

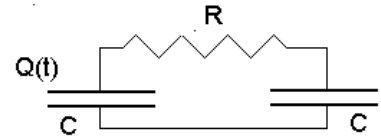
Answer **three (3)** of the following **four (4)** questions. Please give a complete description of your method of solution since *partial credit* will be given.

1. A long straight wire of radius  $R$  carries a total current  $I$ . Assume that the current  $I$  is distributed uniformly over the crosssection of the wire.



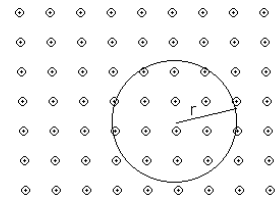
- (a) What is the current density  $\vec{j}$  within the wire? [5 points]  
 (b) Find the magnetic field  $\vec{B}$  outside the wire,  $r \geq R$ . [10 points]  
 (c) Find the magnetic field  $\vec{B}$  inside the wire,  $r \leq R$ . [10 points]

2. Two identical capacitors and a resistor are connected together as shown at the right. Assume that at  $t = 0$  the left capacitor has a charge  $Q_0$  and the right capacitor is uncharged. Find the charge  $Q(t)$  on the left capacitor as a function of time. [25 points]

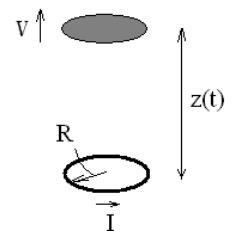


3. Consider a proton with rest energy  $mc^2 = 939MeV$  and charge  $e = 4.8 \cdot 10^{-10}esu$ .

- (a) A proton with energy  $20TeV$  ( $20 \times 10^{12}eV$ ) moves in a region of uniform magnetic field  $\vec{B}$  of magnitude  $50KGauss$ . If the proton's velocity is perpendicular to  $\vec{B}$ , show that it moves in a circle and find that circle's radius. [15 points]  
 (b) A proton with initial velocity  $\vec{v}_0$  enters a region with a uniform electric and magnetic field  $\vec{E}$  and  $\vec{B}$ . If the vectors  $\vec{E}$  and  $\vec{B}$  are orthogonal, what condition must  $\vec{v}$  satisfy if the proton is to move through the region without being deflected? [10 points]



4. A fixed, horizontal, conducting loop of radius  $R$  carries a constant current  $I$ . A uniformly charged, non-conducting disk, also horizontal and of radius  $R$ , is a distance  $z(t)$  directly above the first. You may assume that  $z(t) \gg R$ . The disk carries charge density  $\sigma$ .



- (a) Find the magnetic field due to the current in the fixed loop at the height  $z(t)$ . [10 points]  
 (b) Find the torque  $\vec{\tau}$  exerted on the charged disk if it is moving upward with velocity  $v = \dot{z}(t)$ . [15 points]