustment Cost Parameters and the Debt Elasticity of the Interest Rate

<table>
<thead>
<tr>
<th></th>
<th>$\phi_m$</th>
<th>$\phi_x$</th>
<th>$\phi_n$</th>
<th>$\psi$</th>
<th>$\sigma_i/\sigma_y$</th>
<th>$\sigma_{tb}/\sigma_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Median</td>
<td>1.13</td>
<td>1.40</td>
<td>0.69</td>
<td>0.84</td>
<td>3.36</td>
<td>3.00</td>
</tr>
<tr>
<td>MAD</td>
<td>1.13</td>
<td>1.40</td>
<td>0.69</td>
<td>0.77</td>
<td>1.42</td>
<td>0.52</td>
</tr>
</tbody>
</table>

Data Model
Median of Country-Specific Impulse Response to a Ten-Percent Terms-of-Trade Shock Predicted by the MXN Model
Observations on Impulse Responses to a Terms-of-Trade Shock Implied by the MXN Model

- *Substitution effect of an increase in $\text{tot}_t$ on supply side:* Firms produce more exportables and less importables, and, given $p^n_t$, would produce less nontradables.

- *Substitution effect of an increase in $\text{tot}_t$ on demand side:* Demand for importable goods and nontraded goods rises, domestic demand for exportable goods falls. The improvement in the terms of trade generates a positive wealth effect increasing the demand for all goods.

- The price of nontradables, $p^n_t$, rises and the real exchange rate appreciates.

- Both exports and imports increase. Net effect on trade balance turns out to be positive. Thus model impulse response is consistent with Harberger-Laursen-Metzler effect.

- Aggregate investment increases by less than 10% on impact. But investment in the exportable sector rises by 61% while in decreases by over 40% in the importable sector.
Comparison of SVAR and MXN Model

Proper comparison of empirical and theoretical models requires measuring macroeconomic indicators \((y_t, c_t, i_t, tb_t)\) in the same units.

To this end, we construct the theoretical counterpart to the observable variable ‘GDP at constant LCU’ used in the SVAR analysis. This requires deflating nominal variables by a Paasche GDP deflator index. This yields

\[
y_{t \text{ constant prices}} = p_{ss}^x y_{t}^x + p_{ss}^m y_{t}^m + p_{ss}^n y_{t}^n,
\]

Similarly, to obtain total consumption expenditure at constant prices, we must divide \(c_t\) by the factor \(\frac{p_{ss}^x y_{t}^x + p_{ss}^m y_{t}^m + p_{ss}^n y_{t}^n}{p_{ss} y_{t}^x + p_{ss} y_{t}^m + p_{ss} y_{t}^n}\), which yields

\[
c_{t \text{ constant prices}} = \frac{c_t p_{ss}^x y_{t}^x + p_{ss}^m y_{t}^m + p_{ss}^n y_{t}^n}{p_{ss}^x y_{t}^x + p_{ss}^m y_{t}^m + p_{ss}^n y_{t}^n},
\]

Similar expressions obtain for the observable versions of \(i_t\) and \(tb_t\).
Share of Variances of Output and Other Indicators Explained by Terms-of-Trade Shocks According to the MXN Model

To compute the share of the variance of output explained by TOT shocks in the MXN model, we proceed as follows:

(1) With \( \text{tot}_t \) as the sole driving process, compute the variance of output predicted by the MXN model.

(2) Divide this value obtained in (1) by the observed unconditional variance of output predicted by the SVAR model (i.e., the variance of output when all shocks in the SVAR are active).

We do the same with the other macroeconomic indicators of interest (consumption, investment, the trade balance, and the real exchange rate).
Share of Variance Explained by Terms of Trade Shocks: 
SVAR Versus MXN Predictions

<table>
<thead>
<tr>
<th></th>
<th>$tb$</th>
<th>$y$</th>
<th>$c$</th>
<th>$i$</th>
<th>$RER$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MXN Model</td>
<td>21</td>
<td>13</td>
<td>18</td>
<td>11</td>
<td>1</td>
</tr>
<tr>
<td>SVAR Model</td>
<td>12</td>
<td>10</td>
<td>9</td>
<td>10</td>
<td>14</td>
</tr>
</tbody>
</table>

Note. Cross-country medians.

Finding:
• The median share of the variance of output explained by total shocks, according to the MXN model is close to the one predicted by the SVAR model (13 vs. 10 percent).
• Thus both the MXN and SVAR models concur in that, contrary to the conventional wisdom, terms-of-trade shocks are not a major driver of the business cycle.
• This result extends to the other macroeconomic indicators included in the SVAR, although the MXN model overestimates the role of TOT shocks for the trade balance and consumption and underestimates it for the real exchange rate.
The Importance of Measuring Variables Consistently in the SVAR and MXN Models

One possible reason for the discrepancy between our findings of a small role for TOT shocks as drivers of the business cycle and the conventional view that assigns them a major role is measurement.

Suppose that in computing the predictions of the MXN model for the importance of TOT shocks, we had measured output in units of current consumption \((p_t^x y_t^x + p_t^m y_t^m + p_t^n y_t^n)\)—a common practice—instead of at constant prices using a Paasche price deflator \((p_{ss}^x y_{ss}^x + p_{ss}^m y_{ss}^m + p_{ss}^n y_{ss}^n)\).

Let \(x_t^{CPI}\) denote variable \(x_t\) measured in units of consumption.

Let \(x_t^{YPI}\) denote variable \(x_t\) measured in units of output.

<table>
<thead>
<tr>
<th>Ratio of Variances Predicted by Theoretical Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\frac{\text{var}(x_t^{CPI})}{\text{var}(x_t^{YPI})})</td>
</tr>
<tr>
<td>-----------------------------------------------</td>
</tr>
<tr>
<td>(2.4)</td>
</tr>
</tbody>
</table>

- Predicted variances due to ToT shocks of output, consumption, and investment are **larger** when these aggregates are expressed in units of consumption goods as opposed to units of output.
The Terms-of-Trade Disconnect

The table in slide slide 43 conveys the impression that the MXN and SVAR model speak with the same voice with respect to the importance of terms-of-trade shocks for aggregate movements in output.

This is certainly the case on average across the 38 countries in the panel. However, the picture that emerges when one looks at the predictions of the MXN and SVAR models at the country level is quite different.

This is the point of the graphs on the next slide.
Evaluating The Conventional Wisdom
How Does the Model Fit Country-Level Data?

Graph showing the relationship between the SVAR model and the MXN model for various countries.
Observations on the Figure

- If the MXN model were to fit the data well, all circles in the figure would line up close to the 45-degree line.

- The cloud of circles, however, displays no discernible pattern.

- Thus although the predictions of the MXN model are in line with the SVAR model on average across countries, the match is quite poor when we look at countries individually.

- This result extends to the other macroeconomic indicators included in the SVAR model, as the figure in the next slides shows.
Variance of Consumption, Investment, the Trade Balance, and the Real Exchange Rate

Explained By Terms-of-Trade Shocks: SVAR Versus Model
Conclusions: Empirical Analysis

1. Conventional wisdom has it that terms of trade shocks represent a major source of fluctuations for emerging countries.

2. Using SVAR analysis, we have found a modest role for TOT shocks.

3. Does this mean that world prices are not important transmitters of aggregate disturbances? No. It simply indicates that ToT shocks, being a highly aggregated summary of world prices faced by a country, might be a poor way of capturing the mechanism through which external shocks transmit to the domestic economy.

4. The typical country trades internationally in a large number of goods and services. Thus, world shocks are likely to be transmitted through a large number of world prices. Using a single summary statistic, such as the terms of trade, may not capture all of the domestic effect of external disturbance.

5. The above observations suggest using more disaggregated world price data. Fernández, Schmitt-Grohé, and Uribe (JIE, forthcoming) follow this route. They estimate a variation of the SVAR model studied here in which the terms of trade is replaced by 3 world commodity prices. They find that jointly, these prices explain about 30 percent of aggregate fluctuations in emerging and poor countries.
Conclusions: Theoretical Analysis

1. The analysis suggests that the theoretical framework on which the conventional wisdom is based, a multi-sector, open economy version of the RBC model, which we called the MXN model, captures well the transmission mechanism of TOT shocks on average, but does a poor job at the country level.

2. One promising avenue is to expand the MXN model to allow for multiple importable and exportable goods (as opposed to just one importable and one exportable good). In this setting, just as in the empirical analysis, the terms of trade will not suffice to capture the whole mechanism through which world shocks transmit to the domestic economy.

3. An important byproduct of the theoretical analysis presented in this chapter (as well as in Chapter 7) is the need to be careful about measuring variables in the same units in the theoretical and the empirical models. Failing to do so can lead to spurious differences between the predictions of the theoretical model and the data.