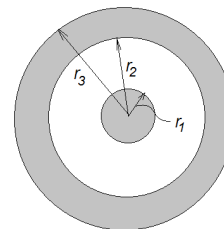


Answer each of the following **three (3)** questions.

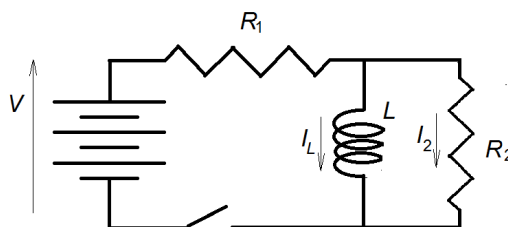
Please give a complete description of your method of solution since *partial credit* will be given.

1. A solid conducting sphere of radius  $r_1$  is surrounded by a concentric conducting spherical shell of inner radius  $r_2$  and outer radius  $r_3$ . The inner conducting sphere carries the charge  $Q$  while the conducting shell has no net charge.



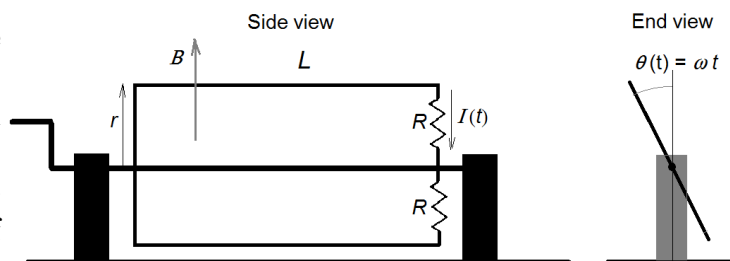
- (a) Find the electric field everywhere in space. [14 points]  
 (b) Determine the charge distributions on the two conductors. [14 points]  
 (c) Find the electrostatic potential of the inner conductor, assuming that the potential vanishes at infinity. [6 points]

2. Consider the circuit on the right composed of two resistors  $R_1$  and  $R_2$ , an inductor  $L$ , a battery of voltage  $V$  with negligible internal resistance and a switch.



- (a) For  $t < 0$  the switch is closed and the circuit is in a steady state. What are the currents  $I_L$  and  $I_2$  flowing in the inductor and resistor? (Label these currents as positive if flowing in the direction of the arrows in the figure.) [5 points]  
 (b) The switch is opened at  $t = 0$  and remains open for all later time. Find the current  $I_2(t)$  as a function of time. [23 points]  
 (c) Sketch an approximate graph of your result for  $I_2(t)$  versus  $t$ . [5 points]

3. A circuit formed from a conducting wire bent into a rectangle of side  $2r$  and length  $l$  is fixed to an insulating rod with a crank at one end, free to rotate about its axis. The conducting rod is interrupted in two places by the insertion of a resistance  $R$  as shown in the figure.



There is a constant, uniform magnetic field  $\vec{B}$  pointing in the vertical direction. The rectangular loop is turned at constant angular velocity  $\omega$  starting at  $t = 0$  in the vertical position.

- (a) Find the current  $I(t)$  flowing through the loop. [12 points]  
 (b) The moving charge (producing  $I$ ) will experience a force from the magnetic field. Find the torque  $\tau(t)$  that must be exerted on the crank to overcome this force and maintain the constant angular velocity  $\omega$ . [12 points]  
 (c) Find the instantaneous power  $P(t)$  dissipated in both resistors at the time  $t$ . [4 points]  
 (d) Calculate the mechanical power that is must be provided to turn the crank. [3 points]  
 (e) Is the power needed to turn the crank equal to that consumed in the resistors? [2 points]