

# **Pricing to Habits and the Law of One Price**

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## **Stylized facts we wish to address**

- The Law Of One Price fails at the good-by-good level even for highly traded goods.
  - Goldberg and Knetter, *JEL* 1997.
  - Crucini and Shintani, 2006.
- A rise in government spending leads to
  - A real exchange rate depreciation.
  - An increase in private consumption.
  - A trade balance deterioration.

(Ravn, Schmitt-Grohé, and Uribe, 2007; Monacelli and Perotti, 2006; Perotti, 2006; Gali et al., 2006)

- Estimation of empirical impulse responses
  1. Use structural VAR to estimate effects of government purchases shocks.

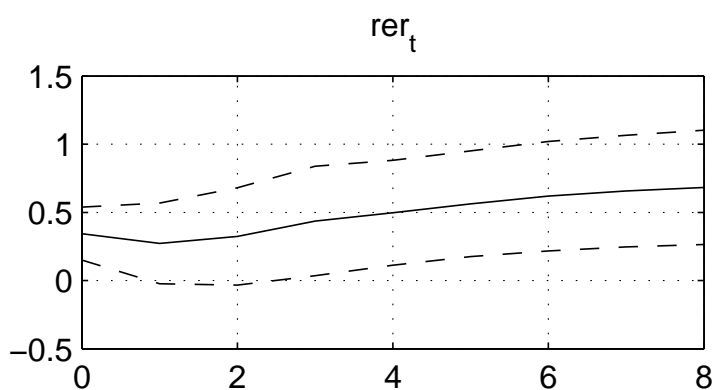
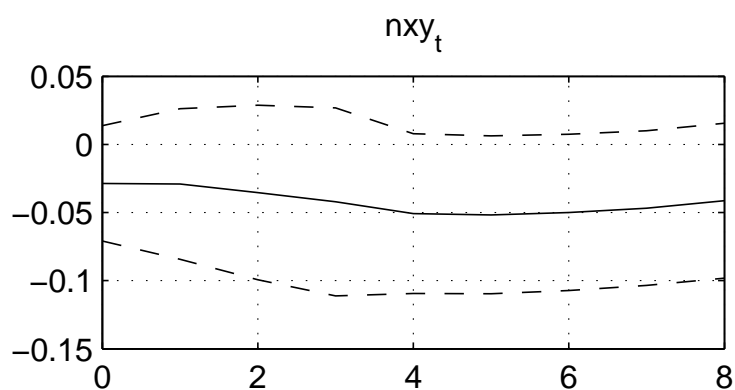
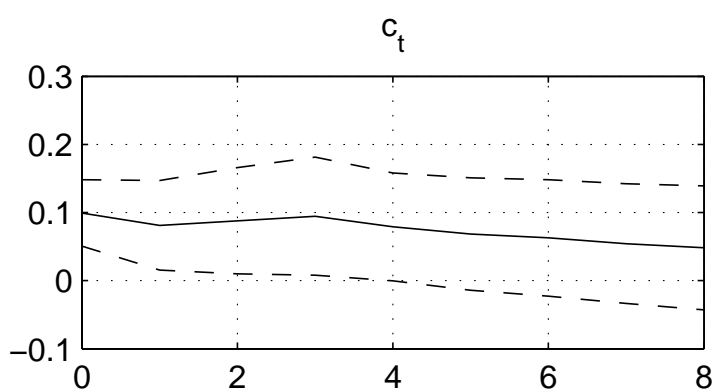
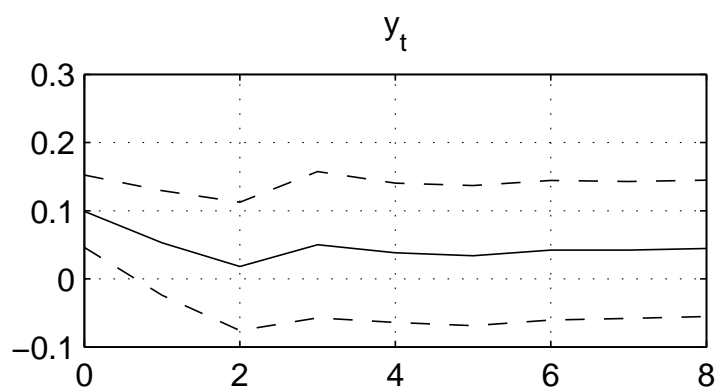
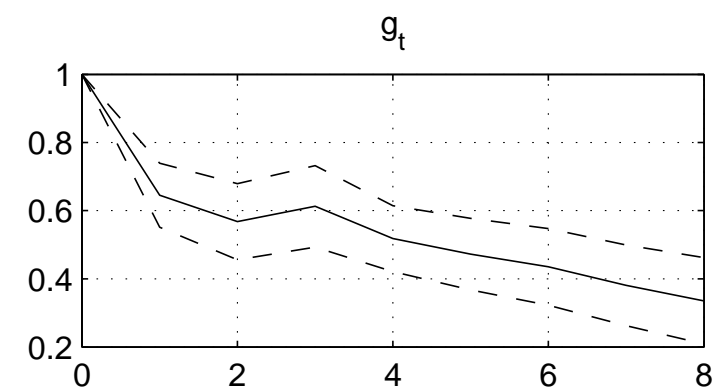
$$AX_t = B(L)X_{t-1} + u_t$$

where

$$X_t = \begin{bmatrix} \log g_t \\ \log y_t \\ \log c_t \\ \frac{tb_t}{y_t} \\ \log e_t \end{bmatrix}$$

2. Four lags ( $L = 4$ ).
3. Identification: government spending is not affected by structural innovations to any other variable than government spending itself.
4. Panel of Countries: Australia, Canada, U.K., and U.S.
5. Sample: Quarterly data from 1975 to 2005

# Estimated Impulse Response Functions To A Unit Innovation in Domestic Government Purchases



Solid lines: point estimate

Dashed lines: point estimate  $\pm 2$  std

# Theory

- We abstract from:
  - Nontraded goods.
  - Rule-of-thumb consumers.
  - Distribution costs.
  - Sticky prices or wages.
  - Incomplete asset markets.
  - Tariffs or quotas.
  - Nonseparabilities of preferences across consumption and leisure.

## A Model of Pricing to Habits

- Two-country production economy without capital.
- Preferences

$$E_0 \sum_{t=0}^{\infty} \beta^t [\phi \ln(x_t) + (1 - \phi) \ln(1 - h_t)]$$

- Two traded goods:  $a$  and  $b$

$$x_t = \left[ \omega x_{a,t}^c{}^{1-\frac{1}{\xi}} + (1 - \omega) x_{b,t}^c{}^{1-\frac{1}{\xi}} \right]^{\frac{1}{1-\frac{1}{\xi}}}$$

- External deep habits

as in Ravn, Schmitt-Grohé, and Uribe (*RES*, 2006)

- Private Households

Habit-adjusted consumption of good  $a$

$$x_{a,t}^c = \left[ \int_0^1 (c_{i,a,t} - \theta^c s_{i,a,t-1}^c)^{1-\frac{1}{\eta}} di \right]^{\frac{1}{1-\frac{1}{\eta}}}$$

$$s_{i,a,t}^c = \rho s_{i,a,t-1}^c + (1 - \rho) \tilde{c}_{i,a,t}$$

Habit-adjusted consumption of good  $b$

$$x_{b,t}^c = \left[ \int_0^1 (c_{i,b,t} - \theta^c s_{i,b,t-1}^c)^{1-\frac{1}{\eta}} di \right]^{\frac{1}{1-\frac{1}{\eta}}}$$

$$s_{i,b,t}^c = \rho s_{i,b,t-1}^c + (1 - \rho) \tilde{c}_{i,b,t}$$

- Public sector

$$x_{a,t}^g = \left[ \int_0^1 (g_{i,a,t} - \theta^g s_{i,a,t-1}^g)^{1-\frac{1}{\eta}} di \right]^{\frac{1}{1-\frac{1}{\eta}}}$$

$$x_{b,t}^g = \left[ \int_0^1 (g_{i,b,t} - \theta^g s_{i,b,t-1}^g)^{1-\frac{1}{\eta}} di \right]^{\frac{1}{1-\frac{1}{\eta}}}$$

- Domestic Demand for good  $a$

$$d_{i,a,t} = \left( \frac{P_{i,a,t}}{P_{a,t}} \right)^{-\eta} x_{a,t} + \theta s_{i,a,t-1}$$

$$\text{Price elasticity} = -\eta \left( 1 - \theta \frac{s_{i,a,t-1}}{d_{i,a,t}} \right)$$

- Foreign Demand for good  $a$

$$d_{i,a,t}^* = \left( \frac{P_{i,a,t}^*}{P_{a,t}^*} \right)^{-\eta} x_{a,t}^* + \theta s_{i,a,t-1}^*$$

$$\text{Price elasticity} = -\eta \left( 1 - \theta \frac{s_{i,a,t-1}^*}{d_{i,a,t}^*} \right)$$



# Firms

- Firms can price discriminate internationally.
- Production Function:

$$y_{i,a,t} = h_{i,a,t}$$

- Optimal pricing

$$P_{a,t} = \left[ 1 - \frac{1}{\eta \left( 1 - \theta \frac{d_{a,t-1}}{d_{a,t}} \right)} + \theta \Omega_{a,t} \right]^{-1} MC_t$$

$$P_{a,t}^* = \left[ 1 - \frac{1}{\eta \left( 1 - \theta \frac{d_{a,t-1}^*}{d_{a,t}^*} \right)} + \theta \Omega_{a,t}^* \right]^{-1} MC_t$$

$\Rightarrow$  Time-varying deviation from the Law of One Price ( $P_{a,t}^*/P_{a,t} \neq 1$  and moves over time).

## Calibration

Parameter	Value	Description
$\beta$	0.99	Subjective discount factor (quarterly)
$\sigma$	1	Intertemporal elasticity of substitution
$\phi$	0.15	Preference parameter
$\omega$	0.5	Preference parameter
$\xi$	1.5	Elasticity of substitution composite
$\eta$	5	Elasticity of substitution varieties
$s_g, s_g^*$	0.2	Government shares

# Estimation

- Goal: Estimate deep-habit parameters:

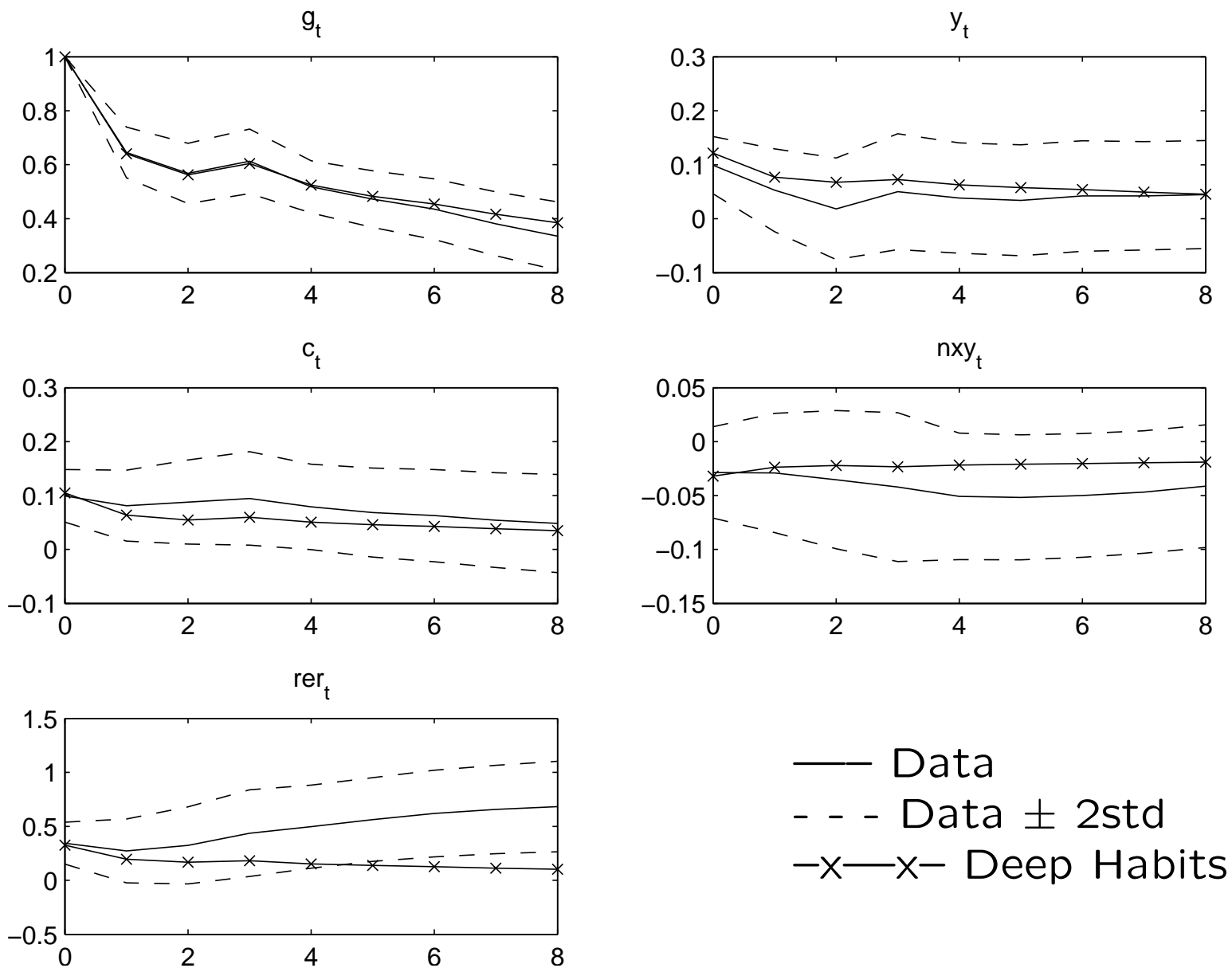
$$\Theta \equiv [\theta^c \quad \theta^g \quad \rho]$$

- Strategy: Pick  $\Theta$  to minimize the distance between empirical and theoretical impulse responses.
- Match 9 quarters of impulse responses of five variables.

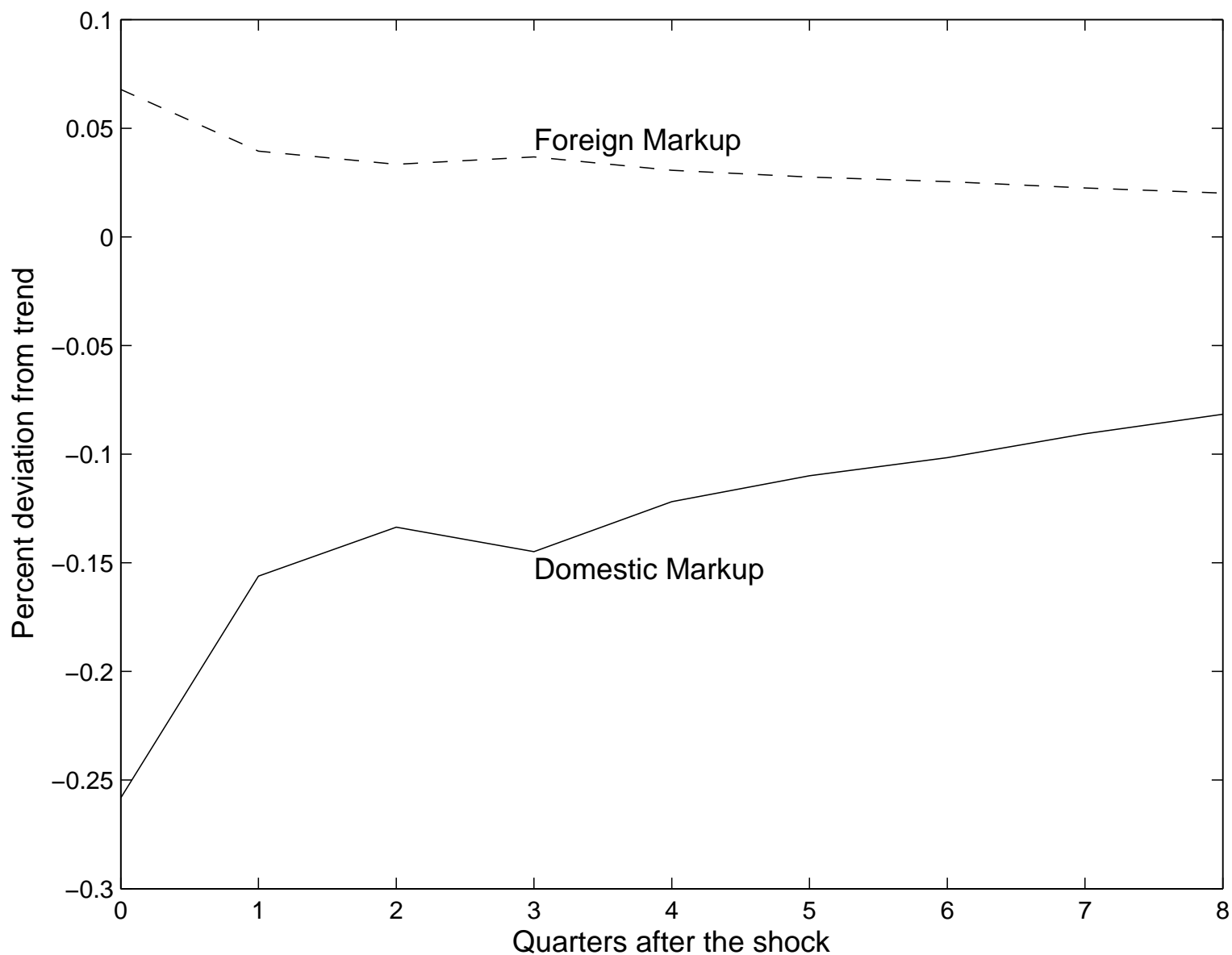
## Estimated Parameters

Parameter	Point Estimate	Standard Deviation
$\theta^c$	0.52	0.08
$\theta^g$	0.57	0.15
$\rho$	0.99	0.03

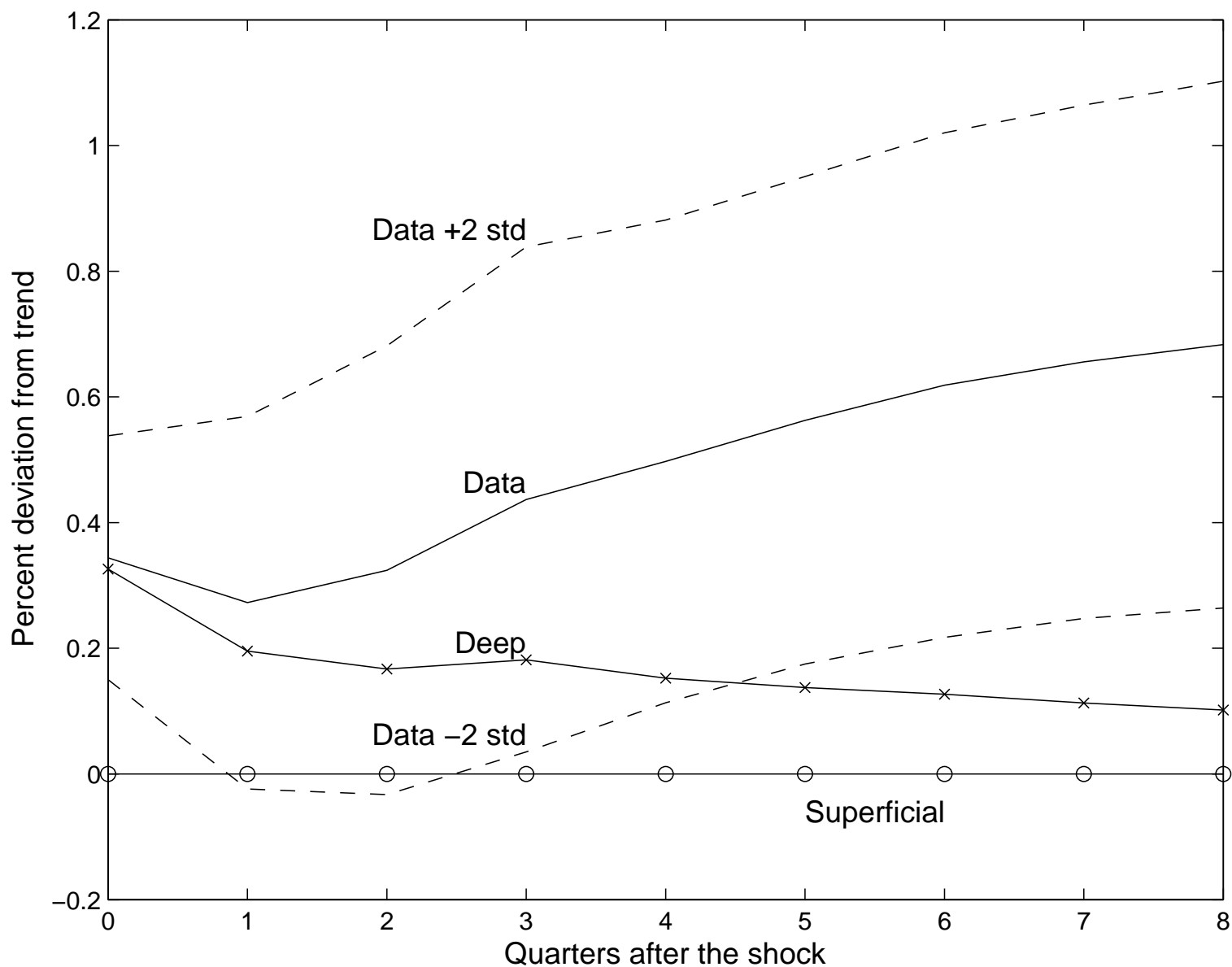
# Predicted and Estimated Impulse Responses



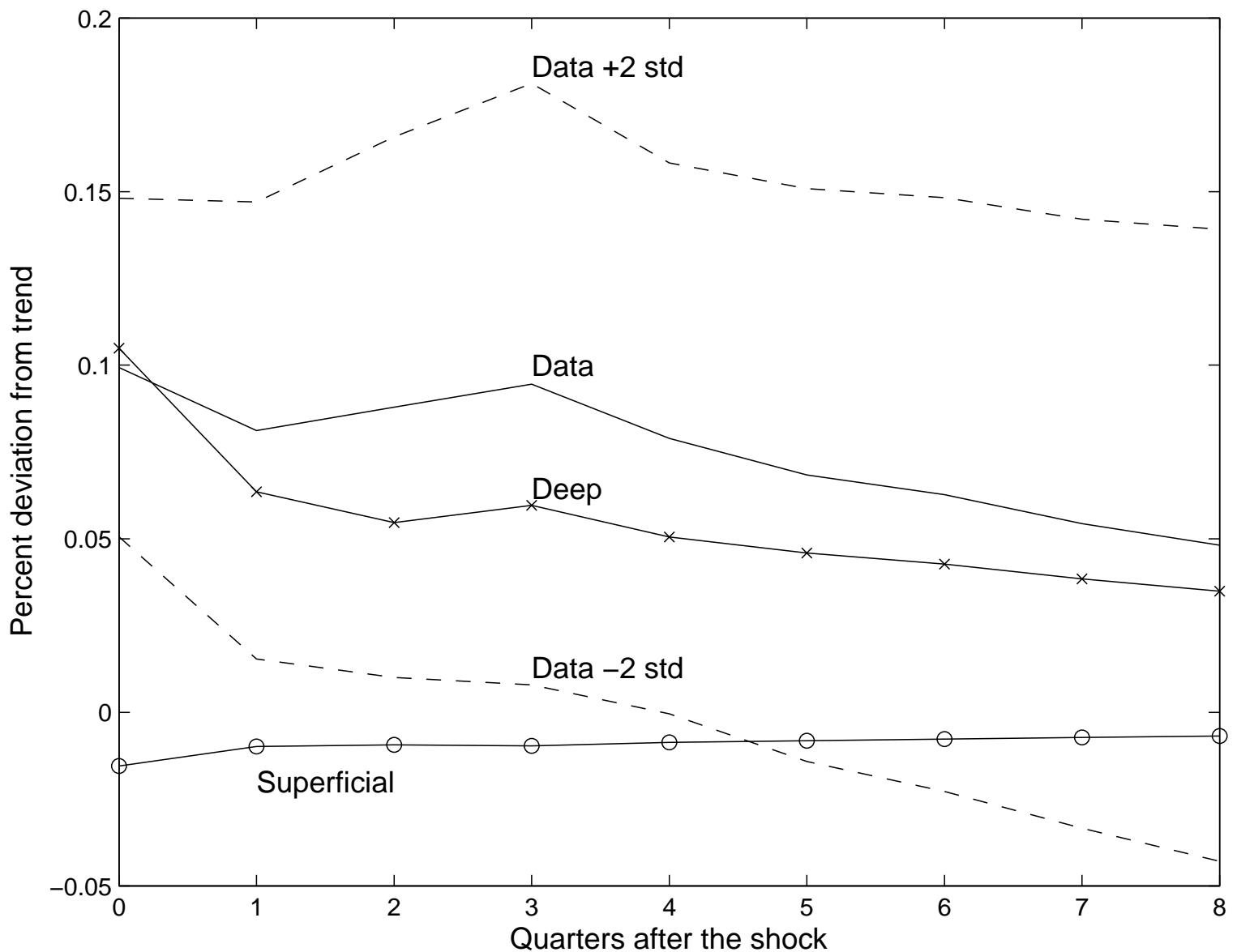
## Response of the Domestic and Foreign Markups to a One-Percent Government Spending Shock



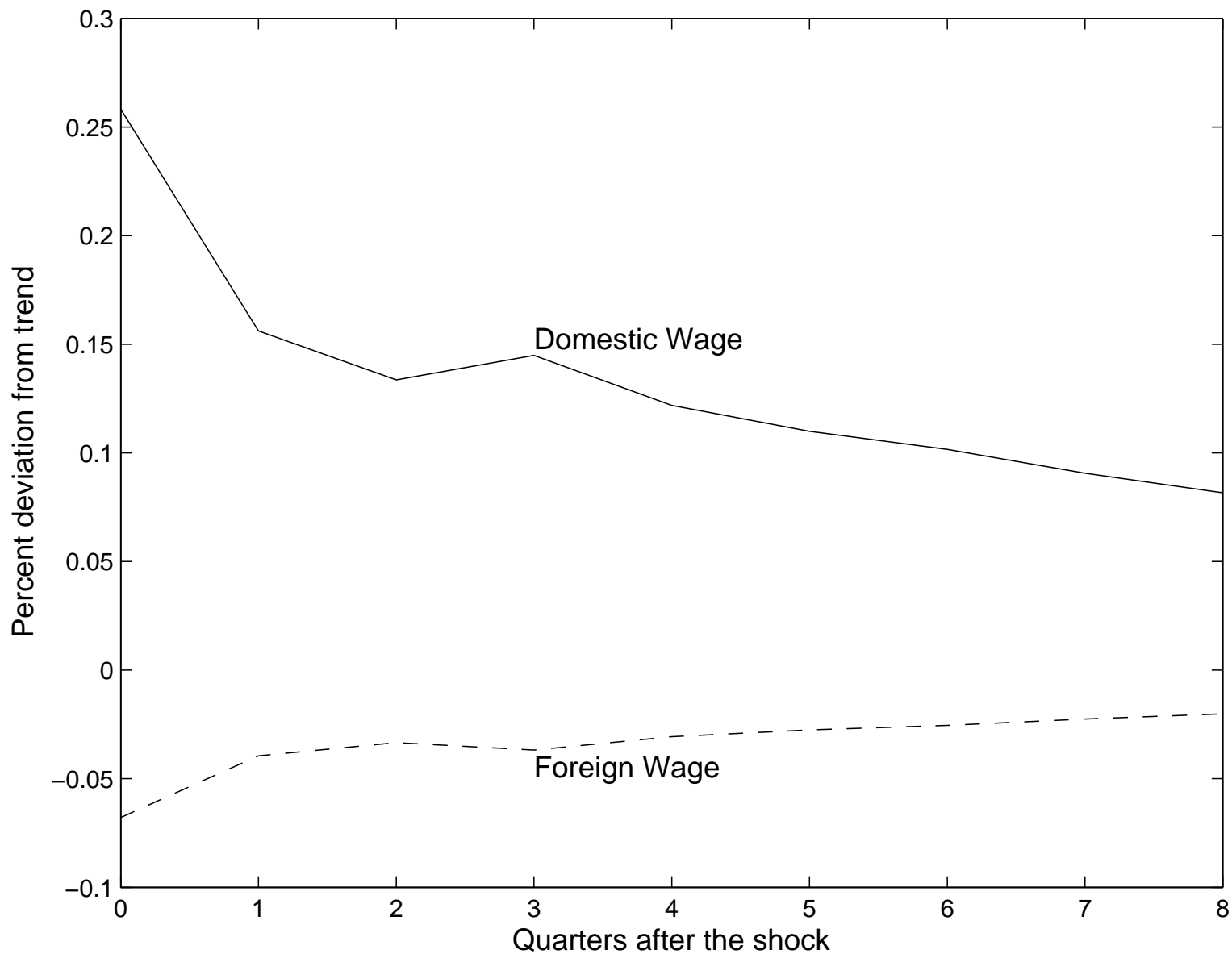
## Response of the Real Exchange Rate to a Government Spending Shock



## Response of Private Consumption to a Government Spending Shock



## Response of the Real Wage to a Government Spending Shock





## Conclusion:

- Under Pricing to Habits there are deviations from the LOOP
- Deviations from the LOOP are time varying
- Pricing to Habits can explain why in response to a demand shock
  - the real exchange rate depreciates
  - private consumption rises
  - the trade balance deteriorates
- Estimation of the model yields:  
 $\theta^c = 0.52$ ,  $\theta^g = 0.57$ , and  $\rho = 0.99$