

The Comparison of ACI and MCB Methods for Choosing a Set that Contains the Optimal Dynamic Treatment Regime

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Organization of this presentation

- About the project
- Simulation

Goal

The goal of this project is to apply simulation (and clinical data) to find out the probabilities that the two proposed methods will provide a set that includes the optimal DTR(s) in different scenarios, and to assess how good they are performing in excluding other DTRs. The two methods are:

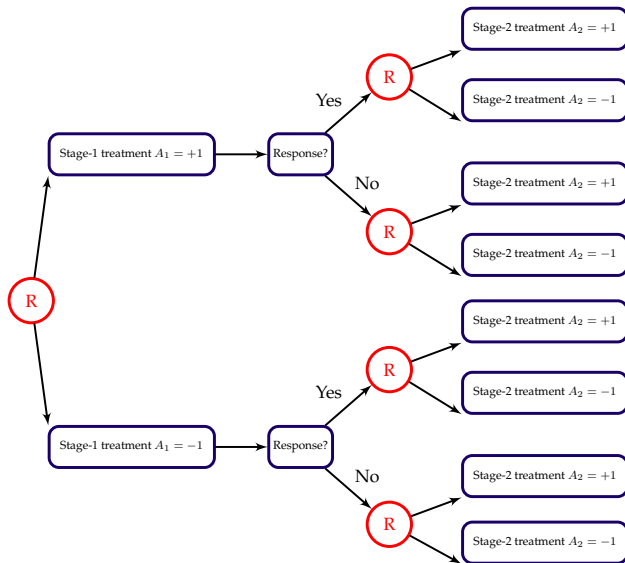
- Adaptive Confidence Intervals (ACI) by Laber et al.
- Multiple Comparisons with the Best (MCB) by Ertefaie et al.

Method

The way to determine whether ACI or MCB is a better method in different scenarios is by comparing:

- The probabilities that the best DTRs are included into the constructed set, and
- The average set size from each method, which is the sum of probabilities of all DTRs within each method.

SMART Design



Scenarios for Data Simulation

Simulations are constructed based on a two-stage SMART and the generative model for final outcome Y is set as follows:

$$Y = \gamma_1 + \gamma_2 X_1 + \gamma_3 A_1 + \gamma_4 X_1 A_1 + \gamma_5 A_2 + \gamma_6 X_2 A_2 + \gamma_7 A_1 A_2 + \epsilon, \epsilon \sim N(0, 1)$$

Scenarios are constructed by setting different values of γ vector $(\gamma_1, \gamma_2, \gamma_3, \gamma_4, \gamma_5, \gamma_6, \gamma_7)$ and δ vector (δ_1, δ_2) that determines $X_2|X_1, A_1$ as $X_2|X_1, A_1 \sim \text{Bernoulli}(\text{expit}(\delta_1 X_1 + \delta_2 A_1))$, $\text{expit}(x) = e^x / (1 + e^x)$

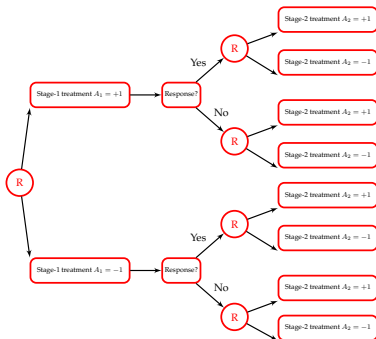
Scenarios for Data Simulation

Scenario One

All **eight** DTRs are equally the optimal ones.

$(\gamma = (0,0,0,0,0,0,0,0), \delta = (0,0))$

Result: MCB performs better than the ACI. (Average set size: 7.699(ACI), 7.5162(MCB))



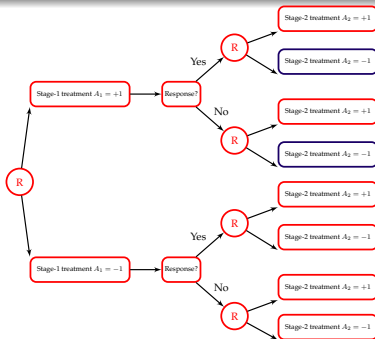
Scenarios for Data Simulation

Scenario Two

If a DTR starts with $A_1 = 1$, we will have a unique better A_2 ; if a DTR starts with $A_1 = -1$, the effect of two A_2 s will be the same. In this way, we will obtain **five** equally best DTRs.

$(\gamma = (0,0,-0.5,0,0.5,0,0.5), \delta = (0,0))$

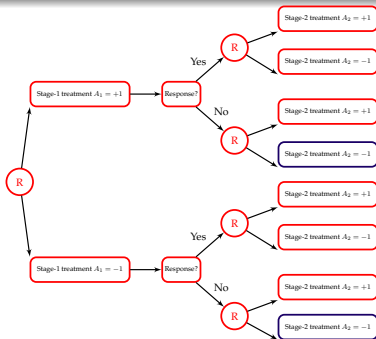
Result: MCB performs better than the ACI. (Average set size: 4.8283(ACI), 4.8174(MCB))



Scenarios for Data Simulation

Scenario Three

Final outcomes are based on response of the first stage treatment. Responders of the first stage have same final outcomes, but non-responders have different expected final outcomes based on A_2 . We have **four** optimal DTRs. ($\gamma = (0,0,0,0,0.5,-0.5,0)$, $\delta = (0,0)$)
Result: MCB performs better than the ACI. (Average set size: 3.8925(ACI), 3.8815(MCB))



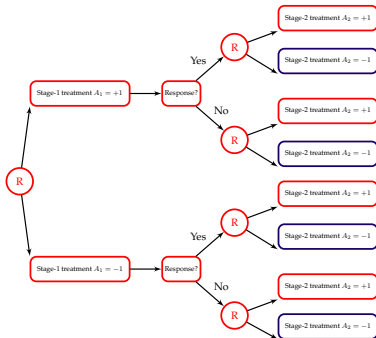
Scenarios for Data Simulation

Scenario Four

Final outcomes are different based on A_1 and A_2 decisions, and only **two** optimal DTRs will be obtained.

($\gamma = (0,0,-1,0,-1,0,-0.5)$, $\delta = (0,0)$)

Result: ACI performs better than the MCB. (Average set size: 1.9585(ACI), 1.98(MCB))



Based on the simulation results in four different scenarios, we recommend MCB method. The reasons are:

- On average, MCB performs better than ACI.
- In real clinical trials, Scenario One is more likely to happen.

We are focusing on real data analysis using the data from Extending Treatment Effectiveness of Naltrexone (EXTEND) study.

Thank you