

# MICRO-SCALE LASER PEEN FORMING OF SINGLE CRYSTAL

Paper (M405)

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## Abstract

As the result of quickly increased requirement in many industrial products resulting from microtechnology, laser thermal micro-forming and micro surface treatment (microscale laser shock peening ( $\mu$ LSP)) have been well studied. By combining the beneficial effects of these two processes with a controlled bending deformation, microscale laser peen forming ( $\mu$ LPF) attracts more attention recently since it not only improves the fatigue life of the material but also shapes micro scale metallic parts at the same time. In the present study,  $\mu$ LSP of single crystal aluminum was presented to study anisotropic material response. Local plastic deformation was characterized by lattice rotation measured through electron backscatter diffraction (EBSD). Residual stress distributions of both sides of a peened sample, characterized by x-ray micro-diffraction, were compared with the results obtained from FEM simulation.  $\mu$ LPF anisotropic behavior was investigated in three effective slip systems via both the anisotropic slip line theory and numerical method. Also, the work hardening effect resulted from self-hardening and latent hardening was analyzed through comparing the results with and without considering hardening.

## Introduction

It is well known that laser shock peening (LSP) can induce desirable compressive residual stresses in the target and improve its fatigue life [1, 2]. Recently, a new forming technology known as laser peen forming (LPF) which is developed from LSP has attracted more attention because of the inherent advantage of LPF. It is undesirable to form large structural components by bending or hydraulic pressing since these processes result in tensile residual stress on surfaces subject to fatigue and stress corrosion cracking. As a result, mechanical shot peen forming was developed and has been successfully used for over 40 years to shape many of these large components. Laser peen forming now can compliment this traditional forming technology and has much greater depth of residual stress, which results in 3 to 8 times greater curvature than can be

achieved with mechanical shot peen forming [3]. Also, compared with shot peen forming, a desired shape may be achieved by laser peen forming with more accuracy and better repeatability, and faster.

Hackel et al. [4] employed a pulse laser beam of an energy fluence 60 to 200 J/cm<sup>2</sup> with a spot size ranging from 3mm×3mm to 6mm×6mm for forming shapes and contours in metal strips. They showed that the laser peen forming process can generate deep compressive stress without inducing unwanted tensile stress at the metal surface and is especially useful for thick (greater than 3/4 inch thick) material that is difficult to shape or contour. Zhou et al. [5] investigated the deformation mechanisms for a special configuration; that is, a sample clamped by two concentric washers. Laser spot size they used ranges from 3 to 10mm in diameter. By using laser peen forming, metal sheet forming is realized without mold and the dimensions of the obtained shapes are determined by the boundary condition. Zhou et al. [6] further studied response of various metal sheets to LPF and presented detailed deformation characterization. The investigation showed its potential to become a flexible manufacturing process with excellent properties and short manufacturing time.

Recently, micro forming becomes a more important technology to manufacture micro metallic parts, in particular for bulk production, because of quickly increased requirement in many industrial products resulting from microtechnology [7, 8]. Laser microforming as a new technology has already been explored for a number of potential high-precision industrial applications, such as laser micro-bending of magnetic disk-drive components, adjustment of contact springs of miniature relays and reed-contacts, and accurate bending of thin plate springs, etc [9, 10]. It can be seen that most of these applications encounter cyclic loadings. Thus, it is desirable to improve fatigue life of micro-parts after microforming process.

Micro-laser peen forming ( $\mu$ LPF) has already attracted some attentions [11]. They showed that compressive stresses, like in the macro LPF process, can also be

induced at the surface of both sides by micro-scale laser peen forming. However, an important consideration in understanding the mechanics of  $\mu$ LPF at the micro-scale is that the laser spot size is likely to be in the same order of magnitude as the average grain size of the target so that the deformation is expected to occur predominately within a small number of grains. Thus in order to accurately model the process, the material properties must be treated as anisotropic and heterogeneous rather than isotropic and homogeneous. In order to gain insight into the deformation and stress fields associated with  $\mu$ LPF, it is advantageous to first apply the process to single crystal so that the effects of the anisotropy can first be identified in a homogeneous material.

In this paper, the effects of micro-scale laser peen forming on single crystal aluminum are studied by using both numerical and experimental methods. Beside residual stress distribution measured by x-ray micro-diffraction, peen formed crystal samples are also characterized by profilometer curvature measurement and lattice rotation of electron backscatter diffraction (EBSD). In addition, a preliminary numerical simulation based on single crystal plasticity was presented to understand the process of  $\mu$ LPF, especially anisotropy and effect of strain hardening. Anisotropic slip line theory was employed to compliment the numerical simulation to explain the stress and deformation state resulting from laser peen forming on a single crystal surface under plane strain conditions. Through the presented work, we can grab some main features of micro-scale peen forming and shed some shine for future work on understanding heterogeneity and associated problems of the ultra-high strain rate plastic deformation related to laser shocking.

### Experiment Conditions

A frequency tripled Q-switched Nd:YAG laser ( $\lambda = 355 \text{ nm}$ ) in  $\text{TEM}_{00}$  mode was used in micro-scale laser peen forming and the parameters of pulse duration, wavelength and beam diameter are shown in Fig. 1. If a line loading is applied parallel to a  $\langle 110 \rangle$  direction in a FCC crystal, certain slip systems act cooperatively which enable approximate plane strain deformation conditions to be achieved [12]. Therefore, a line of  $\mu$ LSP shocks parallel to a  $\langle 110 \rangle$  direction was created on the sample surface with a  $25\mu\text{m}$  spacing because this spacing results in approximate 2-D deformation. Pulse energies, 202 and  $280\mu\text{J}$ , corresponding to laser intensities of  $3.57$  and  $4.95\text{GW}/\text{cm}^2$ , respectively, were applied. A thin layer of high vacuum grease (about 10 microns thick) was

spread evenly on the sample surface to isolate the thermal effect from the coating, and a  $16\mu\text{m}$  thick polycrystalline aluminium foil, chosen for its relatively low threshold of vaporization, was tightly pressed onto the grease. The sample was placed in a shallow container filled with distilled water around 1 mm above the sample's top surface to confine the produced plasma. The induced deformation is due to shock pressure and not due to thermal effects since only the coating is vaporized during the process [2].

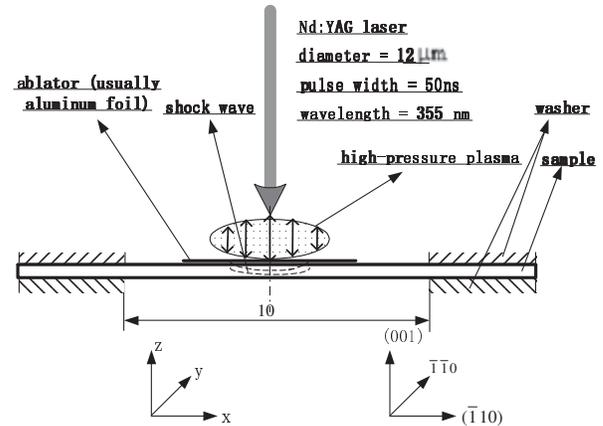


Fig. 1 Sample geometry and laser peen forming condition

In order to investigate the effects of specimen thickness under the same laser energy, the samples of single crystal aluminium with  $150\mu\text{m}$ ,  $200\mu\text{m}$  and  $300\mu\text{m}$  thickness have been chosen, which have normal orientation of (001) as shown in Fig. 1. The samples were cut to the dimension of  $20\text{mm} \times 3\text{mm}$  by using wire electrical discharge machining (EDM) and mounted to holders as shown in Fig.1 carefully to make them as flat as possible. The sample surface on both sides was polished mechanically first, in order to remove the thermal affected layer by EDM, and then electro-polished to eliminate residual stress. Before shocking process, the pre-bending is measured by using a Mitutoyo SJ-201P profilometer as shown in Fig. 2 and the samples with a pre-bending less than  $8\mu\text{m}$  were chosen to minimize the pre-bending effects.

### Post Peen Forming Material Characterization

After laser peen forming, the sample was characterized by curvature change, residual stress distribution and lattice rotation. The first characterization is necessary for studying capability of micro-scale curvature adjustment by  $\mu$ LPF and second for its potential to improve fatigue life. Lattice rotation, accounting for the rotation part in the polar decomposition of elastic deformation, is induced by plasticity and can be quantitative analyzed by electron backscatter

diffraction (EBSD). Thus, we can directly compare the experimental results of lattice rotation with simulation results.

The curvature change is characterized by using profilometer measurement, whose range in depth direction is 350 $\mu\text{m}$  with the resolution 0.4 $\mu\text{m}$ . The measuring force is 4mN, which assures the detector has no bending effect on the samples while measuring. Residual stresses were estimated from x-ray micro-diffraction profiles, which were collected from Beamline X20A (synchrotron radiation sources) at National Synchrotron Light Source at Brookhaven National Lab. X-ray of X20A can be focused by a tapered glass capillary to spot sizes as small as 3 microns. Complete details of x-ray micro-diffraction experiment and the corresponding evaluation method of sub-profile analysis can be found in Chen, et al.[13] For lattice rotation, the crystallographic orientation of peened area for both top and bottom surfaces was collected using EBSD, which provided information about the lattice rotation on the shocked area. EBSD data was collected using a system supplied by HKL Technology and attached to a JEOL JSM 5600LV scanning electron microscope.

### FEM Simulation Conditions

In order to further understand  $\mu\text{LPF}$  process, the numerical simulation of micro-scale peen forming on the single crystal aluminum was carried out by using quasi-static loading. The numerical simulation will allow more precise understanding of anisotropy effects associated with  $\mu\text{LPF}$ . In addition, the lattice rotation is calculated numerically and residual stress can be estimated. Subsequent simulations which account for more realistic material constitutive behavior, as well as accounting for inertial contributions, will concentrate on how the additional effects modify the baseline solution. Thus, it is expected that these simulations will lay the ground work for more realistic simulations.

Finite element simulations based on single crystal plasticity [14] were carried out with a user-material subroutine (UMAT), which was written by Huang<sup>15</sup> and modified by Kysar [16]. It is incorporated into the finite element analysis using the general purpose finite element program ABAQUS/Standard. In the UMAT, the  $\{111\}\langle 110\rangle$  slip systems in FCC metal are employed and a critical resolved shear strength  $\tau_{CRSS} \approx 1\text{MPa}$  is assumed for each of the slip systems. The element used in the simulation was a plane strain reduced integration, hybrid element (CPE4RH) and total simulation size is 384 $\mu\text{m}$ ×192 $\mu\text{m}$  (thickness×width). The mesh size is about 0.1 $\mu\text{m}$  in the area close to the loading and 1.5 $\mu\text{m}$  far away from the

loading. As for boundary conditions of the plane strain model, the applied surface tractions correspond to the applied pressure on the shocked surface. At the bottom surface, the vertical displacement is specified to be zero and the outer edges are traction free. In the simulation, elastic-ideally plastic behavior is assumed. The simulation ignores rate and inertial effects. The loading on the surface has a Gaussian distribution:

$$P(x) = P_0 \exp\left(-\frac{x^2}{2R^2}\right), \text{ where } x \text{ is the radial distance}$$

from the center of the laser beam and  $R$  is the radius of plasma. Following Zhang and Yao [17], the resulting plasma radius is  $R = 9.5\mu\text{m}$  at the end of the laser pulse for the laser beam diameter 12 $\mu\text{m}$ . The plasma is expected to expand further after 50ns, but the resulting pressure decreases very quickly so that effect is ignored [2, 17]. The simulation is divided into two steps, loading and relaxation step, and the maximum magnitude of applied pressure is determined by trial and error method. The pressure magnitude was varied until the simulation result of curvature change matched experimental findings. Rate dependence used is a power-law relationship proposed by Hutchinson [18] and described by Connolly and McHugh [19], Huang [15], Kysar [20], Peirce et al. [21], and Savage et al. [22]:

$$\dot{\gamma}_k = \dot{\gamma}_0 \text{sgn}\tau_k \approx \left\{ \left| \frac{\tau_k}{g_k} \right| \right\}^m \quad (1)$$

where is  $\dot{\gamma}_0$  the reference strain rate,  $\tau_k$  is the applied resolved shear stress,  $m$  is the rate sensitivity exponent, and  $g_k$  is related to critical resolved shear stress of the  $k$ th-slip system, as given by Peirce et al.<sup>21</sup> In this simulation,  $\dot{\gamma}_0 = 10^{-3}$  and  $m = 50$ .

### FEM Simulation with Work Hardening

In LPF, the target is subjected to very strong shock pressures (>1 GPa), the interaction time is very short (<100 ns), and the strain rate is very high (>100,000  $\text{s}^{-1}$ ). A review of the constitutive equations for such high strain rates was given by Meyer [23]. The simplest model to describe the work hardening behavior of metals is Ludwik equation:  $Y = A + B\varepsilon^n$  at ambient temperature and quasistatic loading, where  $Y$  is the yield strength,  $n$ ,  $A$  and  $B$  are material constants, and  $\varepsilon$  is the equivalent plastic strain. For single crystals of face-centered-cubic (FCC) metals, work hardening experiences three stages [24]. During stage I, dislocations move on a single set of parallel slip planes and there is little work hardening. Stage II hardening

starts when intersecting slip systems are activated and dislocations moving on the intersecting glide planes entangle each other. Dislocation density increases rapidly with increasing strain in stage II. At higher strains, stage III happens when the rate of work hardening diminishes with increasing strain because screw dislocations can cross-slip from one slip plane to another and so by-pass obstacles and annihilate dislocations of opposite sign in neighboring planes at sufficiently high stresses. For most polycrystalline cubic metals, stage III work hardening is the dominant mode observed in tests on most at room temperature. Because approximately linear stage II hardening may be present in the early stages of straining, Ludwik equation is often poor at low strains for FCC single crystals of metals.

In this paper, Asaro's hardening theory of single crystal [14] has been applied, in which the critical shear stress  $\tau_0^k$  of the Schmid law is determined by the current dislocation density and substructure, and represents variation of hardness of material due to work hardening. Since work hardening of slip system depends on shear deformation of slip systems, variation of  $\tau_0^k$  may be estimated by

$$\Delta\tau_0^k = h_1^k |\Delta\gamma_1| + h_2^k |\Delta\gamma_2| + h_3^k |\Delta\gamma_3| + h_4^k |\Delta\gamma_4| + \dots = \sum_i h_i^k |\Delta\gamma_i| \quad (2)$$

where  $h_i^k$  expresses hardening rate against increment of shear deformation  $\Delta\gamma_i$  on each slip system. When  $k$  equals to  $i$ ,  $h_i^k$  represents hardening by glide on its own slip system. When  $k$  is not the same as  $i$ ,  $h_i^k$  represents hardening by glide on other slip systems. The former is called the self hardening, and the latter is called the latent hardening. It is found that latent hardening rate does not depend on combination of slip systems. The ratio denoted by  $q$  between latent hardening rate and self hardening rate can be evaluated by the following equation [14]:

$$h_i^k = qh + (1-q)h\delta_{ij} = h \begin{bmatrix} 1 & q & q & \dots & q \\ q & 1 & q & \dots & q \\ q & q & 1 & & \vdots \\ \vdots & \vdots & & \ddots & q \\ q & q & \dots & q & 1 \end{bmatrix} \quad (3)$$

and  $q=1.4$  is best to match simulation with experimental results. Where  $h$  is given by

$$h = h_0 \operatorname{sech}^2 \left( \frac{h_0 \gamma}{\tau_{\max}^k - \tau_0^k} \right)$$

$$\gamma = \sum_i |\Delta\gamma_i|$$

where  $\tau_{\max}^k$  is the maximum value of yield shear stress,  $\tau_0^k$  is the initial value of yield shear stress, and  $h_0$  is a material constant. In this paper,  $h_0 = 8.9\tau_0$  and  $\tau_{\max}^k = 1.8\tau_0$  are used [14].

## Results and Discussion

### Curvature Changes

Our previous work [11] showed that 100 $\mu\text{m}$  poly copper with 3.57GW/cm<sup>2</sup> laser intensity was bent downward while the same sample was bent upward with high energy of 4.95GW/cm<sup>2</sup> intensity. In this paper, in order to verify deformation mechanism of LPF, these two levels of laser energy were used for single crystal aluminium as well, but the minimum thickness of 150 $\mu\text{m}$  was selected instead of 100 $\mu\text{m}$  because single crystal aluminium is much softer than poly copper sample. For the aluminium single crystal, as it can be seen in Figs. 3 and 4, 150 $\mu\text{m}$  thick sample was bent downward with low laser energy of 3.57GW/cm<sup>2</sup> intensity and bent upward with 4.95GW/cm<sup>2</sup> intensity. This trend is consistent with the case of poly copper samples and detailed explanation can be found in our previous work [11]. In order to examine thickness effects, we have also applied laser shocks of the same intensity (3.57GW/cm<sup>2</sup>) onto specimens with different thickness. Fig. 2 shows the curvature change of 200 $\mu\text{m}$  and 300 $\mu\text{m}$  thick samples and it can be seen that the curvature change become smaller as thickness increases. For the 200 $\mu\text{m}$  sample, it was bent downward 11 $\mu\text{m}$  and the corresponding bending angle is about 0.13 $^\circ$ .

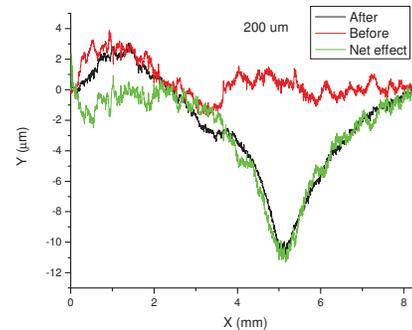


Fig. 2 Curvature measurement on the bottom side before and after peen forming for 200 $\mu\text{m}$  sample with 3.57GW/cm<sup>2</sup> laser intensity

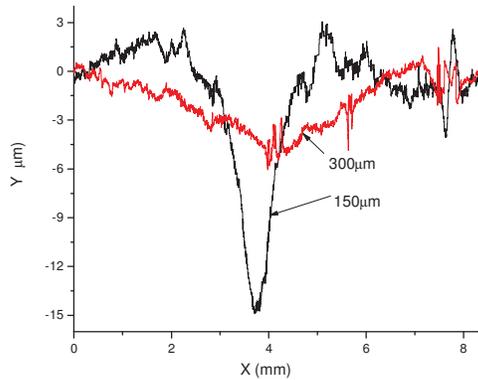


FIG. 3 Curvature measurement for 150um and 300um sample with low energy

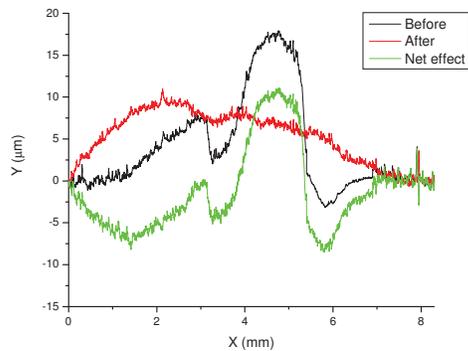


Fig. 4 Curvature measurement for 150um with high energy

### Residual Stress Distribution

In order to spatially resolve the residual stress induced by  $\mu$ LPF, measurements were made on both top and bottom surfaces along the lines perpendicular to the peened line. The spacing between adjacent measurement points is  $10\mu\text{m}$  and the corresponding x-ray diffraction profile at each position is recorded and repeated for each scan line. Fig. 5 shows the residual stress distribution for  $200\mu\text{m}$  sample with laser energy of  $3.57\text{GW}/\text{cm}^2$ . It can be seen that a compressive residual stress is generated near the center of peened region on the bottom side and there is a tensile residual stress near the center bordered by a region of compressive stress on the top side. Although the laser spot size is only  $12\mu\text{m}$ , the high shock pressure in  $\mu$ LPF can generate significant compressive residual stresses over a much larger region, up to  $200\mu\text{m}$ . For  $150\mu\text{m}$  samples with two laser energy levels, residual stress distributions are shown in Fig. 6. Measurements indicate that high laser energy of  $4.95\text{GW}/\text{cm}^2$  intensity induces compressive residual stress in both sides and the pattern with low energy of  $3.57\text{GW}/\text{cm}^2$  is the same as the one of  $200\mu\text{m}$ . Similar to the results

of previous work [11], the pattern of residual stress corresponds to the bending mechanism; that is, for bending upward, residual stresses are compressive on both sides and tensile on the top and compressive on the bottom for bending downward.

Fig. 7 shows the simulation results of residual stress contour for  $200\mu\text{m}$  sample with  $3.57\text{GW}/\text{cm}^2$  laser intensity. Residual stress patterns for the case when we observe downward bending are in good agreement with the experimental results for different thickness. However, for upward bending case of  $150\mu\text{m}$  thick specimen under laser intensity  $4.95\text{GW}/\text{cm}^2$ , the simulation model is limited to grab the corresponding curvature change because of quasi-static loading.

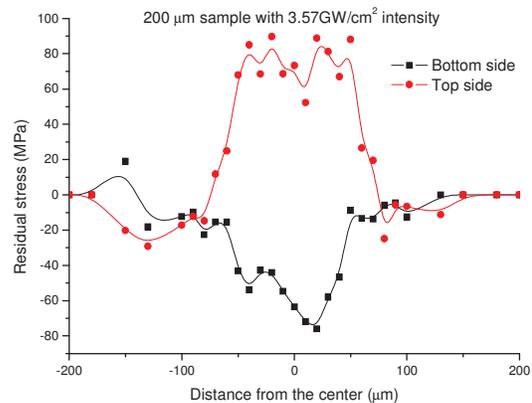


Fig. 5 Residual stress distribution by X-ray micro-diffraction for  $200\mu\text{m}$  sample

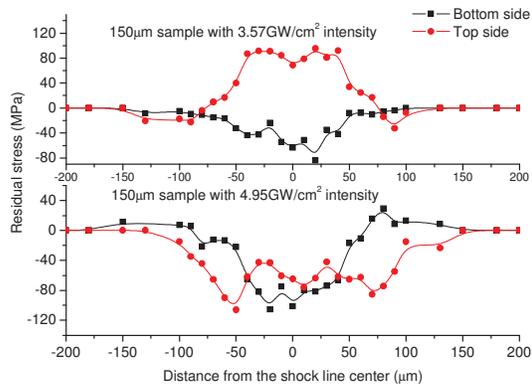


Fig. 6 Residual stress distribution by X-ray micro-diffraction for  $150\mu\text{m}$  with two laser energy levels

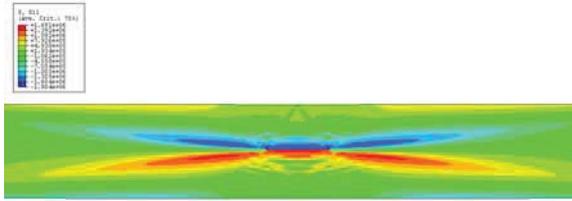


Fig. 7 Residual stress contour by FEM simulation

### Lattice Rotation Field by EBSD

All EBSD data were acquired in the automatic mode, using external beam scanning and employing a  $3\mu\text{m}$  step size. The scan area is about  $350\mu\text{m}\times 150\mu\text{m}$  on the shocked region as shown in Figs. 8(a) and (b), respectively. The EBSD results from each individual scan comprise data containing the position coordinates and the three Euler angles which describe the orientation of the particular interaction volume relative to the orientation of the specimen in the SEM, allowing the in-plane and the out-of-plane lattice rotations to be calculated relative to the known undeformed crystallographic orientation, which serves as the reference state.

The lattice rotation contour map of bottom surface is shown in Fig. 4 (a) for  $200\mu\text{m}$  sample. Fig. 4(b) shows the lattice rotation contour map for the top side. The red region corresponds to counter-clockwise rotation about the y-axis (as defined in Fig. 1) which is positive and the blue region corresponds to clockwise rotation which is negative. Similar to  $\mu\text{LSP}$  process, the lattice rotation on top surface caused by  $\mu\text{LPF}$  is zero (green region) far away from the shocked line which corresponds to the shock-free region. The lattice rotation distribution along the shocked line is quite uniform which suggests the approximate two-dimensional deformation state mentioned before. The lattice rotation value is up to  $\pm 3^\circ$  between  $\pm 120\mu\text{m}$  from the center of shocked line on the top surface and the rotation direction is anti-symmetric about the shock line on both sides. The rotation contour of bottom side approximately corresponds to the bending curvature since lattice rotation in each side of shock line is almost constant and rotation value is close to the bending angle. The difference is because that the bending angle measured by Profilometer reflects overall curvature while lattice rotation represents the bending angle close to shock line.

Fig. 9 presents the lattice rotation contours for  $150\mu\text{m}$  and  $300\mu\text{m}$  samples' top surface with low energy of  $3.57\text{GW}/\text{cm}^2$ . They showed similar patterns as that of  $200\mu\text{m}$  sample, but the maximum angle of lattice rotation is different and corresponds to the thickness.

Maximum rotation angle decreases as the thickness increases, for example,  $3.5^\circ$  for  $150\mu\text{m}$ ,  $3^\circ$  for  $200\mu\text{m}$  and  $2^\circ$  for  $300\mu\text{m}$  sample, because of harder bending when the thickness increases. Lattice rotation by simulation for  $200\mu\text{m}$  is shown in Fig. 10, which shows the same contour for both sides and is corresponding to the experimental of bottom side. But for the top surface feature of lattice rotation, it is impossible to be grabbed by simulation with quasi-static loading. Therefore, it is necessary to carry out simulation under dynamic loading condition in future.

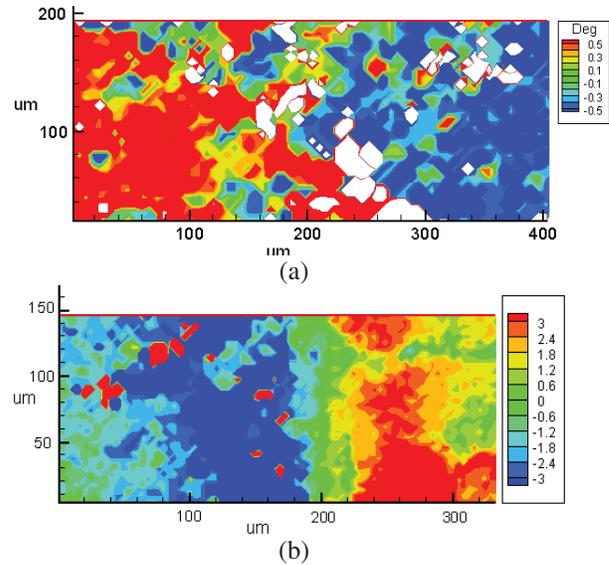


Fig. 8 Lattice rotation distribution by EBSD measurement for  $200\mu\text{m}$  sample with  $3.57\text{GW}/\text{cm}^2$  laser intensity: a) bottom side; b) top side

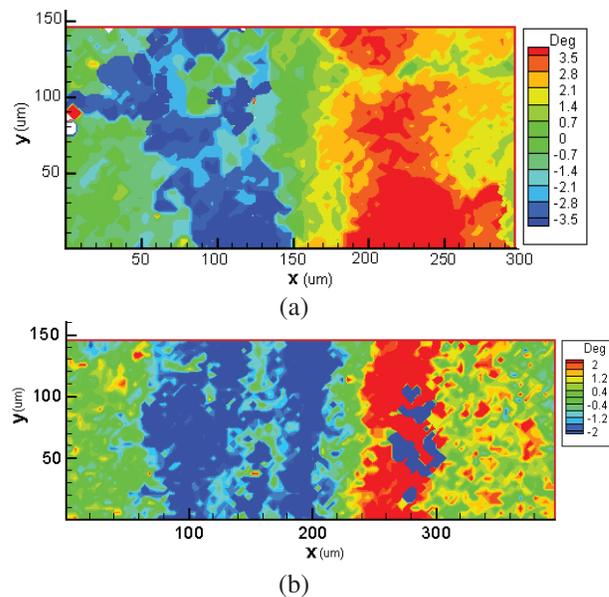


Fig. 9 Lattice rotation by EBSD for 150um and 300um sample top side with low energy: a) 150um; b) 300um



Fig. 10 Lattice rotation contour by FEM simulation for 200um sample

### Shear Strain Distribution in Each Slip System

Fig.11 shows the shear strain distribution for the three slip systems as well as the total shear strain by FEM simulation without considering work-hardening; that is, Fig. 11(a) shows the distribution of slip system *i* and the distribution of slip system *iii* is symmetric with that of slip system *i* and shear strain is almost zero for slip system *ii* so that it is not included in Fig.11. It can be seen that plastic deformation is caused mainly by slip system *i* and *iii* because Schmid's factor is zero for slip system *ii*. It is of great interest to understand the logics behind these shear distributional pattern for each slip system. In this paper, anisotropic slip line theory is applied to preliminary explain these distributions.

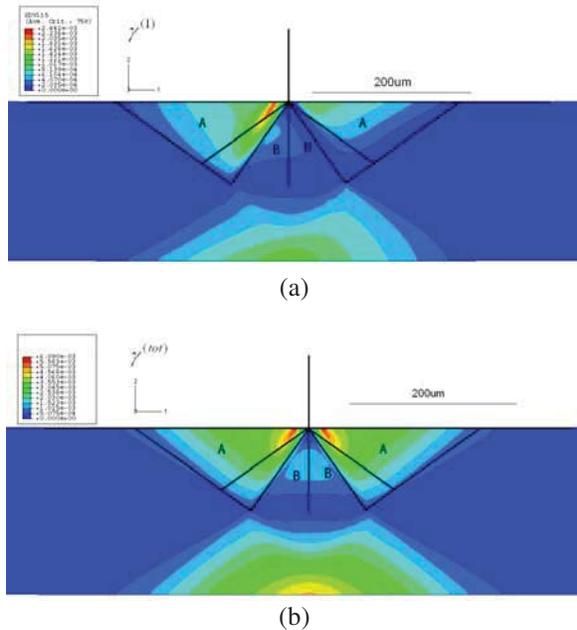


Fig. 11 Shear strain contour in slip system: a) slip system *i*; b) total shear strain

Construction of slip field According to the anisotropic slip line theory [12, 20, 29] when loading is applied along (110) direction in FCC crystals three out of twelve slip systems will be activated. Rice [29] employed anisotropic slip line theory to solve punch problem. Wang et al. extended this work to the  $\mu$ LSP, where laser induced Gaussian pressure loading is approximated as punch with non-uniform pressure distribution. Furthermore in  $\mu$ LSP domain of interest is considered to be semi-infinite and deformation is local. On the other hand in  $\mu$ LPF case nature of deformation mechanism is different and global deformation has to be taken into account. Width of Gaussian pressure loading is order of magnitude smaller than width of specimen, thus from global point of view it can be assumed to be point load that causes bending. Therefore following [12, 29], center of the Gaussian pressure loading can be seen as the point of singularity in which centered fan is placed. Slip line field constructed in such way is depicted in Fig. 12. Comparison of proposed explanation shows good agreement with numerical simulation, as shown in Fig. 11(b) for the total shear strain distribution. It also agrees well with the numerical solution of shear strain distribution for slip system *i*. However, this issue requires further attention, more detailed analytical study of stress field based on the anisotropic slip line theory is required, which would lead to closed form solution of this problem.

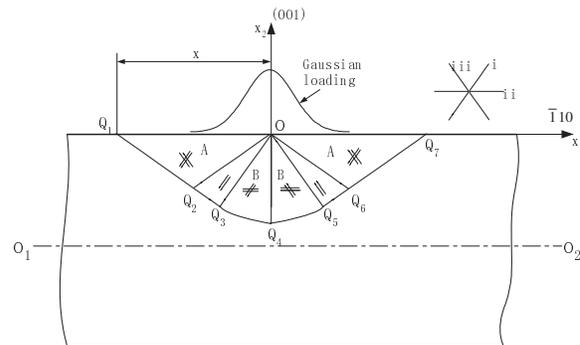


Fig. 12 Geometry of slip line field for a Gaussian distribution of peen forming

### Effect of Work Hardening

In order to lay some ground for future realistic numerical simulation, which account for the material behavior under high dynamic loading with extreme high strain rate ( $10^7 \sim 10^9 \text{ s}^{-1}$ ) including both work hardening and strain rate effects on LPF, here we only consider the effects of work hardening first to simplify the problem.

As expected, the target is hard to be deformed when encountering effects of work hardening. Fig. 13 shows the difference of the bending curvature for the single crystal aluminium sample with and without considering work hardening for the same simulation condition. The maximum displacement with work hardening consideration is around  $7\mu\text{m}$  and without work hardening is about  $10\mu\text{m}$ . For work hardening effects on total shear strain corresponding to Fig. 11(b), it is found that work hardening almost has no effect on the plastic deformation width under the previously defined simulation conditions, but the maximum of total shear strain on the top surface is reduced almost 40% if work hardening is considered, as shown in Fig. 14. In addition, it is of great interest to look into shear strain distribution in each slip system with work hardening effects because anisotropic character associated with micro-scale laser peen forming is observed in FEM simulation results under quasi-static loading without considering work hardening and high strain rate effects. Comparing simulation results of shear strain distribution in each slip system without and with work hardening, it is found that the patterns and effected area is same for these two conditions. Therefore, we have more confidence that this anisotropy is more likely associated with  $\mu\text{LPF}$ , but the magnitude of shear strain will become smaller if considering high strain rate effects.

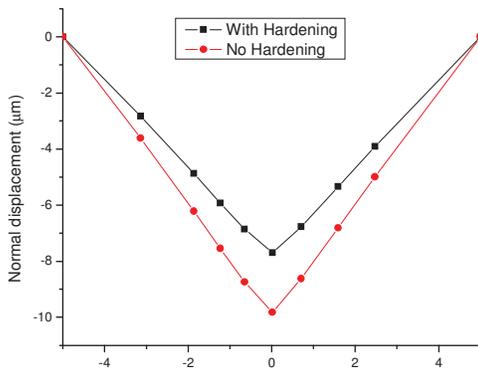


Fig. 13 Normal displacement of FEM simulation with and without work hardening

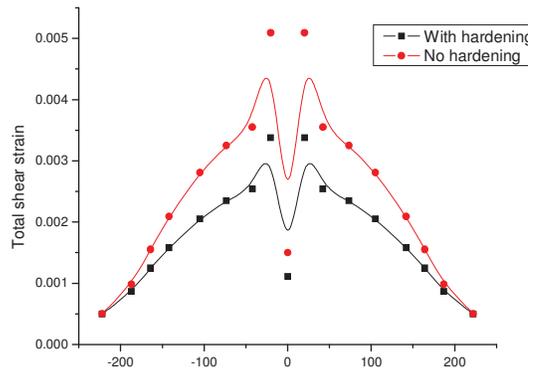


Fig. 14 Total shear strain contour of FEM simulation with work hardening

## Conclusions

In this paper,  $\mu\text{LPF}$  of single crystal aluminum with orientation [001] under approximate plane strain condition was investigated using both, experimental and numerical methods. Construction of the slip line field is proposed. Like  $\mu\text{LSP}$ , it was found that the potential exists for rapid changes in field variables for  $\mu\text{LPF}$  as well. The lattice rotation field under laser peen forming is found to be anti-symmetric on both top and bottom surfaces and top side is similar as that of  $\mu\text{LSP}$ , but bottom side is proximately accounting for the curvature slope of global deformation. The magnitude of lattice rotation on the top surface increases when sample thickness becomes thinner, such as  $\pm 2^\circ$  for  $300\mu\text{m}$ ,  $\pm 3^\circ$  for  $200\mu\text{m}$  and  $\pm 3.5^\circ$  for  $150\mu\text{m}$ , and lattice rotation covers a region around  $\pm 150\mu\text{m}$  across the shock line. Compared with previous work of  $\mu\text{LPF}$  on the polycrystalline copper, it was found that anisotropy has little effect on bending mechanisms. Similarly, residual stresses are compressive on bottom side for both upward and downward bending of single crystals, and are tensile on top side for bending downward and compressive for bending upward. The methodologies and results presented herein enable a systematic study of the micro scale laser peen forming process and shed some light on understanding laser peen forming process under micro scale length.

## Acknowledgement

This work is supported by the National Science Foundation under grants DMI-02-00334 and DMI-06-20741. JWK would like acknowledge support by the National Science Foundation under the Faculty Early Career Development (CAREER) Program with grant

CMS-0134226. Single crystal sample preparation provided by Dr. Yongxue Gang is also acknowledged.

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